

STRUCTURAL AND MORPHOLOGICAL PROPERTIES OF ULTRALUMINOUS INFRARED GALAXIES AT $1 < z < 3$

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Abstract. Using the Hubble Space Telescope (HST)/Wide Field Camera 3 (WFC3) near-infrared high-resolution imaging from the 3D-HST survey, we analyze the morphology and structure of 502 ultraluminous infrared galaxies (ULIRGs; $L_{\text{IR}} > 10^{12} L_{\odot}$) at $1 < z < 3$. Their rest-frame optical morphologies show that high-redshift ULIRGs are a mixture of mergers or interacting systems, irregular galaxies, disks, and ellipticals. Most of ULIRGs in our sample can be roughly divided into merging systems and late-type galaxies (Sb–Ir), with relatively high M_{20} (> -1.7) and small Sérsic index ($n < 2.5$), while others are elliptical-like (E/S0/Sa) morphologies with lower M_{20} (< -1.7) and larger n (> 2.5). The morphological diversities of ULIRGs suggest that there are different formation processes for these galaxies. Merger processes between galaxies and disk instabilities play an important role in the formation and evolution of ULIRGs at high redshift. In the meantime, we also find that the evolution of the size (r_e) with redshift of ULIRGs at redshift $z \sim 1 - 3$ follows the relation $r_e \propto (1+z)^{-(0.96 \pm 0.23)}$.

Key words: galaxies: evolution – galaxies: fundamental parameters – galaxies: structure – galaxies: high-redshift

1. INTRODUCTION

ULtraluminous InfraRed Galaxies (ULIRGs; $L_{8-1000 \mu\text{m}} > 10^{12} L_{\odot}$) were first hinted at by the deep InfraRed Astronomical Satellite (IRAS; Neugebauer et al. 1984) surveys. Within the past decade, observations have shown that high-redshift ULIRGs are massive galaxies ($M_{*} > 10^{10} M_{\odot}$) with an extremely high ratio of infrared to optical flux density ($F(24 \mu\text{m})/F(R) > 1000$) and intensive star formation ($100-1000 M_{\odot} \text{ yr}^{-1}$) (Chapman et al. 2003; Houck et al. 2005; Yan et al. 2007; Dey et al. 2008; Desai et al. 2009; Huang et al. 2009; Fang et al. 2014). At high redshift there are many samples of pre-selected ULIRGs, such as Dusty-Obscured Galaxies (DOGs with $(R - [24])_{\text{Vega}} > 24$; Houck et al. 2005), Submillimeter Galaxies (SMGs with $F(850 \mu\text{m}) > 0.5 \text{ mJy}$; Chapman et al. 2003), and Multiband Imaging Photometer for *Spitzer* (MIPS) $24 \mu\text{m}$ selected samples (Yan et al. 2007), and follow-up analysis is then necessary to single out ULIRGs.

Since the discovery, ULIRGs have been suggested to be a feasible evolutionary phase towards the formation of local massive early-type galaxies (Sanders et al. 1988; Veilleux et al. 2009; Hou et al. 2011). But, the existence of a large number of massive galaxies with $M_* > 10^{10} M_\odot$ at $z \sim 2 - 3$ challenges the merge theory which implies that massive galaxies assemble at a later time through the merge of smaller galaxies (Narayanan et al. 2009). During the gas-rich major merger, intense star formation is triggered and the dust-enshrouded galaxies can be identified as ULIRGs (Wu et al. 1998). At the same time, it is possible that the gas can be fed into the central massive black holes as quasars. There are many structural features of mergers, such as multiple bright nuclei, tadpoles (appear to have undergone a merger by evidence of tails), irregular shapes, pairs of galaxies depending on the merge stages or the types of merger. Therefore, morphological and structural studies of $z \sim 2$ ULIRGs, with or without merger features, can help us to understand the formation and evolution of massive galaxies (Shen et al. 2003; Sandage 2005; Ball et al. 2008; Kong et al. 2006, 2009; Fang et al. 2009, 2012).

