Review article

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Silicon-based on-chip multiplexing technologies and devices for Peta-bit optical interconnects

Abstract: An effective solution to enhance the capacity of an optical-interconnect link is utilizing advanced multiplexing technologies, like wavelength-division-multiplexing (WDM), polarization-division multiplexing (PDM), spatial-division multiplexing (SDM), bi-directional multiplexing, etc. On-chip (de)multiplexers are necessary as key components for realizing these multiplexing systems and they are desired to have small footprints due to the limited physical space for on-chip optical interconnects. As silicon photonics has provided a very attractive platform to build ultrasmall photonic integrated devices with CMOS-compatible processes, in this paper we focus on the discussion of silicon-based (de)multiplexers, including WDM filters, PDM devices, and SDM devices. The demand of devices to realize a hybrid multiplexing technology (combining WDM, PDM and SDM) as well as a bidirectional multiplexing technologies are also discussed to achieve Peta-bit optical interconnects.

Keywords: wavelength-division-multiplexing (WDM); polarization-division multiplexing (PDM); spatial-division multiplexing (SDM); hybrid multiplexing; bidirectional multiplexing; silicon; Peta-bit; photonic integrated circuit (PIC).

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1 Introduction

Modern micro-processors include tens to hundreds of cores on a single die to improve performance. In order to maximize their performance, a very large bandwidth is needed for the cores to access data stored in local and distant caches as well as in off-chip main memory [1, 2]. For example, the required bandwidth for a Corona architecture consisting of 256 cores with a goal of 10 TFLOP peak performance, is 10 TBps when one byte per FLOP for on-/off-chip communication is used [3]. To meet such a bandwidth challenge for communication among the cores and off-chip memory, optical interconnects are regarded as a very promising solution by combining monolithic CMOS silicon photonics and optimized processor-memory network architectures [1, 2]. If we take into account the core number will continue to increase to more than 1000 in the following years as many industry pundits predict, the capacity of an optical-interconnect link must be improved further [3]. An effective solution is utilizing advanced multiplexing technologies [3], including wavelength-division-multiplexing (WDM), polarization-division multiplexing (PDM), spatial-division multiplexing (SDM), etc, as are used for long-haul optical fiber communications.

For example, DWDM (dense WDM) technology has been used very widely to enable tens of channels with different carrier wavelengths to transmit along a single mode optical fiber for long-haul networks. A natural evolution is to extend this technology to data centers [2]. However, in a DWDM system the emission wavelengths of all the laser sources have to be aligned and stabilized precisely by e.g., controlling the temperature of the chip carefully. As a consequence, the management for wavelength tuning, conversion, routing and switching in DWDM systems becomes complicated, expensive, and power-hungry, which is acceptable for the long-haul optical network. For on-chip optical networks, however, it might be too expensive and power-consuming to afford especially when lots of laser sources and drivers are included on one chip. As a result, regarding to the realization of affordable intra-chip / inter-chip optical interconnects with low-power-consumption, CWDM (coarse WDM) technology is a potentially better option than DWDM technology regarding to the relaxed requirements for the wavelength alignment/control. A 4-channel CWDM link with 400 GHz channel-spacing has been used to realize a 50 Gbps communication link between two chips [4]. The short transmission distance
means the transparent window for optical waveguides or fibers is large, which makes more CWDM channels available if needed. Recent progress of CWDM devices will be reviewed in Section 2.

It is also interesting and necessary to enhance the link capacity with single-wavelength carrier light. In this case, the technologies of polarization-division multiplexing (PDM) and space-division multiplexing (SDM) become very useful. PDM technology has been used to enhance the capacity for long-haul optical fiber communications by utilizing two orthogonal polarizations together with phase modulation or optical quadrature amplitude modulation (QAM), which allows transmission speeds of 100 Gbit/s or more over a single wavelength [5]. Due to the random variation of the polarization state of light in fibers, PDM is generally used together with advanced channel coding techniques so that digital signal processing (DSP) can be used to decode the signal. Note that the polarization state of light can be maintained very well for the case of on-chip optical interconnects since optical signals propagate along highly birefringent planar optical waveguides within the chip. Therefore, it is not necessary to work with advanced channel coding techniques as well as DSP so that the PDM for on-chip optical interconnects can be simplified. In Section 3, we give a review for polarization handling devices used to realize PDM technology.

SDM technology provides a way to improve the capacity by using multi-core [6] or multimode optical waveguides/fibers [7, 8], and has attracted more and more attention for long-haul optical fiber communications in the recent years. When using multi-core SDM technology for photonic networks-on-chip, the advantage is that the links are separated physically and no (de)MUXer is needed. The drawback is the large footprint and the increased layout complexity especially when there are many waveguide cores included. For example, a significant excess loss might be introduced due to the waveguide crossings, which usually exists for large-scale photonic integrated circuits (PICs). And it is not convenient to switch optical signals between any two waveguides due to the limited physical space. An alternative is using multimode SDM technology [9–11], for which each eigen-mode in a multimode optical waveguide carries different data. Multimode SDM has been proposed to enhance the capacity of fiber optical communications [7]. However, it is not easy to achieve mode (de)Muxer to handle higher-order modes in a multimode optical fiber. Recently multimode SDM technology has been developed very well with a few-mode fiber which only supports a few modes. Some complicated free-space optical setups are introduced for mode (de)multiplexing [8], which, however, is very difficult to extend for having more modes included. One should note that the situation becomes much better for photonic networks-on-chip because optical signal propagates along planar optical waveguides within chips, in which case the eigen-modes could be converted conveniently by using some specific PICs [10]. This makes it very attractive to develop multimode SDM technology for on-chip optical networks. Recent progresses on devices for mode (de)multiplexing technology are reviewed in Section 4.

In order to improve the total capacity to be up to Peta-bit/s, a potential way is combining all these multiplexing technologies to form a kind of multi-dimensional hybrid multiplexing technology, which will be discussed in Section 5. Bidirectional multiplexing technology can be usually applied to establish the optical interconnects between two chips, for which non-reciprocal devices are needed. This will be discussed in Section 5.2.

Regarding that silicon photonics has provided a very attractive platform to build ultrasmall integrated photonic devices with standard CMOS (complementary metal oxide semiconductor) processes, this paper will review recent progresses of the key photonic integrated devices on silicon for realizing the multiplexing technologies used in photonic networks-on-chip.

## 2 Silicon-based WDM filters

Utilizing the interference of optical beams provides a fundamental principle to realize wavelength-selective response desired for WDM filters. It is well known that a Mach-Zehnder interferometer (MZI) is a basic device with two-beam interference and a single-stage MZI has a sine-like spectral response. An improved spectral response can be synthesized with multiple cascaded MZIs by optimizing and controlling the coupling coefficients as well as the critical phase delays of the stages [12]. For example, a cascaded MZI filter with flattened spectral responses can be achieved, which is useful for two-channel optical interleavers [13–16]; however, it is still not easy to achieve multi-channel WDM (de)multiplexers by using MZIs. Alternatively, multi-beam interference is preferred because it enables narrow-passband wavelength filtering over a large wavelength period (i.e., the free spectral range, FSR). The typical multi-beam interferometers include arrayed-waveguide gratings (AWGs) [17–29] and echelle diffraction gratings (EDG) [30–34], which can (de)multiplex tens of WDM channels simultaneously and have been used in practical DWDM systems worldwide. In Section 2.1, we give a review for recent progresses on these two types of planar
waveguide (de)multiplexers (i.e., AWGs as well as EDGs) with ultrasmall footprints based on silicon-on-insulator (SOI) nanowires.

Another form of multi-beam interferometer is based on optical cavities (e.g., F-P cavities, microring resonators (MRRs), etc) [35–38], which have periodical Lorentzian spectral responses to select a series of resonance wavelengths. For WDM applications, in order to select one or several channels from all channels multiplexed, one can choose one or more optical cavities and each cavity should be designed to have a FSR large enough to cover all the multiplexed channels. When using an F-P cavity (which is a standing-wave resonator with two ports), one channel is dropped from the output ports while the other channels are reflected back to the input port. Consequently it is not suitable to use F-P cavities for multi-channel demultiplexing. In contrast, an MRR is a travelling-wave resonator with two or four ports and there is no reflection ideally. It is convenient to cascade many MRRs and even realize an array with \( N \times N \) elements to deal with \( N \) channels [39]. We will discuss MRR filters in Section 2.2.

