Abstract: To realize nonreciprocal transmission, it is necessary to break the time-reversal symmetry of the transmission system, but it is very challenging to keep the linear polarized (LP) input and output unchanged in the free space transmission system. Magnetized semiconductor InSb can realize terahertz (THz) nonreciprocal transmission for the two conjugated photonic spin states, but it cannot realize efficient one-way transmission of LP state due to gyro-mirror symmetry. In this work, by introducing a pair of orthogonal uniaxial anisotropies from the meta-gratings on both sides of InSb, both the gyro-mirror and time-reversal symmetries are broken for the LP state, thus making this cascaded grating–InSb–grating structure serves as a high-performance isolator for the LP light. The experiment results indicate isolation of 50 dB at 0.4 THz for the same LP input and output under a weak biased magnetic field of 0.17 T. Moreover, we further illustrate the factors affecting the isolation bandwidth of the device, also demonstrated another broadband structure with the 10 dB isolation bandwidth from 0.2–0.7 THz, and the relative bandwidth achieves 110%. The mechanisms of THz nonreciprocal transmission and polarization manipulation proposed in this work will contribute to the development of efficient THz magneto-optical devices.
regulated by the direction and value of the external MF. Li et al. [23] experimentally verified the transverse MO effect of InSb, and Mu et al. [24] studied the Faraday MO effect of InSb in a longitudinal MF configuration in the experiment, and combined the InSb with artificial microstructure, realizing a linear polarization conversion with >70% MO modulation depth by the weak MF. InSb also has the potentials in designing isolators. For instance, in 2018, Lin et al. [25] proposed a reflective THz isolator with transverse MO effect of InSb, this one-way isolator achieves 35 dB isolation with 6.2 dB insertion loss for a p-wave polarization. However, it has only a narrow bandwidth and strict incident angle. The unique properties of InSb may provide more effective applications in THz nonreciprocal devices.

MO material introduced into the artificial microstructure, such as magnetic photonic crystal [26, 27], magnetoplasmonics [28–31], and MO metasurfaces [32–34], may significantly enhance the MO effect and provide singular electromagnetic transmission characteristics. In 2011, Belotelov et al. [29] demonstrated that the MO effect can be enhanced by combining the MO material with the microstructure. Wang et al. [26] constructed a nonzero Chen number in photonic crystals by using the gyromagnetic properties of YIG and first experimentally observed topological boundary states with the nonreciprocal one-way transmission in the microwave regime. In 2016, Tamagnone et al. [35] reported a THz isolator based on a multilayer stacked graphene under a strong biased magnetic field (MF) of 7 T, which exhibits the isolation of about 20 dB but insertion loss of 7.5 dB at 2.9 THz. THz MO microstructure devices provide new opportunities for the development of THz nonreciprocal transmission mechanisms and devices. THz MO microstructure provides new opportunities for the development of THz nonreciprocal transmission mechanisms.

In this paper, our goal is to achieve efficient THz isolation for the linear polarized (LP) waves without changing the polarization state, that is, the forward output wave is still an LP wave with the same polarization angle but the backward wave is forbidden to be output. To achieve this purpose, we first theoretically analyzed the non-reciprocity of the two conjugated photonic spin eigenstates in longitudinally magnetized InSb, finding that no non-reciprocity for LP state without breaking the gyro-mirror symmetry. By introducing a pair of orthogonal uniaxial anisotropies from the meta-gratings on the two sides of InSb, both the gyro-mirror and time-reversal symmetries are broken for the LP state, thus making this cascaded grating–InSb–grating structure serves as a high-performance isolator for the LP light. The above mechanisms of THz one-way transmission and polarization manipulation have been confirmed by both theory and experiments, and a further broadband result has also been demonstrated.