For galaxies at $1 < z < 3$, Hubble Space Telescope (HST)/Wide Field Camera 3 (WFC3) near-infrared (NIR) imaging can provide crucial clues to the rest-frame optical morphologies ($\lambda_{\text{rest}} \sim 5000 \text{ \AA}$). At such redshift, the HST/WFC3 NIR bands have not yet reached the Balmer break ($\lambda_{\text{rest}} \geq 4000 \text{ \AA}$) and probe redder wavelengths. This enables us to study the rest-frame optical morphologies and structures of ULIRGs at $1 < z < 3$. By using HST NIR images (NICMOS or WFC3), many groups (Dasyra et al. 2008; Melbourne et al. 2008, 2009; Busmann et al. 2009, 2011; Zamojski et al. 2011; Kartaltepe et al. 2012) found that the morphologies of ULIRGs are diverse, e.g., disks, bulges, multiple components, and irregulars. This implies that ULIRGs may have different formation processes such as mergers and secular evolution without mergers.

Since the samples of previous research programs are commonly small (< 80 for ULIRGs at $1 < z < 3$), it still remains many uncertainties on the structural properties of ULIRGs. This paper constructs a sample of 502 ULIRGs from the 3D-HST survey¹ (Brammer et al. 2012; Skelton et al. 2014). Moreover, comparing with previous studies based on HST/NICMOS F160W images ($0''.09 \text{ pixel}^{-1}$), this work will utilize HST/WFC3 NIR images ($0''.06 \text{ pixel}^{-1}$) to investigate the morphological diversities of high-redshift ULIRGs, and for the first time we explore the size evolution with redshift of our sample and calculate nonparametric morphological parameters of ULIRGs at $1 < z < 3$. Section 2 describes the selection of ULIRGs and the data (include images and catalogs) from the 3D-HST fields. We present the structural and morphological properties of ULIRGs in Sections 3 and 4, and summarize our results in Section 5. Throughout this paper, we adopt a standard cosmology with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_\Lambda = 0.7$, and $\Omega_M = 0.3$. All magnitudes use the AB system unless otherwise noted.

2. SAMPLE SELECTION AND DATA

Total infrared luminosity ($L_{\text{IR}} = L_{8-1000 \mu\text{m}}$) is an important measurement in characterizing ULIRGs at $1 < z < 3$. Direct measurement of L_{IR} requires far-infrared photometric data, yet they are not available for most of $24 \mu\text{m}$ se-

¹ <http://3dhst.research.yale.edu/Home.html>

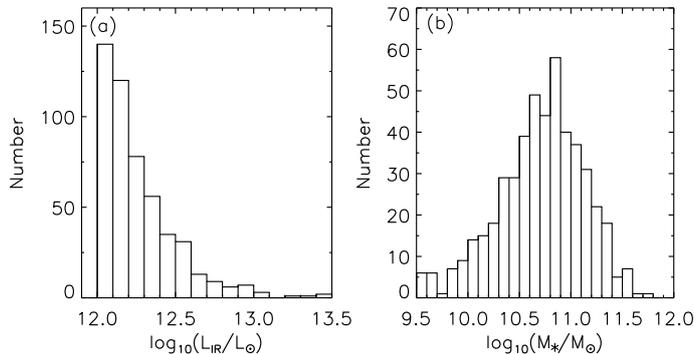


Fig. 1. (a) Distribution of infrared luminosity (L_{IR}) of 502 ULIRGs at redshift $1 < z < 3$ from the three 3D-HST fields (AEGIS, COSMOS, and GOODS-N). (b) Distribution of stellar mass (M_*) of ULIRGs in our sample.