### 2.1 Planar waveguide (de)multiplexer (AWGs & EDGs)

#### 2.1.1 AWGs

An AWG consists of input waveguides, arrayed waveguides, output waveguides as well as one or two free propagation regions (FPRs) [17]. The adjacent arrayed waveguides have a constant length difference \( \Delta L \), which is an important parameter to influence the dispersion ability of an AWG [18]

\[
\Delta L = (\lambda_0, n_g, d_g, D) / (\lambda_0, n_g, D, \Delta m, R),
\]

where \( \lambda_0 \) is the operation wavelength, \( \Delta \lambda_{ch} \) is the channel spacing, \( n_g \) is the effective index of the FPR slab waveguide, \( n_g \) and \( N_g \) are respectively the effective index and the group index of the arrayed waveguide, \( d_g \) is the end separation of the arrayed waveguides, \( D \) is the separation of the output waveguides, \( R \) is the FPR length, and \( m \) is the interference order.

AWG (de)multiplexers have been commercialized with low-index-contrast optical waveguides, e.g., SiO\(_2\)-on-Si buried waveguides [40, 41]. However, the AWG chip usually has a size of several cm\(^2\). Instead very small AWG (de)multiplexers can be realized when using SOI nanowires with ultra-high \( \Delta \) and ultrasmall cross section [19–26]. However, the performance (especially the crosstalk) of SOI-nanowire AWGs is very sensitive to the size variation of the arrayed waveguides (e.g., the non-uniformity of the Si-core dimension) [23]. With the current fabrication technologies, the roughness for the core sidewall of SOI nanowires is about 2 nm [16] and the fluctuation due to this core-width variation can be reduced by enlarging the core width in the straight regions [23]. Note that the top silicon thickness uniformity of 6-inch SOI wafers is about \( \pm 2 \) nm and the uniformity is improved to about \( \pm 1 \) nm in a area as small as 1 mm\(^2\) [42, 43]. Therefore, it is helpful to minimize the phase error if the AWG/EDG occupies a small area.

It is well known that ultrasmall bending radius (\( R \approx 2 \) \( \mu \text{m} \)) and decoupling separation (\( \approx 2 \) \( \mu \text{m} \)) are allowed for SOI nanowires [44], which is very helpful to reduce the AWG size. However, when using a standard AWG layout design, the separation between two adjacent arrayed waveguides may be much larger than the decoupling separation (\( \approx 2 \) \( \mu \text{m} \) [44]) of SOI-nanowire waveguides to achieve the length difference \( \Delta L \) between adjacent arrayed waveguides as required. Therefore, the layer design of an SOI-nanowire AWG should be improved to minimize the footprint. We proposed several kinds of novel layouts with overlapped FPRs [45], microbends as well as spirals in the arrayed waveguides [46, 47]. A reflective AWG demultiplexer with photonic crystal (PhC) reflectors was also demonstrated in order to reduce the AWG size further and make the layout design of AWGs very flexible.

### A. Ultrasmall AWG (de)multiplexer with overlapped FPRs

Figure 1A shows the picture of a fabricated AWG (de) multiplexers with two overlapped FPRs [22]. Each half of an arrayed waveguide includes three straight waveguides which are connected smoothly by two bending waveguides in sequences. With such a layout, the structure becomes more compact than a conventional one. We have designed and fabricated a 5\( \times \)5 SOI-nanowire AWG (de)multiplexer with ultrasmall footprint of only \( \approx 40 \) \( \mu \text{m} \times \approx 50 \) \( \mu \text{m} \), as shown in Figure 1A. In this design, the total number of arrayed waveguides \( N_{w}\approx12 \), the channel spacing \( \Delta \lambda_{ch}=11 \) nm. Figure 1B shows the measured spectral responses of all the five channels for TE polarization. It can be seen that the device has a relatively low crosstalk (\( \approx -17 \) dB) and uniform responses.

### B. AWG (de)multiplexer with micro-bends

Figure 2A and B shows the fabricated AWG with a novel layout including overlapped FPRs and arrayed waveguides with a series of microbends. These microbends enable a large lightpath difference in a small
occupied area (with a small separation between waveguides), and consequently the total size is minimized. The demonstrated 400 GHz 15×15 AWG router has 34 arrayed waveguides and the total size is only 163 µm×147 µm. Figure 2C shows the measured spectral responses of 15 channels when the TE polarization light is input from the central input waveguide. The channel spacing is around 3.1 nm, which is close to the design value 3.2 nm. The crosstalk between adjacent channels is ~–10 dB, which is partially due to the phase errors in the arrayed waveguides with microbends. The temperature dependence for the AWG router was also characterized. Figure 3A shows the measured spectral response of the central output channel as the temperature varies from 23°C to 110°C. It can be seen that the channel wavelength can be thermally tuned effectively and the temperature dependence of the central wavelength is about 0.068 nm/°C.

C. Reflective-type AWG (de)multiplexer

Another effective method to reduce the size of an AWG is using a reflective-type structure [48–50]. However, the layout design freedom for those conventional reflective-type AWG based on micrometric optical waveguides is limited. First, the sections at the end of arrayed waveguides are arranged in parallel and they are perpendicular to the same reflection mirror [48–50]. Second, one usually has to cleave or dice the arrayed waveguides carefully and the cleaved facet should be polished further to be smooth and flat [48]. Dielectric or metal films (e.g., Cr-Au film) are usually needed to enhance the reflection efficiency [48–50], which makes the fabrication relatively complex. Furthermore, one should note that it is still difficult to achieve a high-quality reflector at the micrometric waveguide facet and consequently the performance of reflective AWGs is usually degraded [50, 51].

For SOI-nanowire AWGs, it becomes even more difficult to introduce conventional metal mirrors because of the small physical space. Alternatively, a pure-dielectric reflector based on photonic crystal (PhC) structures is a suitable option for realizing a reflective SOI-nanowire AWG as demonstrated in Figure 3A [27]. The PhC reflectors can be replaced by Bragg grating (i.e., a one-dimensional PhC structure) [30], or Teardrop reflector [52]. In this way, the fabrication of such an ultrasmall reflective AWG is compatible to the standard CMOS process and no additional fabrication process is needed in comparison with regular SOI-nanowire AWGs. Figure 3B shows the measured spectral responses for the eight channels of a 400 GHz-spacing reflective SOI-nanowire AWG with a footprint of 134 µm×115 µm. It can be seen that the excess loss of the fabricated reflective AWG (de)multiplexer is about 3~4 dB and the crosstalk is about -12 dB. As a comparison, we have also fabricated a 16-channel 200 GHz ultra-compact reflective SOI-nanowire AWG on the same chip, as shown in Figure 4A. The footprint is about 193 µm×168 µm, which is about twice larger than that of the 8-channel 400 GHz-spacing AWG. The measured spectral response is shown in Figure 4B. It can be seen that the channel crosstalk is high, which is mainly from the phase errors in the arrayed waveguides. This comparison indicates that a small footprint is indeed important for the device to achieve good performances.

As shown in Figures 3A and 4A, each arrayed waveguide of the reflective AWG has its own PhC reflector, which makes the layout design very flexible even when a very low or very high diffraction order is needed. It is also possible to use arrayed waveguides without any bends, which can minimize the length of the shortest arrayed waveguide. This is helpful to reduce the crosstalk resulting from the phase error in the waveguide array according to the theoretical analysis in Ref. [53].

Figure 1 (A) Picture of the fabricated AWG (de)multiplexers with two overlapped FPRs; (B) the measured spectral responses for all five channels.
2.1.2 Echelle diffraction grating (de)multiplexer

An EDG is another typical planar waveguide (de)multiplexer, which is very similar to a reflective-type AWG. An EDG has no arrayed waveguides but consists of a reflective grating [30], as shown in Figure 5. It is known that multimodal propagation in the FPR deteriorates insertion loss and channel crosstalk because multiple images are formed along the Rowland circle due to the mode dispersion [54]. Fortunately, the 220 nm-thick FPR only supports one guided-mode so that there is no performance deterioration caused by higher-order modes for an SOI-nanowire EDG [30].

A general issue for an EDG is that deeply etched grating facets with high verticality are usually required critically to minimize the excess loss [55]. Fortunately, when using a submicron (e.g., 0.22 μm)-thick SOI platform discussed here, the etching depth is small and the requirement for the sidewall verticality is relaxed. The reflection efficiency of the grating facets can be improved significantly by utilizing local Bragg mirrors at the facets [31]. For an EDG, the crosstalk is mainly from the facet position fluctuation in the reflection mirrors and the silicon thickness variation. The reported EDG usually has a crosstalk level around -20~-35 dB [30–33] and SOI-nanowire EDG (de)multiplexers have been used to realize a multi-channel communication link between two chips [4].

For an EDG the phase delay is obtained by a difference in path length between the grating teeth for a propagating beam in the FPR, which also work as the beam focusing region. This makes it potentially smaller than an AWG for the case with large channel spacing. On the other hand, an AWG can scale down to smaller channel spacing with less penalty than an EDG [26]. And the input/output waveguides of an EDG are sitting at the same side of the FPR, which makes an EDG not as flexible as an AWG. For example, an AWG can work in both directions for some applications [56] while an EDG cannot do so.