2 Results and discussions

2.1 Theoretical analysis

When the external MF is applied along the z-axis, the InSb shows a strong gyrotropy property. If a light propagating through the InSb also along the z-axis with Faraday configuration, Maxwell’s wave equation can be written as [17, 24]:

\[-\beta^2] \begin{bmatrix} E_x \\ E_y \\ E_z \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} + \omega^2 \mu_0 \epsilon \begin{bmatrix} \epsilon_1 & -i\epsilon_2 & 0 \\ i\epsilon_2 & \epsilon_1 & 0 \\ 0 & 0 & \epsilon_3 \end{bmatrix} \begin{bmatrix} E_x \\ E_y \\ E_z \end{bmatrix} = 0. \tag{1}\]

The detailed model of \( \epsilon_1 \) and \( \epsilon_2 \) above can be seen in Part 1 of Supplementary Information. Therefore, two eigen photonic spin states can be solved from Eq. (1):

\[\beta_{CCW} = \omega \sqrt{\mu_0 (\epsilon_1 - \epsilon_2)}, \quad \epsilon_{CCW} = (\epsilon_1 - \epsilon_2), \quad E_y = -iE_x,\]

\[\beta_{CW} = \omega \sqrt{\mu_0 (\epsilon_1 + \epsilon_2)}, \quad \epsilon_{CW} = (\epsilon_1 + \epsilon_2), \quad E_y = iE_x. \tag{2}\]

Here, the first solution \( E_y = -iE_x \) is the counterclockwise (CCW) state, and the second one \( E_y = iE_x \) is the clockwise (CW) state. The CCW state also means the forward left-handed circularly polarized light (LCP+) or backward right-handed circularly polarized light (RCP–). Meanwhile, the CW state denotes the RCP+ or LCP–. According to Eq. (3), we can theoretically calculate the transmittance of CW state through InSb as follows [24]:

\[T_{CW} = \frac{4Re\left(\sqrt{\epsilon_{CCW}}\right)}{\left[Re\left(\sqrt{\epsilon_{CCW}}\right) + 1\right]^2} \exp\left[-\frac{2\text{Im}\left(\sqrt{\epsilon_{CCW}}\right)d}{c}\right]. \tag{3}\]

where \( d = 300 \mu m \) is the thickness of the InSb layer, \( T_{CW} \) has the same form as the \( \epsilon_{CCW} \) replaces the \( \epsilon_{CW} \). The detailed results can be seen in Part 1 of Supplementary Information. Since \( \epsilon_{CW} \neq \epsilon_{CCW} \) in the same biased MF, so the time-reversal symmetry is broken to realize a nonreciprocal transmission for CW or CCW light. Moreover, when the direction of the MF or the propagating direction is inverted, \( \epsilon_{CW} (or \text{CCW}+) = \epsilon_{CCW} (or \text{CW}-) \) in the two reversed MFs, indicating a gyro-mirror symmetry for these two conjugated spin states with the positive and negative MF. It also shows that changing the MF direction is equivalent to changing the propagating direction in this work.

However, if an LP wave is incident into the InSb as shown in Figure 1(a), it can be decomposed into two
conjugated spin states in the same phase. The transmission matrix for the LP state incident into the InSb on the x–y vector basis can be written as:

\[
\begin{pmatrix}
X_{\text{out}} \\
Y_{\text{out}}
\end{pmatrix} = T_{\text{InSb}} \begin{pmatrix} X \end{pmatrix} = \frac{(T_{\text{CW}} + T_{\text{CCW}})/2}{i(T_{\text{CW}} - T_{\text{CCW}})/2}
\]

According to Eqs. (3) and (4), we calculate the transmittance map of LP incidence for the single InSb as shown in Figure 1(c), and the white area is an opaque band in the figure. When \( B = 0 \) T, there is a cutting-off frequency around 0.4 THz that the transmittance is less than −30 dB.