lected sources. This is particularly true for our sample. In our work, we adopt a luminosity-independent conversion from the observed *Spitzer*/MIPS $24\ \mu\text{m}$ flux density to L_{IR} , based on a single template that is the logarithm mean of Wuyts et al. (2008) templates with $1 \leq \alpha \leq 2.5^2$. Wuyts et al. (2011) demonstrated that this luminosity-independent conversion from $24\ \mu\text{m}$ photometry to L_{IR} yields estimates that are in good median agreement with measurement from Herschel/Photoconductor Array Camera and Spectrometer (PACS) photometry. Finally, we construct a sample of 502 ULIRGs with $L_{\text{IR}} > 10^{12} L_{\odot}$ at redshift $1 < z < 3$ from the three 3D-HST fields (AEGIS, COSMOS, and GOODS-N), using the photometric data of *Spitzer*/MIPS $24\ \mu\text{m}$ from Fang et al. (2014), Muzzin et al. (2013), and Kajisawa et al. (2011), respectively.

3D-HST is a NIR spectroscopic survey with the HST, designed to study the physical processes that shape galaxies in the distant universe. The survey contains a great diversity of objects from high-redshift quasars to brown dwarf stars, but is optimally designed for the study of galaxy formation over $1 < z < 3.5$ (Brammer et al. 2012; Skelton et al. 2014). In addition, it also includes NIR (F125W and F160W) high-resolution ($0''.06\ \text{pixel}^{-1}$) imaging data from the WFC3 on the HST (Grogin et al. 2011; Koekemoer et al. 2011). The 5σ point-source detection limit is brighter than 27.0 mag in the F160W (H) and F125W (J) filters. Our study is performed using the latest data (version 4.1) release of the 3D-HST survey. The stellar mass (M_*) and photometric redshift (z , if there is no spectroscopic redshift available) we adopt in our work also come from the 3D-HST photometric catalogs (AEGIS, COSMOS, and GOODS-N). Further details are in Brammer et al. (2012) and Skelton et al. (2014) for the survey and observational design and the data products. Fig. 1 shows the distributions of L_{IR} and M_* of ULIRGs with $1 < z < 3$ in our sample, and all of them have $M_* > 10^{9.5} M_{\odot}$.

3. STRUCTURES OF ULIRGS

Since the redshift distribution of ULIRGs is quite broad ($1 < z < 3$), we analyze their rest-frame optical structures in the WFC3 F125W or F160W bands according to their redshifts. For ULIRGs with $1 < z < 1.8$, we choose the WFC3

² http://www.mpe.mpg.de/~swuyts/Lir_template.html

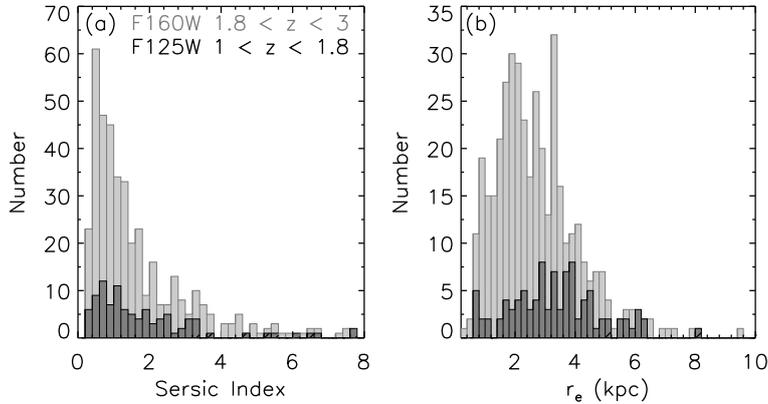


Fig. 2. Sérsic index (n) and effective radius (r_e) histograms of ULIRGs in our sample in different redshift bins. The left panel (a) is the distribution for n , and the right panel (b) is the distribution for r_e .

F125W bandpass for structural analysis, it corresponds approximately to V -band in the rest-frame in this redshift range, but in the redshift range of $1.8 < z < 3$, we analyze galaxy structure in the rest-frame optical band (V) from the F160W image instead. Finally, 98 ULIRGs in our sample have J -band counterparts ($1 < z < 1.8$), and 404 ULIRGs ($1.8 < z < 3$) are detected in the H -band image. The structural parameters of ULIRGs, Sérsic index (n) and effective radius (r_e), from the latest catalog³ (version 1.0) are provided by van der Wel et al. (2012). As described above, we use in our structural analysis the observed J structures at $1 < z < 1.8$ and the H structures at $1.8 < z < 3$.