Table 1 shows the typical parameters for SOI-nanowire AWGs and EDGs reported in the past years. The devices used for photonic networks-on-chip are required to be ultrasmall due to the limited physical space and low loss is also desired according to the power budget of an optical interconnect link, which is different from conventional long-haul networks. Fortunately, low-loss SOI-nanowire AWGs and EDGs with ultrasmall footprints have been realized with optimized fabrication processes as well as improved designs in the past 10 years, as shown in Table 1. For example, the on-chip loss of an AWG/EDG can be lowered to around 2 dB by introducing some specific designs, e.g., bi-level taper structures for AWGs [26], Bragg-grating reflectors for EDGs [31]. Such loss reduction is helpful for realizing low power-consuming photonic networks-on-chip. The crosstalk of SOI-nanowire AWGs and EDGs has also been improved significantly as shown in Table 1. For an AWG, the crosstalk can be effectively reduced to about -20~-25 dB by minimizing the fluctuation due to the core-width variation through the way of enlarging core width in the straight regions [23–26]. In comparison with AWGs, EDGs are more fabrication tolerant since light is propagating in a slab where the thickness is usually controlled well in a small area and
consequently an SOI-nanowire EDG usually has lower crosstalk than an SOI-nanowire AWG (see Table 1). In Ref. [57], it has been demonstrated that error-free WDM transmission with four channels was achieved even when the crosstalk for the WDM filters is up to -17 dB. It is expected to realize error-free transmission with more WDM channels by using the improved SOI-nanowire AWGs and EDGs shown in Table 1.

2.2 Microring resonator (MRR) filters

An MRR usually has one or two couplers to be an all-passed filter or add-drop filter, as shown in Figure 6A-B, respectively. For a MRR, the important parameters include the resonance wavelength $\lambda_{\text{res}}$, the FSR, the 3 dB bandwidth $\Delta\lambda_{3\text{dB}}$, and the extinction ratio (ER) [35]. The bandwidth $\Delta\lambda_{3\text{dB}}$ and the ER are determined by the cavity loss and the coupling ratios of the couplers. When a small bandwidth $\Delta\lambda_{3\text{dB}}$ (i.e., a high Q factor) is desired, one need not only improve the fabrication processes to achieve a smooth waveguide with reduced scattering loss but also make the bending radius large enough to guarantee a small bending loss [58]. In order to have a high ER, the coupling ratio should be chosen appropriately according to the critical coupling condition [35]. As described in the introduction, a large wavelength window might be required for CWDM on-chip optical interconnects, and thus it will be interesting to have MRR filters with an ultra-large FSR and a large tunability range of wavelength, which is reviewed below.

2.2.1 Microring resonator (MRR) optical filters with an ultra-large FSR

The resonance wavelength of an MRR is given by the following equation: $\lambda_{\text{res}} = n_{\text{eff}} L_{\text{cav}} / m$, where $n_{\text{eff}}$ is the effective index.
Table 1  Reported AWGs & EDGs on SOI nanowires.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Year</th>
<th>Crosstalk (dB)</th>
<th>On-chip loss (dB)</th>
<th>Channel number×channel spacing</th>
<th>Waveguide size (nm²)</th>
<th>Footprint (μmxμm)</th>
<th>Area (mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AWG[19]</td>
<td>2004</td>
<td>~7</td>
<td>~8</td>
<td>8×3.2 nm</td>
<td>450×220</td>
<td>380×290</td>
<td>0.110</td>
</tr>
<tr>
<td>AWG[20]</td>
<td>2004</td>
<td>~5</td>
<td>~10</td>
<td>17×6 nm</td>
<td>350×300</td>
<td>110×93</td>
<td>0.010</td>
</tr>
<tr>
<td>AWG[21]</td>
<td>2005</td>
<td>~10</td>
<td>~1</td>
<td>9×11 nm</td>
<td>350×300</td>
<td>60×70</td>
<td>0.004</td>
</tr>
<tr>
<td>AWG[23]</td>
<td>2005</td>
<td><del>17</del>20</td>
<td>2.2~5.2</td>
<td>16×1.6 nm</td>
<td>450×220</td>
<td>500×200</td>
<td>0.100</td>
</tr>
<tr>
<td>AWG[22]</td>
<td>2006</td>
<td>~10</td>
<td>~10</td>
<td>5×11 nm</td>
<td>500×250</td>
<td>40×50</td>
<td>0.002</td>
</tr>
<tr>
<td>AWG[24]</td>
<td>2006</td>
<td>~12</td>
<td>~2.5</td>
<td>16×1.6 nm</td>
<td>450×220</td>
<td>425×155</td>
<td>0.066</td>
</tr>
<tr>
<td>AWG[25]</td>
<td>2010</td>
<td>~21</td>
<td>1.2~3.3</td>
<td>10×20 nm</td>
<td>500×220</td>
<td>370×500</td>
<td>0.185</td>
</tr>
<tr>
<td>AWG[26]</td>
<td>2010</td>
<td>~21</td>
<td>1.1~2.4</td>
<td>8×3.2 nm</td>
<td>450×220</td>
<td>200×350</td>
<td>0.070</td>
</tr>
<tr>
<td>AWG[27]</td>
<td>2011</td>
<td>~12</td>
<td><del>3</del>5</td>
<td>8×3.2 nm</td>
<td>500×220</td>
<td>200×150</td>
<td>0.042</td>
</tr>
<tr>
<td>AWG[29]</td>
<td>2007</td>
<td>~30</td>
<td>~1.9</td>
<td>10×20 nm</td>
<td>500×220</td>
<td>200×150</td>
<td>0.042</td>
</tr>
<tr>
<td>EDG[30]</td>
<td>2009</td>
<td><del>16</del>19</td>
<td>~3</td>
<td>8×3.2 nm</td>
<td>500×220</td>
<td>200×200</td>
<td>0.050</td>
</tr>
<tr>
<td>EDG[31]</td>
<td>2009</td>
<td>~10</td>
<td>~10</td>
<td>21×1.0 nm</td>
<td>450×250</td>
<td>2000×1500</td>
<td>3.000</td>
</tr>
<tr>
<td>EDG[26]</td>
<td>2010</td>
<td>~15</td>
<td>3~7</td>
<td>30×3.2 nm</td>
<td>450×220</td>
<td>500×220</td>
<td>0.500</td>
</tr>
</tbody>
</table>

of the eigenmode of the cavity waveguide, $L_{cav}$ is the cavity length, $m$ is the interference order. Accordingly one can achieve the equation for the FSR as follows: $\text{FSR} = \frac{\lambda}{m'}$, where $m' = m \left( \frac{n_2}{n_{air}} \right)$, the group index $n_g = n_2 - \frac{2}{m'} \left( \frac{\partial n_{eff}}{\partial \lambda} \right)$. It can be seen that the FSR is inversely proportional to the cavity length (i.e., the bending radius) [59, 60]. Since the total bandwidth of a microring-based WDM system [61] is limited by the FSR of the MRR, a smaller MRR is desired to have a larger FSR so that more wavelength channels can be fitted to have higher aggregated data bandwidth [59]. For example, the ultra-large FSR is required to be more than 75 nm when a 48-channel WDM link with a channel spacing of 200 GHz. For the case of using SOI nanowires, the bending radius can be as small as several microns [59, 60] so that the FSR is as large as several tens of nanometers, which indicates an ultra-large quasi-FSR. It is well known that a high ER is achieved for the resonance wavelengths when the following critical coupling condition is satisfied [62]

$$k_{c1}^{(0)} = k_{c2}^{(0)}, \quad (7)$$

where the coupling ratios are defined as shown in Figure 6A. On the other words, when this critical coupling condition is broken, the resonance peak is depressed and the ER could be low. An MZI-coupled race-track resonator was proposed to modify the ER of one resonance wavelength by thermally tuning the coupling ratio of the MZI coupler [37, 63], which also enables to tune the 3 dB bandwidth [64]. By utilizing the wavelength-dependence of the MZI’s coupling ratio, one can depress the resonance peaks except that one to be used so that there is only one major resonance peak over a broad band so that an ultra-large quasi-FSR is achieved as demonstrated in [65, 66].
As an example, Figure 8A shows the structure of a fabricated MZI-coupled MRR and the measured spectral response is shown in Figure 8B [66]. From this Figure, it can be seen that there is a major resonant wavelength $\lambda_{MRR0}$ at around 1540 nm with a high ER (>25 dB) in the wavelength range from 1520 nm to 1630 nm (which is limited by the tunable range of the laser source used in the measurement). And the other resonant wavelengths in this range (1520–1630 nm) are depressed distinctly. It indicates that the MZI-coupled MRR has an ultra-large quasi-FSR (>120 nm). This can be also extended to the design of an MRR-based add-drop filter by combining a directional coupler (DC) and a MZI coupler.