With the increase of the MFs, the forward wave only transmits CW wave, and the reflected wave only permits CCW wave in the cyclotron resonance frequency band. Figure 1(c) is mirror-symmetric for \( B = 0 \). Therefore, as shown in Figure 1(a), when the LP propagates forward through the InSb, the CW light transmits \( T_{\text{CW},+} \neq 0 \), and the CCW is reflected, \( T_{\text{CCW},-} = 0 \). When the LP propagates backward through the InSb (the MF direction is still unchanged), the CCW light transmits \( T_{\text{CCW},+} \neq 0 \), and the CW is reflected \( T_{\text{CW},-} = 0 \). Due to the gyro-mirror symmetry of the InSb, the transmitted waves \( T_{\text{CW},+} = T_{\text{CCW},-} \) in the above two cases, so \( T_{\text{out}} \) is a reciprocal component with the positive and negative MF \( (T_{\text{out}}(B) = T_{\text{out}}(-B)) \), half of the LP energy cannot transmit and the polarization becomes one chiral spin state. Therefore, the LP state could not be well isolated by the single InSb crystal.

Since our goal is to achieve efficient isolation for the LP waves without changing the polarization state, it is necessary to introduce a dielectric asymmetry to break the gyro-mirror symmetry while maintaining the non-reciprocity of InSb. Here, we consider utilizing the sub-wavelength dielectric meta-grating structure with artificial uniaxial anisotropy to introduce the dielectric asymmetry into this nonreciprocal transmission system. As shown in Figure 1(b), a couple of meta-gratings are placed before and after the InSb, forming a cascaded grating–InSb–grating (GIG) structure, where the grating direction of two gratings are orthogonal to each other and 45° to the incident LP direction. In this case, the transmission matrix of the whole system can be written as:

\[
\begin{pmatrix}
X_{\text{out}} \\
Y_{\text{out}}
\end{pmatrix} = T_{\text{MG}} T_{\text{InSb}} T_{\text{MG}} \begin{pmatrix} X \end{pmatrix}
\]

\[
= \frac{1}{2} \begin{pmatrix}
2\cos \frac{\delta}{2} (\cos \frac{\delta}{2} + \sin \frac{\delta}{2}) & T_{\text{CW}} \\
2\sin \frac{\delta}{2} (\cos \frac{\delta}{2} - \sin \frac{\delta}{2}) & T_{\text{CCW}}
\end{pmatrix}
\]

where \( \delta \) is the phase difference between the x- and y-polarized LP state brought by the meta-grating. For the sake of simplicity, we assume the meta-grating has the linear dispersion as \( \delta = 0.5\pi f^2 \) THz⁻¹ where \( f \) is the frequency of the wave in the theoretical analysis. According to Eqs. (3) and (5), we calculate the transmittance map of LP incidence for the GIG structure as shown in Figure 1(d). Unlike Figure 1(c), Figure 1(d) is no longer mirror-symmetric for \( B = 0 \), and the isolation can be also calculated as follows:

\[
\text{Iso} = T(B) - T(-B)
\]

where \( T(B) \) and \( T(-B) \) are the intensity transmission for the positive MF and negative MF (i.e. equivalent to the forward and backward transmission), respectively. Figure 1(e) shows the isolation map as the frequencies and MFs corresponding to the dark blue and white regions can realize efficient one-way transmission.

![Figure 1](image_url)

Figure 1: Schematic diagram of THz nonreciprocal one-way transmission based on InSb: the forward and backward LP waves incident into (a) the longitudinally magnetized InSb and (b) the InSb sandwiched in between two orthogonal meta-gratings. The theoretically calculated transmittance map as a function of frequency and the MF for the LP incidence of (c) the bare InSb and (d) GIG structure. (e) The calculated isolation for the LP incidence of GIG structure. In all the calculations, the carrier density of InSb is set to \( 4 \times 10^{18} \) cm⁻³ as the temperature is 80 K.
In special, when this meta-grating works as a perfect quarter wave-plate (QWP) \((\delta = 0.5\pi)\), the transmission matrix can be simplified as:

\[
\begin{pmatrix}
T_{X_{\text{out}}} \\
T_{Y_{\text{out}}}
\end{pmatrix} = T_{\text{QWP}} T_{\text{InSb}} T_{\text{QWP}} |X\rangle = \begin{pmatrix}
T_{\text{CW}} \\
0
\end{pmatrix}
\tag{7}
\]