Fig. 2 shows the n and r_e distributions of ULIRGs in our sample in different redshift bins. From Fig. 2a, the derived Sérsic indexes, ranging from 0.4 to 8, indicate a wide range of structural diversities for these ULIRGs, from spheroid to diffuse structures, e.g., irregulars in appearance, disk-like systems, and elliptical structures. In total, there are 80% of the ULIRGs distributed at $n < 2.5$ and 20% at $n > 2.5$. In addition, we also find that the distribution of sizes of ULIRGs is broad, ranging from 0.5 to 8 kpc, but most (81%) of them are distributed at $r_e < 4$ kpc. In Fig. 3, the sizes of our ULIRG sample are compared to those of $z \sim 0.1$ late-type galaxies (LTGs) from Shen et al. (2003). We find that ULIRGs with $M_* > 10^{10.5} M_\odot$ at $1 < z < 3$ follow a clear $r_e - M_*$ relation. However, most of them have smaller sizes, compared to those of local LTGs with similar stellar mass. Also, there are present compact ULIRGs with $r_e < 1$ kpc, even in massive systems.

In order to explore the size evolution with redshift for ULIRGs at $1 < z < 3$, we plotted in Fig. 4 the sizes of ULIRGs from our sample. The solid square, triangles, and star symbol in this figure represent the ULIRGs from Veilleux et al. (2002), Dasyra et al. (2008), and Kartaltepe et al. (2012), respectively. Based on HST NICMOS H -band imaging of 33 $z \sim 2$ ULIRGs from a $24 \mu\text{m}$ -selected sample of the *Spitzer* survey, Dasyra et al. (2008) found that their effective radii range from 1.4 to 4.9 kpc, with a mean of $\langle r_e \rangle = 2.7$ kpc and a dispersion of $\sigma = 0.8$ kpc. Using high-resolution HST/WFC3 NIR imaging from CANDELS-GOODS-South

³<http://www.mpia-hd.mpg.de/homes/vdwel/candels.html>

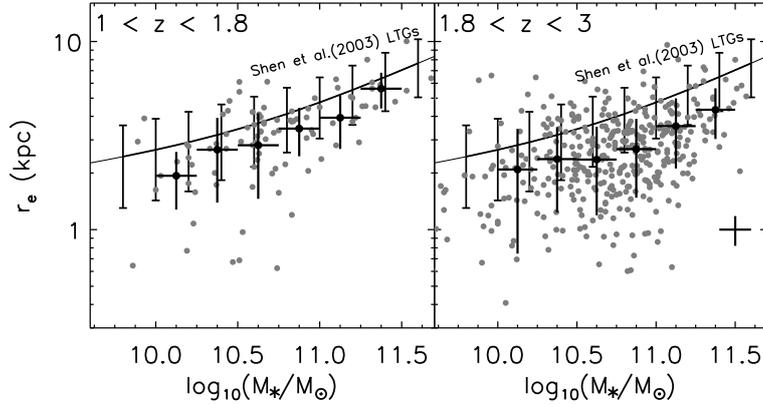


Fig. 3. Relation of stellar mass (M_*) and effective radius (r_e) for ULIRGs in our sample in different redshift bins. The solid lines with 1σ standard errors are provided by Shen et al. (2003) for local late-type galaxies (LTGs). Black solid circles represent the median sizes of ULIRGs in different M_* bins ($\Delta\log_{10}(M_*/M_\odot) = 0.25$). Typical error bars for the data points are shown in the right panel.

field, Kartaltepe et al. (2012) provided the more detailed morphological study of 52 ULIRGs at $z \sim 2$. The median value of sizes of these ULIRGs is 3.3 ± 1.7 kpc. Utilizing the IRAS 1 Jy sample of 118 ULIRGs, Veilleux et al. (2002) found the mean size of local ULIRGs 4.8 ± 1.37 kpc at R band.