As an alternative, MRR can also play the role as a wavelength-dependent coupler and thus one can build an add-drop filter with a MRR-based 2×2 coupler (coupler #0), as shown in Figure 9. These two rings have different bending radii ($R_1$ and $R_2$) so that their FSRs are different slightly and there is a common resonance wavelength around the desired wavelength (e.g., 1550 nm). Due to the Vernier effect, the period of the common resonance wavelengths will become very large. Here the MRR-based coupler (coupler #0) is design to have a high cross-coupling ratio $k^{(0)}_{12}$ at its resonance wavelengths (see Figure 10A) while another coupler (coupler #1) is a regular DC whose cross-coupling ratio $k^{(1)}_{12}$ is not strongly wavelength-dependent. In this way, the critical coupling to have a high ER occurs around the common resonance wavelengths. Otherwise, the critical coupling condition is broken and the resonance is depressed significantly, which gives an ultra-large quasi-FSR, as indicated by the calculated responses shown in Figure 10B and C. In this example, an SOI nanowire is used and the parameters are: $R_1$=5.56 $\mu$m ($FSR_1$=16 nm), $R_2$=6.10 $\mu$m ($FSR_2$=14.5 nm), the coupling ratio $k^{(0)}_{12}$=0.4, the coupling ratio between the input waveguide and ring #1 is about 0.4, the coupling ratio between the two rings is 0.08. From Figure 10B and C, it can be seen that an ultra-large FSR (>150 nm) is achieved.

2.2.2 MRR optical filters with large tunable range of wavelength

For an MRR, the resonance wavelength is usually tuned by introducing a refractive index change for the ring waveguide electrically or thermally [67–69], and the wavelength detuning $\Delta \lambda$ is given by $\Delta \lambda=(\Delta n_{eff}/n)\lambda$. However, it is difficult to have a large wavelength detuning since the index change due to electrooptical (EO) or thermo-optical (TO) effect is usually small. For example, when there is 100°C temperature increase for a SOI-nanowire-based MRR, the wavelength detuning is about $\Delta \lambda$=8 nm only according to the TO coefficient ($C_{TO}$=1.8×10⁻⁴/°C) of silicon. This tuning range of wavelength can be improved if a large change for the effective index is achievable. For example, a nano-slot waveguide proposed in [70] provides a potential way since its effective index $n_{eff}$ changes very
significantly as the nano-slot thickness changes due to the strong field enhancement in the nano-slot region. A suspended horizontal nano-slot waveguide (as shown by the inset in Figure 11) can be used so that the thickness of the nano-slot can be modified mechanically. Figure 11 shows the calculated effective index \( n_{\text{eff}} \) for such a suspended horizontal nano-slot waveguide as the nano-slot thickness \( h_{\text{slot}} \) varies from 5 nm to 60 nm. It can be seen that the change of the effective index \( n_{\text{eff}} \) is as large as 0.5 when the slot width changes from 5 nm to 30 nm mechanically. The corresponding wavelength tuning range is ultra-large (up to 200 nm) to cover a broad band. The mechanical tuning of a nano-slot can be realized by using e.g., optical forces [71], or electrostatic comb-drive actuators [72].

When using regular SOI nanowires, a potential approach to achieve a large tuning wavelength-range is utilizing the so-called Vernier effect with a cascaded-ring system, which includes two cascaded rings (i.e., ring #1 and ring #2), as shown in Figure 12A and B [73–75]. These two rings have different FSRs (e.g., \( \Delta \lambda_{\text{FSR1}} = 5.94 \) nm and \( \Delta \lambda_{\text{FSR2}} = 5.70 \) nm) by choosing different radii (e.g., \( R_1 = 19.82 \) \( \mu \)m and \( R_2 = 20.62 \) \( \mu \)m). Figure 13A shows the calculated spectral responses of the drop ports for ring #1 and #2. When the \( i \)-th resonance wavelength \( \lambda_{\text{i}(1)} \) of ring #1 is coincided with the \( j \)-th resonance wavelength \( \lambda_{\text{j}(2)} \) of ring #2, there is a major peak (with an ER of >20 dB) locating at the common resonance wavelength \( \lambda_{\text{c}(i)} \) as shown in Figure 13B. When ring #2 is tuned with a small resonance-wavelength shift \( \Delta \lambda_2 = (\Delta \lambda_{\text{FSR1}} - \Delta \lambda_{\text{FSR2}}) \) by introducing an appropriate index change \( \Delta n_{\text{eff}} \), the common resonance wavelength \( \lambda_{\text{c}(i)} \) corresponding to the major peak has a shift as large as \( \Delta \lambda_{\text{FSR1}} \) (see the dashed curve in Figure 13B). It can be seen that the wavelength tuning efficiency \( E = \Delta \lambda / \Delta n_{\text{eff}} \) is multiplied by \( M \) times in comparison with a single-ring system \( (E_2 = \Delta \lambda_2 / \Delta n_{\text{eff}}) \), where \( M = \Delta \lambda_{\text{FSR1}} / (\Delta \lambda_{\text{FSR1}} - \Delta \lambda_{\text{FSR2}}) \). In this way, it is possible to achieve ultra-large tuning range with a small effective index change [74].

### 2.3 General issues for WDM filters based on SOI nanowires

#### 2.3.1 The thermal issue

As presented in Section 2.1.2, the large TO coefficient (TOC) of silicon (\( \text{dn/dT} = 1.8 \times 10^{-4}/\degree\text{C} \)) makes these SOI-nanowire devices strongly temperature-dependent, which is good to realize efficient thermally-tunable WDM filters. On the other hand, however, a temperature controller has to be...
employed to stabilize the chip temperature usually. In order to achieve athermal WDM filters (including AWGs and MRRs), a straightforward approach is introducing another material (like polymer) with negative TOC to compensate the positive TO effect of silicon, which is similar to those used in conventional optical waveguides [76–80]. One can fill the polymer material into the grooves in the silicon waveguide core region [81–83], which however requires very precise control for the waveguide fabrication. An alternative is using polymer as the upper-cladding of the waveguide [84–86]. In Ref. [84] a 1×8 SOI-nanowire AWG with a channel spacing of 400 GHz was realized experimentally. The wavelength temperature dependence of the AWGs is reduced to -1.5 pm/°C, which is much less than that of normal SOI AWGs. Another way to make temperature-insensitive WDM filters (e.g., AWGs, MZIs) is making arm waveguides consisting of two different sections (e.g., narrow and wide SOI nanowires), whose path-length differences are adjusted optimally [87–89]. In this way, one does not need to introduce any additional material (e.g., polymer) so that the fabrication is CMOS-compatible. The problem is that the diffraction order of the AWG is usually low, which limits its application in some degree.

### 2.3.2 The polarization-sensitive issue

Due to the ultra-high index contrast and the submicron cross section, SOI nanowires usually have giant birefringence on the order of 10⁻⁴, which makes SOI-nanowire PICs significantly polarization-sensitive [22]. For fiber-related applications, polarization-insensitive PICs are usually needed. Theoretically speaking, it is possible to make SOI nanowires non-birefringent by optimizing the waveguide dimensions, like those demonstrated for large SOI ridge waveguides [90–94]. However, it is very hard to achieve non-birefringent SOI nanowires experimentally because of the stringent fabrication tolerance. More importantly, the polarization dependent properties of SOI-nanowire devices are different from those devices based on micrometer optical waveguides. For example, for an SOI-nanowire AWG, not only the channel wavelength but also the channel spacing are polarization sensitive, which makes conventional polarization compensation approaches ineffective [95]. Some special approaches are proposed to minimize the polarization-sensitivity of SOI-nanowire photonic integrated devices including multimode interference (MMI) couplers, MRRs, and AWG (de)multiplexers [95–100]. A general solution to eliminate the polarization-sensitivity of silicon photonic integrated devices is using the so-called polarization-diversity technology [101–103]. In Ref. [103], a very smart design for a polarization diversity system was demonstrated to realize polarization-insensitive AWG by using a two-dimensional grating coupler, which simultaneously serves as a fiber-chip coupler, a polarization splitter as well as a rotator. However, it does not work for the case when the AWG needs to be integrated with other components in the same chip. In-plane polarization diversity devices will be needed for large-scale PICs. For example, in Ref. [56], an on-chip polarization diversity circuit is used to realize a polarization-diversified receiver chip by working together with a single Si₃N₄ AWG which has two signals
running along opposite directions to ensure that the receiver is free of polarization-dependent wavelength shift. Polarization diversity technologies are not only essential for solving the polarization issues of SOI-nanowire PICs, but also the key for realizing the PDM technology. For such polarization diversity circuits, the polarizing beam splitter (PBS) and polarization rotator (PR) are the most important elements [101–103], which will be reviewed in the following section.