Thus, the output wave only depends on the \(T_{\text{CW}}\) and has one-way transmission property since the \(T_{\text{CW}}\) is nonreciprocal as discussed above. Moreover, there is no \(y\)-component output, which means the output wave is a pure \(x\)-LP, so the frequency points that satisfy Eq. (7) can be defined as the perfect isolation case. Figure 1(b) intuitively shows the working principle of the device: when the \(x\)-LP propagates forward through the GIG structure, after passing through the first grating, the CW wave is output; then, the CW wave can pass through the magnetized InSb within the cyclotron resonance band; finally, the CW wave is transformed into \(x\)-LP wave after passing through the second grating with orthogonal orientation. When the \(x\)-LP propagates backward through the GIG structure, the CW wave is still converted, but this backward CW wave cannot pass through the InSb. In this way, the perfect one-way isolation is achieved in theory, while keeping the input–output LP unchanged. Therefore, the efficient one-way isolation band occurs in the overlapping frequency band between the cyclotron resonance of InSb and circular polarization conversion of the meta-gratings.

2.2 Experimental results

Based on the above analysis, we designed and fabricated an MO meta-grating with GIG structure as shown in Figure 2(a). Our InSb single crystal wafer was purchased from Klamar-Reagent Corporation, which was prepared by the liquid phase epitaxial method. The InSb wafer is single-side polished, 300 \(\mu\)m in thickness, (111) orientation, n-doped with the intrinsic carrier concentration of \(4 \times 10^{14} \text{ cm}^{-3}\) and the mobility of \(4 \times 10^{5} \text{ cm}^{2} \text{ V}^{-1} \text{ s}^{-1}\) at 80 K. Two Si meta-gratings with orthogonal grating orientations were fabricated on both sides of the InSb. The high resistivity Si wafer was tightly bonded to the InSb crystal. The Si was thinned by the plasma etching, and then the Si grating structures on the InSb substrate were fabricated by UV lithography and plasma etching. The meta-grating consists of two-dimensional periodic long rectangular column arrays, and its scanning electron microscope (SEM) image and the detailed geometries are shown in Figure 2(b). The structure of the backside is the same as that of the front side, but the long axis direction of the grating is orthogonal to that of the front side.

We use the terahertz time-domain magneto polarization spectroscopy (THz-TDMPS) system to experimentally demonstrated the property of the GIG as shown in Figure 2(c). Compared with the traditional THz-TDS system, the GIG sample is placed in a vacuum cryogenic Dewar bottle \((T = 80 \text{ K in our work})\) with a pair of adjustable longitudinal magnets on both sides \((B = 0–170 \text{ mT})\). There is one rotatable THz polarizer behind the THz source and the other one in front of the THz detector, which is used to generate and detect arbitrary THz polarization states, respectively. The details of the experimental system and the related data processing can be found in Part 2 of Supplementary Information.

At first, we investigated the transmission and polarization properties of the single meta-grating without InSb substrate. We measured the transmittance and phase difference along the major axis (along the \(y\)-axis) and minor axis (along the \(x\)-axis) of the grating. Meanwhile, we also obtained the numerical simulation results of the finite difference time domain (FDTD) method. The numerical modeling method can be found in Part 4 of Supplementary Information.

![Figure 2](image-url)
Information. As shown in Figure 3(a), the transmittance $T_x$ and $T_y$ for $x$-LP and $y$-LP are almost the same around 0.1–1 THz. And in Figure 3(b), the phase difference between $x$-LP and $y$-LP is decreasing with the frequency. In particular, the phase difference comes to 90° near 0.5 THz, so the grating is close to an ideal QWP. According to the above theoretical analysis, the GIG structure is expected to achieve efficient one-way transmission near this frequency point under the MF.