In Fig. 4, the red solid circles represent the median sizes of our ULIRG sample in different redshift bins ($\Delta z = 0.5$). The red line, $r_e \propto (1+z)^{-0.96 \pm 0.23}$, corresponds to the best fit to the four median points. The slope ($\alpha = -0.96$) of the size evolution of ULIRGs is steeper than that of gas-rich LTGs ($\alpha = -0.75$ from van der Wel et al. 2014) with similar stellar mass, but it is still much flatter than for the massive early-type galaxies (ETGs) with $\alpha = -1.48$ from van der Wel et al. (2014). If to include the Veilleux et al. (2002) data point of local ULIRGs when fitting a power law to the $r_e - z$ relation, we find that the slope (-0.77 ± 0.11) becomes closer to the LTG value. A possible explanation is that ULIRGs represent a marginally more compact subsample of the LTG population. This interpretation is supported by a large fraction of LTGs in our sample (see Section 4). Moreover, we find that the sizes of ULIRGs at high redshifts are on average one to two times smaller than those of local ULIRGs (from Veilleux et al. 2002) with similar infrared luminosity.

4. MORPHOLOGIES OF ULIRGS

Morphologies of galaxies correlate with a number of physical properties, such as stellar mass, star formation rate and rest-frame color of galaxies, thus they can provide direct information on the formation and evolution history of these objects. Following the method applied in Section 3, we use the observed J morphologies at $1 < z < 1.8$ and the H morphologies at $1.8 < z < 3$ in our following analysis. Fig. 5 (J band) and Fig. 6 (H band) show examples of the NIR images for ULIRGs in the COSMOS field of the 3D-HST survey. We performed the visual inspection by three of us, and found that galaxies in our sample exhibit very diverse morphologies, covering a wide range of types from interacting systems to compact spheroids. As

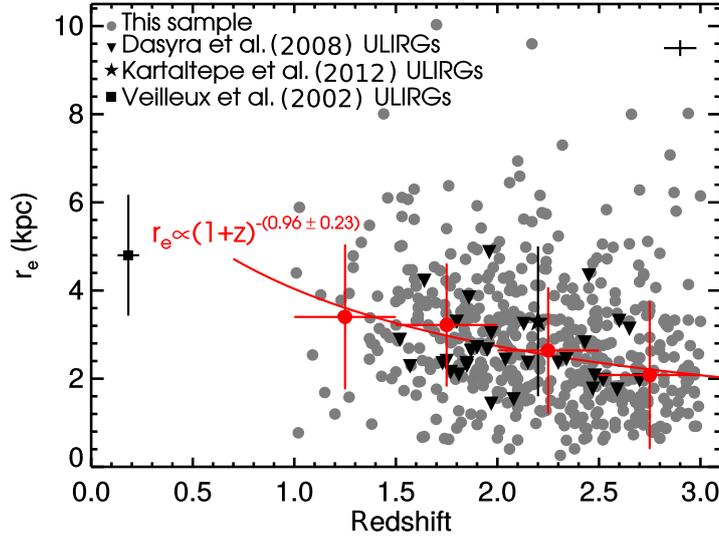


Fig. 4. Evolution of the sizes r_e with redshift in our ULIRGs sample. Red solid circles represent the median sizes of ULIRGs in different redshift bins ($\Delta z = 0.5$). Red line is the best fit to the four median points ($r_e \propto (1+z)^{-0.96 \pm 0.23}$). The sizes of ULIRGs from the literature (Veilleux et al. 2002; Dasyra et al. 2008; Kartaltepe et al. 2012) are also plotted in this figure. Typical error bars for the data points are shown in the upper-right corner.

illustrated in Fig. 7, some of the ULIRGs show morphological features of early-phase mergers, advanced-phase mergers, or merger remnants. Meanwhile, there are many extended disks and irregular morphologies for high-redshift ULIRGs.