3 Polarization multiplexing and the devices (PBS, PR)

Polarization-multiplexing is attractive for photonic networks on-chip as a low-cost and simple way to improve the capacity, especially because planar optical waveguides have excellent polarization-maintaining ability and avoid the randomness of the polarization state of light. Figure 14 shows the schematic configuration of a PIC with the PDM technology. Here the PBS (or PBC) works as the (de)MUXer while the PR is utilized to generate two orthogonal polarization modes with the same light source to low the cost. High ER is desired for the PBS as well as the PR so that the channel crosstalk is low. Furthermore, it is also desired to achieve broadband PBSs and PRs, which make it possible to work together with the WDM technology to form a kind of hybrid multiplexing system. As classical elements, these polarization diversity components (including PBSs and PRs) are also very useful for many other applications, e.g., polarization transparent silicon nano-PICs [103], coherent optical communications [104], and integrated photonic quantum circuits [105]. Here we give a review for the recent work on ultrasmall broadband polarization diversity components on silicon.

3.1 Ultrasmall PBSs

It has been realized that most photonic integrated devices are polarization dependent due to the birefringence of optical waveguides (as summarized in Table 2), which provides various ways to realize waveguide-type PBSs, including multimode interferometers (MMIs) [106–110], DCs [111–118], MZIs [119–121], photonic crystal (PhC) structures [122–126], AWGs [127], MRRs [128], etc. Among them, a DC structure is an attractive option for PBSs because of its structural simplicity. Usually a symmetrical DC consisting of two identical coupling waveguides is used and the PBS length is chosen to be equal as $p$ times of the coupling length $L_{\pi,1}$ of one polarization and $(p+m)$ times of the coupling length $L_{\pi,2}$ of the other polarization, in which way the PBS is long and narrowband intrinsically [112]. In contrast, asymmetrical coupling systems have been considered as an improved option to achieve ultra-short and ultra-broadband PBSs [102], for which the waveguides are optimized to satisfy the phase-matching condition for only one polarization so that complete cross-coupling occurs. On the other hand, the other polarization is likely to have significant phase mismatch due to the strong waveguide birefringence and consequently there is almost no cross-coupling, as shown in Figure 15A in principle. It can be seen that such a PBS is as short as the beat length for the cross-coupled polarization. According to the reciprocity of light, such a DC-based PBS can also be easily extended to be an add-drop device for the PDM system by introducing an add port, as shown in Figure 15B.

An asymmetrical coupling system can be constructed by including two or three non-identical waveguides with different propagation constants in the coupling region. An easy way to make two non-identical waveguides is simply choosing different widths ($w_{col1}$, $w_{col2}$) or heights ($h_{col1}$, $h_{col2}$) of the core, as shown in Figure 16. Regarding the fabrication processes of PICs, the option of modifying the core width only is preferred to avoid any additional etching process. However, for two straight optical waveguides with different core widths ($w_{col1} \neq w_{col2}$, $h_{col1} = h_{col2}$), their fundamental modes for any polarization have different effective indices and consequently the phase matching condition is not satisfied. Therefore, one cannot have efficient cross-coupling between their fundamental modes for any polarization.

![Figure 14](image-url) The schematic configuration of a PIC with the PDM technology.
Alternatively one can couple the fundamental mode in a narrow optical waveguide to the higher-order mode in a wide optical waveguide by optimally choosing their widths according to the phase matching condition (i.e., $n_{\text{eff,0}} = n_{\text{eff,1}}$). Another narrow optical waveguide can be placed at the other side of the wide waveguide as the output port, in which way the higher-order mode in the wide waveguide can be coupled to the fundamental mode of the output waveguide. Such a three-waveguide asymmetrical coupling system is achieved for realizing a PBS as shown in Figure 17A [129]. For example, when 220 nm-thick SOI nanowires are used, the optimal waveguide widths are $w_1 = 410$ nm and $w_2 = 1.195 \mu m$ according to the phase matching condition for TM polarization, i.e., $n_{\text{eff,0,TM}} = n_{\text{eff,1,TM}}$. Figure 17B and C shows the simulated light propagation in the designed PBS when the TE$_0$ and TM$_0$ modes are launched at the input port, respectively.

It can be seen that the TM$_1$ mode is excited in the middle wide waveguide and then coupled to the TM$_0$ mode in the narrow output waveguide. In contrast, there is no coupling for the input TE$_0$ mode due to the phase mismatching as expected. Figure 17D and E show the measured transmission spectral responses at the through port and the cross port when the TE- and TM-polarized light inputs, respectively. It can be seen that the TE-polarized light is output from the thru port and the TM-polarized light is output from the cross port. Some notable ripples are observed for TE polarization as shown in Figure 17E, which is partially due to the Fabry-Perot cavity effect resulting from the reflectivity of waveguide facets. Another possible reason for the ripples of the transmission response at the cross port is the slight misalignment of input linearly polarized light [118]. Nevertheless, the present PBS has an ER of about 13 dB over a large wavelength range, which can be improved further in the future.

An asymmetrical coupling system for the PBS can also be realized by using a bent asymmetrical directional coupler, as shown in Figure 18A. The phase matching condition for two parallel bent waveguides is given by $n_{\text{eff,0}} R_1 = n_{\text{eff,0}} R_2$, where $R_1$ and $R_2$ are the bending radii of the narrow and wide optical waveguides. It can be seen that the phase matching condition can be satisfied by making the narrow optical waveguide have a larger bending radius than the wide optical waveguide (i.e., $R_1 > R_2$) [130]. In Figure 18B and C, we show light propagation in the designed PBS with the following parameters: $L_{\text{co}} = 4.5 \mu m$, $R_1 = 19.3 \mu m$, $R_2 = 20.0 \mu m$, $w_1 = 0.534 \mu m$, $w_2 = 0.46 \mu m$, and $w_3 = 203 \mu m$. In this design, the phase matching condition is satisfied for TM polarization and the total length of the PBS is $< 10 \mu m$. It can be seen that the TM$_0$ mode is cross-coupled very efficiently while the TE$_0$ mode is output from the through port without any coupling almost (see Figure 18B and C). Figure 18D and E show the simulated and measured transmission responses at the thru and cross ports of the fabricated PBS when TE and TM polarized lights are launched respectively. It can be seen that the simulation and measurement results agree well with each other. The ER for TE polarized light is more than 15 dB in a broad band. In contrast, for the TM polarization, the
response is wavelength-dependent because of the intrinsic wavelength-dependence of the evanescent coupling. It has also been shown that this PBS has large fabrication tolerance (e.g., $\Delta w = \pm 20\, \text{nm}$) [131].

Asymmetrical coupling systems can also be realized by introducing different types of optical waveguides with giant birefringence. For example, the regular SOI nanowire can be used as one of the coupling waveguides while the other waveguide in the coupling region can be made of some special optical waveguide, e.g., silicon nano-slot waveguides [132, 133], silicon hybrid plasmonic waveguides [134, 135], etc.

Figure 19A and B show the PBS based on an asymmetrical coupling system consisting of a nano-slot waveguide and a SOI-nanowire [132]. The S-bend section for the nano-slot waveguide plays a role as a mode converter between the input/output SOI-nanowire and the nano-slot waveguide (similar to that in Ref. [136]) so that the PBS becomes very compact (~7 $\mu$m) and also convenient to integrate with other SOI-nanowire components on the same chip. The transition loss and the back reflection at the junction of the mode converter are very small because the field amplitude at the nano-slot is negligibly small for the TM polarization that is coupled to the nano-slot waveguide [132]. In the coupling region, these two waveguides are designed to satisfy the phase-matching condition for TM polarization so that it is completely cross-coupled when choosing the length of the coupling region appropriately, as shown in Figure 19C. For TE polarization, it goes through the SOI-nanowire without coupling because of the phase mismatch, as shown in Figure 19D [132]. The present asymmetrical coupling system shown in Figure 19A has an add port so that it can also be used as an add-drop device for the PDM system.