In order to quantitatively investigate the morphological features of ULIRGs at $1 < z < 3$, we also measure nonparametric morphological parameters (Abraham et al. 1996; Lotz et al. 2004), such as the Gini coefficient (G ; the relative distribution of a galaxy's pixel flux values) and high moment (M_{20} ; the second-order moment of the brightest 20% of the galaxy's flux). Based on the rest-frame optical morphologies of galaxies, Lotz et al. (2008) defined G - M_{20} criteria to classify ETGs (E/S0/Sa), LTGs (Sb-Ir), and mergers:

ETGs (E/S0/Sa): $G \leq -0.14M_{20} + 0.33$ and $G > 0.14M_{20} + 0.80$,

LTGs (Sb-Ir): $G \leq -0.14M_{20} + 0.33$ and $G \leq 0.14M_{20} + 0.80$,

Mergers: $G > -0.14M_{20} + 0.33$.

Fig. 8 shows the distribution of ULIRGs in our sample on the G vs. M_{20} diagram. For the morphological properties of ULIRGs at $1 < z < 3$, the majority of them shows mergers and irregular and disk-like structures, with relatively high M_{20} (> -1.7) and small Sérsic index ($n < 2.5$, $\langle n \rangle = 1.4 \pm 1.3$), while others are elliptical-like (E/S0/Sa) morphologies with lower M_{20} (< -1.7) and larger n (> 2.5 , $\langle n \rangle = 3.6 \pm 1.2$). Among the ULIRGs with $1 < z < 1.8$ ($1.8 < z < 3$), the fractions of ETGs, LTGs, and mergers correspond to 3% (2%), 55% (73%), and 42% (25%), respectively. This is in agreement with the result of visual morphologies of ULIRGs. The existence of so many massive galaxies with stellar masses

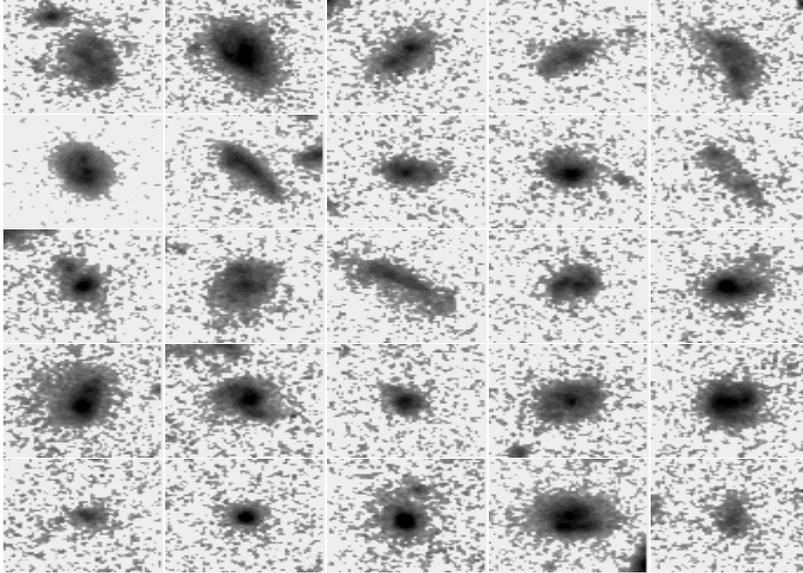


Fig. 5. HST/WFC3 *J*-band images of ULIRGs at $1 < z < 1.8$ from the COSMOS field of the 3D-HST survey. The size of each image is $4'' \times 4''$.

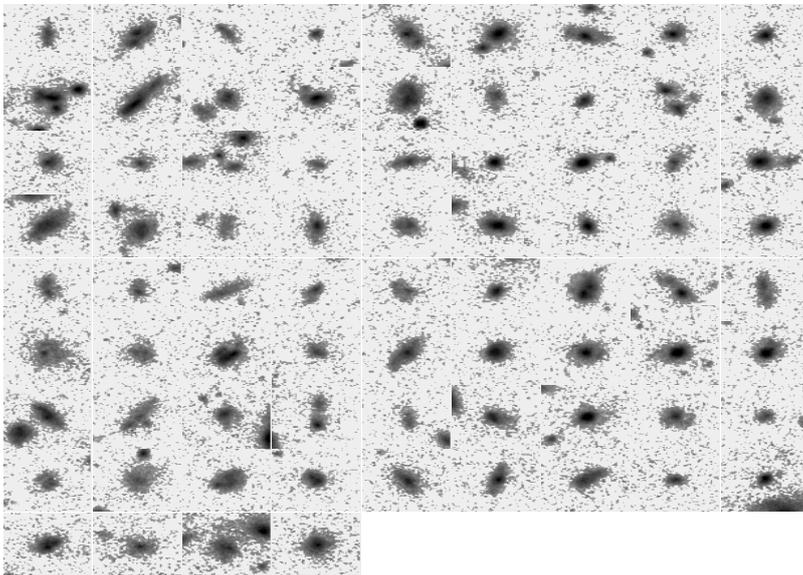


Fig. 6. HST/WFC3 *H*-band images of ULIRGs at $1.8 < z < 3$ from the COSMOS field of the 3D-HST survey. The size of each image is $4'' \times 4''$.

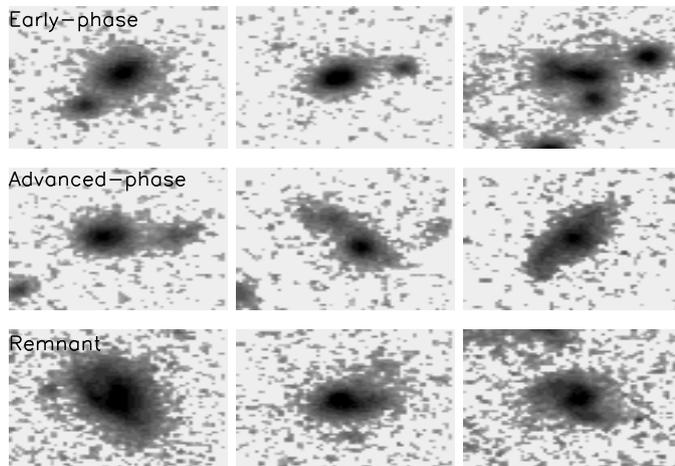


Fig. 7. Examples of different merging types: early-phase mergers, advanced-phase mergers, and merger remnants. The size of each image is $4'' \times 4''$.

$M_* \gtrsim 10^{10}$ at high redshifts challenges the merger scenario for the formation of massive galaxies. The current numerical simulations (Narayanan et al. 2009) have failed to produce as many major mergers as required to explain the observed number of ULIRGs at $1 < z < 3$. An alternative formation scenario for ULIRGs is that a massive, gas-rich galaxy could have the star formation rate (SFR) as high as $180 - 500 M_\odot \text{ yr}^{-1}$ without any merging process. The diversity of morphologies indicates that ULIRGs may occur in different interaction stages of major mergers, in minor mergers, or via secular evolution not involving mergers at all.

For ULIRGs in our sample, the fraction of objects classified as ETGs only is small, and remains roughly constant across the full luminosity/redshift range. The fraction of galaxies classified as LTGs decreases dramatically with luminosity while the fraction of mergers and interactions increases. The fraction of mergers and interactions among the $1.8 < z < 3$ ULIRGs is lower than at $1 < z < 1.8$, while the fraction of LTGs is higher at similar IR luminosity and the same rest-frame wavelength. This suggests that there has been an evolution in the morphology of ULIRGs between these two redshifts.

Star-forming galaxies in the local universe follow a tight correlation between stellar mass and SFR, defining a main sequence (MS; Brinchmann et al. 2004). The MS is also seen at $0.5 < z < 3$ (Noeske et al. 2007; Elbaz et al. 2007; Daddi et al. 2007). Galaxies with SFRs significantly higher ($2 \times$ MS) than this relation predicts are considered to be starbursts. For ULIRGs in our sample, about 65% of the objects have significantly higher SFRs relative to the normal MS. This implies that violent starbursts play an important role in ULIRGs at $z \sim 2$.