A silicon hybrid plasmonic waveguide consisting of a SOI nanowire, a metal cap and an ultra-thin SiO$_2$ layer ($h_d$) between them (see Figure 20A [137]) can also be used to realize an asymmetrical coupling system for PBSs. For example, an ultrasmall ($2 \times 5.1\, \mu$m$^2$) PBS is presented by using a three-waveguides coupling system consisting of two SOI nanowires with a silicon hybrid plasmonic waveguide between them [134]. This asymmetrical coupling system was designed to make TM polarization cross-coupled and the total length of the designed PBSs (including the bending output section) is about 5–10 $\mu$m when the gap width is chosen as small as 100 nm. In Ref.
[138], we propose a simplified ultra-short PBS by using an improved asymmetrical coupler consisting of an SOI nanowire and a silicon hybrid plasmonic waveguide, as shown in Figure 20B. These two waveguides are designed optimally to make the phase-matching condition satisfied for TE polarization (instead of TM polarization). In this way, both two waveguides have relatively large widths around 300 nm and the length of the coupling region is only about 2.2 μm when the gap width is chosen as large as 200 nm, which makes the fabrication not difficult. A sharp bending is connected at the thru port to be as a compact polarizer by utilizing its large polarization dependent loss. The designed PBS (including the bending output section) has a footprint as small as only ~1.9×3.7 μm², which is the shortest PBS reported to date. Figure 20C show the simulated light propagation in the designed PBS with L_c=2.2 μm and R=1.3 μm when the TE_0 and TM_0 modes are launched. It has been shown that this PBS has a relatively high ER (~12 dB) over a ~120 nm bandwidth while the insertion loss is only 0.025 dB and 0.66 dB for TE and TM polarizations, respectively, which is mainly due to the metal absorption [138].

3.2 Polarization rotators

Great efforts have been made to realize polarization rotation by using the hybridized-mode interference or mode evolution in an asymmetrical structure, e.g., with bends, angled sidewalls, corner-cut cross sections, etc., as summarized in Table 3. In [139, 140], the structure with periodical sections of asymmetrical load is used to realize a PR which is quite long (~3 mm) and has a large excess loss due to the scattering as well as the mode-mismatching at the junctions between alternating sections. Similarly cascaded bent sections have also been used [141, 142] and
Figure 19  The PBS based on an asymmetrical coupling system consisting of a SOI-nanowire and a nano-slot waveguide: (A) the SEM picture; (B) the cross section. The simulated light propagation in the designed PBS with $w_{co}=0.4 \mu m$, $w_{Si}=0.26 \mu m$, $h_{co}=250 \text{ nm}$, $w_{slot}=60 \text{ nm}$, and $w_{g}=100 \text{ nm}$: (C) TM; (D) TE.

Figure 20  (A) The cross section of a silicon hybrid plasmonic waveguide with field enhancement in the low index region [137]; (B) the schematic configuration of the proposed PBS; (C) the 3D-FDTD simulation for the light propagation in the designed PBS when the input is TE or TM respectively.
the PR length is as short as ~60 μm with the assistance of slant waveguide sidewalls [141]. However, the design and fabrication are quite complex. Compact PRs (~150 μm) can also be realized by utilizing the reactive ion-etch lag effect [143], as well as angled InP waveguides [144]. For silicon photonics, PRs have been demonstrated by using micrometric SOI ridge waveguides with slanted sidewalls [145–148]. However, they are as long as several hundred microns and the fabrication for slanted side-walls is not easy [148]. SOI-nanowire PRs have also been demonstrated with modified waveguide structures [149] and a 40 μm-long silicon PR based on mode evolution was demonstrated in Ref. [150], for which the fabrication is relatively easy because only a regular double-etching process is needed.

In [151], an ultra-short SOI-nanowire PR is proposed by introducing an input section, an output section and a polarization-rotation section with a cut corner (see Figure 21A and B). This polarization-rotation section supports two fully hybridized modes (see Figure 21C), which are excited equally almost and two-mode interference takes place along this section. The length of the polarization-rotation section is determined by the beat length \( L_π = \frac{\pi}{(\beta_0 - \beta_1)} \), where \( \beta_0 \) and \( \beta_1 \) are the propagation constants of these two hybridized modes, respectively. Figure 22A and B show the simulated light propagation in an optimized

<table>
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| [139] | Length: 3700 μm  
ER: ~10 dB  
EL: ~2~3 dB  
BW: NA  
Fabrication:  
Two-step etching | [143, 149] |
| [140] | Length: ~900 μm  
ER: ~18 dB  
EL: ~0.25 dB  
BW: NA  
Fabrication:  
Special etching for asymmetric side-wall. | [150] |
| [141, 142] | Length: ~60 μm  
ER: ~20 dB  
EL: 0.3 dB  
BW: NA  
Fabrication:  
Special etching for angled side-walls. | [151, 152] |
| [144] | Length: ~50 μm  
ER: ~20 dB  
EL: ~1 dB  
BW: 100 nm (for ER>15 dB)  
Fabrication:  
Special etching for angled side-wall  
Length: \( 10^0\sim10^1 \) μm  
ER: ~20 dB  
EL: ~0.2 dB  
BW: 100 nm (for ER>20 dB)  
Fabrication:  
Special etching for angled side-wall | [153] |
| [145–148] | Length: 150 μm  
ER: 14~16 dB  
EL: ~0.7 dB  
BW: 47 nm (for ER>9.5 dB)  
Fabrication:  
RIE with lag effect  
Length: <100 μm  
ER: ~15 dB  
EL: <1 dB  
BW: >100 nm (for ER>13 dB)  
Fabrication:  
Regular double etching  
Length: 6~7 μm  
ER: >20 dB  
EL: <0.1 dB  
BW: >100 nm (for ER>15 dB)  
Fabrication:  
Regular double etching  
Length: <100 μm  
ER: ~17 dB  
EL: <0.1 dB  
BW: >100 nm (for ER>10dB)  
Fabrication:  
Single-step etching  
Length: <100 μm  
ER: ~12 dB  
EL: ~0.6 dB  
BW: 35 nm (for ER>12 dB)  
Fabrication:  
Single-step etching |
PR with the following parameters: \( H = 500 \, \text{nm} \), \( W = 500 \, \text{nm} \), \( W_e = 240 \, \text{nm} \), and \( H_e = 240 \, \text{nm} \) [151]. It can be seen that the input TE polarization mode is successfully converted to the TM polarization mode at the output within a very short lengths \( L_c \approx 7 \, \mu \text{m} \), which is much shorter than those previously reported. Recently a slightly modified PR based on SOI nanowires was demonstrated experimentally [152] to show that the TE-TM polarization rotation efficiency is as high as -0.51 dB over a wavelength range of 80 nm.

In Ref. [153, 154], novel designs with a simple fabrication (needing one-step etching only) are proposed and demonstrated to enable polarization splitting and rotation simultaneously, which is very attractive for ultra-compact polarization diversity circuits. In Ref. [153], the proposed polarization splitter-rotator (PSR) consists of a taper and an asymmetrical directional coupler, as shown in Figure 23. The taper section is designed to realize the conversion from the TM\(_0\) mode to the higher-order TE mode by utilizing the mode hybridization and coupling in a high index-contrast optical waveguide with an asymmetrical cross section. For example, when the upper-cladding index of an SOI nanowire with \( h_{co} = 220 \, \text{nm} \) is not equal to that of the under-cladding layer (SiO\(_2\)), there exists mode-hybridization in the region around \( w_{co} = 0.76 \, \mu \text{m} \), as shown in Figure 24A. Figure 24B and C show the electrical-field profiles \( (E_x, E_y) \) of the two hybridized modes when \( w_{co} = 0.76 \, \mu \text{m} \). It can be seen that the \( x \)- and \( y \)-components of the electrical fields are comparable.
Due to this kind of mode hybridization, a mode conversion will happen between the TM\textsubscript{0} mode and the TE\textsubscript{1} mode when light propagates along a width-varying taper section [153–155], as shown in Figure 25A. This TE\textsubscript{1} mode is then coupled to the TE\textsubscript{0} mode of an adjacent narrow waveguide by using an asymmetrical DC (ADC) cascaded at the end of the taper as shown in Figure 23A. As a result, the launched TM\textsubscript{0} mode at the input end is converted into the TE\textsubscript{0} mode at the cross port finally (see Figure 25A). In contrast, the input TE polarization keeps the same polarization state when going through the adiabatic taper structure and is not coupled to the adjacent narrow waveguide due to the phase mismatching, as shown in Figure 25B. Such a PSR has a bandwidth of over 70 nm and the tolerance for the width deviation is about \(-10 \text{ nm} < \Delta w < 20 \text{ nm}\) for an ER of >10 dB. A larger bandwidth and fabrication tolerance can be achieved by choosing a longer taper [153]. Such mode conversion from the TM\textsubscript{0} mode to the higher-order TE mode was also observed theoretically and experimentally in submicron SOI ridge optical waveguide tapers [156]. For submicron SOI ridge optical waveguide, which is usually asymmetrical in the vertical direction even with a

**Figure 23** The structure of the PSR consisting of an adiabatic taper and an ADC [153], (A) a 3D view; (B) a top view.

**Figure 24** (A) The effective indices for the eigen-modes of SOI nanowires with Si\textsubscript{3}N\textsubscript{4} cladding (n\textsubscript{SiN}=2.0). Here the Si thickness h\textsubscript{co}=220 nm; (B) The field profiles for the hybridized modes for the SOI nanowire with w\textsubscript{co}=760 nm, h\textsubscript{co}=220 nm, and n\textsubscript{SiN}=2 (the upper-cladding).