5. SUMMARY

In this paper, we constructed a sample of 502 ULIRGs with $L_{\text{IR}} > 10^{12} L_\odot$ at $1 < z < 3$ from the 3D-HST survey (AEGIS, COSMOS, and GOODS-N). Utilizing the HST/WFC3 NIR (F125W and F160W) high-resolution images, we studied the morphological and structural diversities of these galaxies in the rest-frame

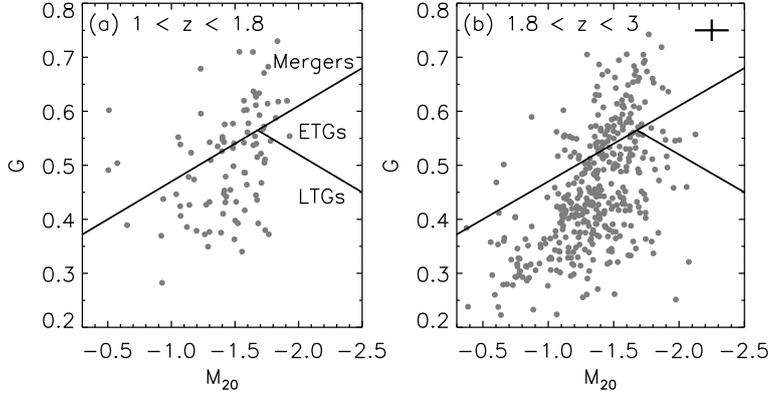


Fig. 8. Distribution of the rest-frame optical ($\sim 5000 \text{ \AA}$) morphologies of ULIRGs in the Gini coefficient vs. M_{20} plane. The solid lines represent the criteria defined by Lotz et al. (2008). Early-type galaxies (ETGs, E/S0/Sa): $G \leq -0.14M_{20} + 0.33$ and $G > 0.14M_{20} + 0.80$; Late-type galaxies (LTGs, Sb–Ir): $G \leq -0.14M_{20} + 0.33$ and $G \leq 0.14M_{20} + 0.80$; Mergers: $G > -0.14M_{20} + 0.33$. Typical error bars for the data points are shown in the right panel.

optical. To clearly depict the morphologies of ULIRGs at $z \sim 2$, we performed nonparametric measures of galaxy morphology. Specifically, we explored the size (r_e) evolution with redshift in our ULIRG sample.

We find the rest-frame optical morphologies of high-redshift ULIRGs are a mixture of mergers or interacting systems, irregular galaxies, disks, and ellipticals. Most of the ULIRGs in our sample can be roughly divided into merging systems and late-type galaxies (LTGs), with relatively high M_{20} (> -1.7) and small Sérsic index ($n < 2.5$), while others are elliptical-like morphologies with lower M_{20} (< -1.7) and larger n (> 2.5). The morphological diversities of ULIRGs suggest that there are different formation processes for these galaxies. Merger processes between galaxies and disk instabilities play an important role in the formation and evolution of ULIRGs at high redshift.

Regarding the structural properties of ULIRGs in our sample, we find that ULIRGs at $1 < z < 3$ follow a clear $r_e - M_*$ relation. However, most of them have smaller sizes, compared to local LTGs with similar stellar mass. Meanwhile, we also find that the evolution of the size with redshift of ULIRGs at $z \sim 1 - 3$ follows the relation $r_e \propto (1+z)^{-(0.96 \pm 0.23)}$. The slope ($\alpha = -0.96$) of the size evolution of ULIRGs is steeper than that of gas-rich LTGs ($\alpha = -0.75$) with similar stellar mass, but it is still much flatter than for the massive early-type galaxies (ETGs) with $\alpha = -1.48$, suggesting that ULIRGs represent a marginally more compact subsample of the LTG population. Moreover, we also find that the sizes of ULIRGs at high redshifts are on average one to two times smaller than those of local ULIRGs with similar infrared luminosity.

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