**Figure 25** The simulated light propagation in the designed PSR when the input field is TM polarization (A), and TE polarization (B). Here the taper lengths are: L\textsubscript{tp1}=4 \textmu m, L\textsubscript{tp2}=44 \textmu m, and L\textsubscript{tp3}=L\textsubscript{tp1}(w\textsubscript{3}-w\textsubscript{2})/(w\textsubscript{1}-w\textsubscript{0}). The other parameters are w\textsubscript{0}=0.54 \textmu m, w\textsubscript{1}=0.69 \textmu m, w\textsubscript{2}=0.83 \textmu m, w\textsubscript{3}=0.9 \textmu m, w\textsubscript{g}=0.15 \textmu m, and L\textsubscript{dc}=7.0 \textmu m.
SiO₂ cladding, one can achieve mode conversion conveniently by utilizing an adiabatic taper. This paves a way to make polarization handling devices based on submicron SOI ridge optical waveguides.

4 Spatial division multiplexing (SDM) Devices: multi-core and multimode

For SDM technology, multiple channels of signals are carried by different cores or modes in parallel, which is important for long-haul optical fiber communications to higher capacity [7, 8]. SDM is also of interest for optical interconnects in data centers where upgrading an existing network or installing a new network is relatively simple [157–160]. It is even more convenient to apply SDM to the photonic network on-chip because the optical signal propagates along planar optical waveguides within the chip and the eigen-modes could be converted, transferred, as well as coupled conveniently between planar optical waveguides with some specific structures.

For the approach of using the multi-core SDM technology for photonic networks on-chip, the advantage is that the device design are easily because one does not need to deal with multiple modes. However, the drawback is the footprint issue and the increased circuit complexity. On the other hand, when using the multimode SDM technology, the waveguide design should be avoid any undesired mode coupling/conversion to low the channel crosstalk. For example, a multimode waveguide cannot be bent sharply and one has to introduce a large bending radius [161]. Besides, it is not easy to handle too many modes (e.g., >10) in a planar waveguides due to the mode coupling and crosstalk. Therefore, a potential way is combining the multi-core and multi-mode approaches to be a two-dimensional SDM technology for achieving many channels when needed. In the following section, we review the recent results for (de)MUXer devices useful for SDM technology.

Several kinds of structures for mode-(de)MUXer have been proposed. In Ref. [162, 163], a design based on multi-mode interference is proposed, which however works for two channels only and not easy to extend for more channels. Adiabatic mode-evolution couplers have been also proposed to realizing the multiplexing of only two modes [162, 163]. However, these devices suffer from several drawbacks, e.g., large footprints (~90 μm long for 2-channel multiplexing [162]), or reliance upon complicated waveguide cross-sections.

In Ref. [10, 164], a 1×N (N≥4) mode-(de)MUXer consisting of cascaded ADCs based on thin SOI nanowires (e.g., h=220 nm) was proposed as shown in Figure 26. The i-th ADC is formed by putting a narrow access waveguide close to the wide bus waveguide to form an evanescent coupling region. The bus waveguide consists of N straight segments whose widths are different and an adiabatic taper is inserted between the adjacent two straight segments. The width $w_i$ of the i-th straight segment is optimized according to the phase matching condition so that the fundamental mode of the narrow access waveguide can be coupled to the i-th higher-order mode in the bus waveguide completely. On the other hand, those undesired eigen-modes will not be excited almost due to the significant phase mismatching and consequently the crosstalk between channels is low in principle.

As an example, a 1×4 mode (de)MUXer is designed for TM-polarization operation. When the narrow access waveguides are designed to have the same width $w_s=0.4 \mu m$, the optimal widths for straight sections of the bus waveguide are chosen as: $w_1=1.02 \mu m$, $w_2=1.68 \mu m$, and $w_3=2.35 \mu m$ according to the phase matching conditions for the first, second and third higher-order modes, respectively. With a 3D finite-different time-domain (3D-FDTD) simulation, the optimal lengths for the coupling regions are achieved as $L_{c1}=4.5 \mu m$, $L_{c2}=7.0 \mu m$, and $L_{c3}=9.7 \mu m$ when the gap width $w_g=0.3 \mu m$ (see variables labeled in Figure 26).

Figure 27A–C shows the simulated light propagation in the designed ADCs. It can be seen that light is efficiently coupled from the TM₀ mode in the narrow access-waveguide to the desired higher-order mode in the wide bus-waveguide and very little power is left in the access waveguide cross-sections.
waveguide. The theoretical excess loss of the designed ADCs is almost zero (<0.1 dB) and the channel crosstalk at the central wavelength is also very low (<25 dB).

Figure 28 shows the SEM picture for the fabricated chip, which includes a 4×1 mode MUXer, a 1×4 mode demUXer, and a multimode straight waveguide between them (refer to Figure 26). Figure 29A–D show the measured transmission responses at all output ports O₁, O₂, O₃, and O₄ when light is input from port I₁, I₂, I₃, and I₄ respectively. From these Figures, it can be seen that light outputs from the corresponding output port as designed. For example, when light is input from port I₁ of the MUXer, the output power from the port O₁ of the demUXer is the maximum. The total insertion loss is about 12~13 dB, which is mainly from the large fiber-coupling loss, since there is no mode-converters at the input/output ends of the chip. By comparing to the transmission response for straight waveguides in the same chip, the (de)MUXer shows low excess loss (<0.5 dB), which is consistent with the theoretical analysis. From Figure 29A–D, it can be seen that the crosstalk is lower than 20 dB in a broad wavelength-band, which makes it possible to work together with WDM for forming a kind of hybrid multiplexing technology when the capacity is desired to be improved further. In Ref. [165], a microring-based hybrid multiplexer was demonstrated to achieve simultaneous mode and wavelength division multiplexing on chip. Error free transmission (BER<10⁻¹²) was realized by using a microring multiplexer with a crosstalk of about -13dB. Therefore, the present low-loss and low-crosstalk mode (de)MUXer should be very useful for the future applications.

For an optical interconnect link with multimode SDM technology, the multimode bus waveguide might be bent in order to change the light propagation direction to the distinction. Here we give a short discussion on light propagation in a 90°multimode bending waveguide (BWG) connecting to a straight waveguide (SWG). It is well known that a singlemode SOI nanowire can enable an ultra-sharp bending (~μm) with a low loss (including the pure bending loss and the transition loss) [44]. However, for a sharply bent multimode SOI nanowire, the modal field peak will shift outward notably. Consequently, when light propagates along an SWG connected to a BWG with a bending radius R, large transition loss and mode crosstalk are introduced due to the mode mismatch if the bending radius R is small. Figure 30A–D show the mode conversion efficiencies from the input modal field in the SWG to the eigenmodes in the BWG when the input field is the TM₀, TM₁, TM₂, and TM₃ mode of the SWG, respectively. From this Figure, it can be seen that the desired mode coupling efficiency (from TMᵢ_SWG to TMᵢ_BWG) decreases as the bending radius decreases, which is due to the increased mode mismatching. On the other hand, the undesired mode coupling (from TMᵢ_SWG to TMⱼ_BWG, j≠i) increases as the radius R becomes smaller. For example, when choosing R=240 μm, the mode coupling ratio is very small (e.g., ~0.001 or smaller) from TM₁_SWG to TM₁_BWG (j≠i). Figure 31A–D show the simulated light propagation in the structure consisting of a SWG and

![Diagram](https://via.placeholder.com/150)

Figure 27 The simulated light propagation in the designed i-th stage ADC, (A) i=1; (B) i=2; (C), i=3.

![Diagram](https://via.placeholder.com/150)

Figure 28 SEM picture for the 4×1 mode MUXer and 1×4 mode deMUXer integrated on the same chip.
a BWG with $R=240 \, \mu m$ when the input is the $TM_0$, $TM_1$, $TM_2$, and $TM_3$ modal fields, respectively. It can be seen that there is multimode interference effects, which indicates that more than one modes are excited as predicted. Therefore, the bending radius has to be large to depress the undesired mode coupling / crosstalk.

In order to achieve a small bending radius as well as low mode crosstalk, one can reduce the mode mismatching by modifying the refractive index profile with the assistance of transformation optics theory [161]. Another simple way is introducing a bending section with a gradually-varying curvature, which has been applied to bent singlemode SOI nanowires successfully [166]. When the bending radius changes adiabatically, both transition loss and mode coupling can be depressed significantly. For example, we design modified bending multimode sections for the bus waveguide, as shown in Figure 32A–D, in which there are several sub-sections whose bending radii

![Figure 29](image)

**Figure 29** The measured responses at output ports ($O_1$, $O_2$, $O_3$, and $O_4$) when light is input from port: (A) $I_1$; (B) $I_2$; (A) $I_3$; (B) $I_4$.

![Figure 30](image)

**Figure 30** The mode conversion efficiency when light is launched from a straight waveguide (SWG) to a bent waveguide (BWG) with a bending radius $R$. The input fields are the $TM_0$ (A), $TM_1$ (B), $TM_2$ (C), and $TM_3$ (D) modal fields of the straight waveguide respectively.
are chosen as $R=\infty$, 400, 200, 130, 100, 78, 62 $\mu$m. Each sub-section (except that one with $R=62$ $\mu$m) is 3.5 $\mu$m long. Figure 32A–D show light propagation in the designed 90° bent section when the input field is the TM$_0$, TM$_1$, TM$_2$, and TM$_3$ modes, respectively. From the comparison between Figure 31A–D and Figure 32A–D, it can be seen that the mode coupling becomes smaller and the crosstalk is reduced with the modified 90° bent section.

Another potential way to overcome the multimode bending issue is introducing a tall and narrow multimode bus waveguide for the ADC, whose cross section is shown in Figure 33. The multimode waveguide supports multiple higher-order modes in the vertical direction while it is quasi-singlemode in the lateral direction. In this way, the bending radius could be as small as several microns while the etching process becomes a little more complicated in comparison with that shown in Figure 26 because double-etching process is needed and the etching depth should be controlled very well. Furthermore, the etching process should be well optimized to have vertical and smooth sidewalls regarding to the high aspect ratio.

5 Outlook

5.1 Hybrid multiplexing technology

Table 4 shows the typical channel number for the multiplexing technologies discussed above. When using any one of the multiplexing technologies alone, the channel number is usually around 10 in practice currently and the link capacity is not more than 1Tbps by assuming that the bit rate is up to 100 Gbps. Therefore, the exponentially increasing demands for high link capacity (e.g., 10 Tbps) cannot be satisfied in the future. One solution is combining several multiplexing technologies to realize a multi-dimensional hybrid multiplexing technology. For example, one can use the PDM and multimode SDM technology to achieve more than 10 channels to support ~1 Tbps capacity with single-wavelength light carrier. WDM technology is then used together to enhance the link capacity of a single waveguide to about 100 Tbps with tens of channels. The optical-interconnect capacity can be further improved with the multi-core waveguide by introducing multi-core SDM technology. With this kind of

<table>
<thead>
<tr>
<th>WDM</th>
<th>PDM</th>
<th>Multimode SDM</th>
<th>Multi-core SMD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Channel number</td>
<td>4–100</td>
<td>2</td>
<td>2–8</td>
</tr>
</tbody>
</table>
multi-dimensional hybrid multiplexing technology, it is possible to achieve a capacity up to 1Petabit/s.

In order to realize the multi-dimensional hybrid multiplexing technology, the key is the hybrid (de)multiplexer for the transmitter and the receiver, which includes different types of multiplexer devices on a single chip. In this case, the related multiplexer should be designed to be compatible with each other. Figure 34 shows an example of using the PDM and multimode SDM technology to achieve ~1Terabit/s capacity with a single wavelength carrier. Here the mode MUXer should be designed to combine the eigenmodes for both polarizations. Alternatively, this can be also realized by cascading mode MUXers and a PBS with the ability to deal with higher-order modes for both polarizations, which is however a challenge because almost all the conventional PBSs are working for the fundamental modes of TE and TM polarizations. In order combine the WDM and PDM/SDM technologies, a simple way is putting WDM filters before the mode MUXer, for which the polarization-handling devices as well as the mode MUXers should be with a broad band. However, lots of waveguide crossings will be introduced for the chip layout, which causes some excess losses. The other option is putting mode MUXers before a WDM filter. In this way the WDM filter is required to have the same central wavelength for the fundamental and higher-order modes (which is a big challenge). Therefore, it can be seen that some novel devices are desired to realizing the multiplexing technologies for future on-chip optical interconnects.

5.2 Bidirectional multiplexing technology

In order to establish the communication between two chips, one should setup bidirectional optical interconnects, which usually are realized by choosing different carrier wavelengths for the forward and backward directions [167–170]. Bidirectional transmission usually has suffered from its sensitivity to backreflections, which lead to crosstalk between opposing transmitted channels and oscillation in bidirectional amplifiers. In order to solve this issue, a three-port bidirectional isolator was demonstrated [171]. Recently an integrated bidirectional optical amplifier (BOA) is proposed to allow amplified bidirectional communication of an entire WDM comb on a single link without crosstalk- and back-reflections-induced penalties, as shown in Figure 35 [172], where the four rings in the circuit have a non-reciprocal behavior [173]. For example, \( \lambda_1 \) and \( \lambda_2 \) are the CCW wavelength resonances of the rings 2 and 4, while \( \lambda_3 \) and \( \lambda_4 \) are the CW wavelength resonances of the rings 1 and 3. The two channels with \( \lambda_3 \) and \( \lambda_4 \) are injected from Port 1 and dropped to the amplifier through ring 2, and finally exit from Port 2 through the ring 4. In contrast, the back-reflections from the amplifier are not coupled back to the Port 1 and propagate towards Port S2. The reason is that ring 1 and ring 2 are out of resonance at \( \lambda_1 \) and \( \lambda_2 \) due to the non-reciprocal effect. Furthermore, the back reflections from Port 2 at \( \lambda_3 \) and \( \lambda_4 \) propagate back to Port S4 because both ring 4 and ring 3 are out of resonance in the CW direction at \( \lambda_3 \) and \( \lambda_4 \). The light injected from port 2 has similar behavior of propagation. In this way, it allows simultaneous amplification of counter-propagating WDM interleaved grids with a single amplifier (e.g., hybrid III-V semiconductor optical amplifiers).

When it is desired to used the same wavelength for a bidirectional link to avoid any additional cost for modifying the lasers, a potential simple way is using two orthogonal polarization states for the bi-directional link by utilizing the polarization handling devices (including PBSs and PRs) discussed in Section 3. Another potential way is introducing non-reciprocal devices, e.g., circulators. In Ref. [173], four-port integrated optical circulators based on MRRs have been presented, as shown in Figure 36A and B. A thin YIG (yttrium iron garnet) layer is deposited on the top of the SiN ring waveguide to achieve the magnetic-optical effect for non-reciprocity.

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**Figure 34** The schematic configuration of a hybrid multiplexed optical interconnect link combining the multimode SDM and the PDM technologies.

**Figure 35** Bidirectional optical amplifier (BOA) layout with non-reciprocal ring resonators [172].
applying a ~50 Gauss radial magneto-static field with a cylindrical magnet [174], a resonance wavelength split of $\Delta\lambda \approx 0.325$ nm can be reached with the optimal parameters $h_{\text{SiN}} = 200$ nm and $h_{\text{Ce:YIG}} = 175$ nm [173], which enables an integrated circulator with a high ER.

6 Conclusion

In this paper, we have reviewed recent progress of on-chip multiplexing technologies and devices for Peta-bps optical interconnect. CWDM technology is potentially a better option than DWDM technology due to the relaxed requirements for the wavelength alignment/control. In order to satisfy the increasing demands, more CWDM channels are needed, which is available since the transparent window for optical waveguides/fibers is large regarding the short transmission distance. The link capacity for a single-wavelength carrier can be enhanced by utilizing the PDM as well as the SDM technologies. Since the planar optical waveguide can maintain the polarization state very well, the PDM technology for on-chip optical interconnects can be simplified greatly because it is not necessary to work with advanced channel coding techniques as well as DSP. By combining these multiplexing technologies to form a kind of multi-dimensional hybrid multiplexing technology, it is possible to achieve hundreds of channels and consequently a huge link capacity as high as Petabps in total. Ultrasmall multiplexers for WDM, PDM as well as SDM have been proposed and demonstrated. However, the channel number is currently still quite limited. It will be desired to achieve more channels, especially for the WDM, and SDM technologies. In addition, in order to realize the multi-dimensional hybrid multiplexing technology, one needs to integrate different types of multiplexer devices on a single chip. Some of these multiplexers are required to be able to deal with not only the fundamental mode but also the higher-order modes, which is not easy and still under exploration. Bidirectional multiplexing technology and devices may be needed to further double the transmission capacity of an optical interconnect link.

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