Then, we focus on the nonreciprocal transmission property of the MO meta-grating with the GIG structure. We placed both THz polarizers to 0°, that is $y$-LP wave is incident into the GIG device, and the experimental system detects the $y$-LP component of the output wave. The transmission spectra of the LP wave passing through the GIG are shown in Figure 3(c). When $B = 0$ T, the transmittance is less than $-10$ dB in the frequency range of $f < 0.7$ THz. With the increase of the positive MFs, the cutting-off frequency gradually moves to the lower frequency as the transmittance increasing. On the contrary, when the negative MFs are applied, the cutting-off frequency gradually moves to a higher frequency with the decrease of transmittance. The experimental results are in good agreement with the theoretical calculation in Figure 1(d), and they are also verified by numerical simulations (see Part 4 of Supplementary information). Therefore, there is a nonreciprocal transmission band for the LP waves in the frequency range of 0.38–0.68 THz. Figure 3(d) shows the isolation between forward and backward transmission defined as $\text{Iso} = T(+B) - T(-B)$ in dB. The isolation peak moves to high frequency and the isolation band (>10 dB) expands with the increase of MFs. Although the QWP point for the Si grating is 0.5 THz, when we combined the grating with the InSb, the impedance match condition of the grating is changed, thus making the QWP point of the GIG structure moves to the lower frequency. Therefore, when $B = 0.17$ T, the best isolation point can reach 50 dB at 0.42 THz with the 10 dB isolation bandwidth of 400 GHz.

Moreover, we analyzed the complete polarization state output through the GIG. When the frequency band deviates from the ideal QWP, the actual output wave will be an elliptical polarization state. We calculate the polarization ellipse as shown in Figure 4, we select two frequency points: $f = 0.42$ and 0.8 THz. When $f = 0.42$ THz, for the forward MFs, the amplitude growing with the MFs, and when $B = 0.17$ T, the output wave is almost the perfect LP state. However, for the backward MFs, the amplitude decreasing with the MFs, showing the isolation effect. For $f = 0.8$ THz, for the forward MFs, the polarization state turns counter clock-wise, but for the backward MFs, the polarization state rotates clock-wise. Thus, in the higher frequency range of $f > 0.8$ THz, this structure shows the Faraday rotation effect which means the rotation angle can be turned by the MFs. For the details of related experimental measurement and data processing, please refer to Part 3 of Supplementary Information.
2.3 Discussion for loss and bandwidth

Finally, as shown in Figures 3(c) and 5(c), the transmittance also reflects the total insertion loss of the device, and the lowest insertion loss is 6.7 dB for the first GIG structure and 6.9 dB for the second GIG structure, respectively. Two main factors contribute to the total loss of the device: the intrinsic absorption loss of the InSb and the surface reflection loss from the grating structure and interfaces. We think there are two ways to reduce the insertion loss in the future: one is to fabricate the InSb wafer with a lower intrinsic carrier concentration, and the second is to design a more optimized microstructure to achieve better impedance matching on the interfaces of the air/grating and grating/InSb.

According to the nonreciprocity mechanism discussed in Section 2.1, the bandwidth of the device is determined by two factors: (1) the frequency band of InSb cyclotron resonance (including the position of resonance frequency determined by the MF and the resonance bandwidth determined by carrier collision frequency); (2) the frequency band of \(\pi/2\) phase shift is realized by meta-grating as a THz QWP. When these two frequency bands are overlapped in the same frequency range, the perfect isolation case described in Eq. (7) can be achieved. The larger the overlap range is, the larger the 10 dB isolation bandwidth is. For a specific MO material, the cyclotron resonance bandwidth is constant, and the resonance center frequency can be tuned by the external magnetic field. Under these conditions, if a meta-grating can be designed as the THz QWP with enough broad bandwidth, a broadband LP isolator can be realized.

Therefore, we also designed and fabricated a subwavelength grating as a broadband QWP to obtain a broadband GIG. As shown in Figure 5(a), the transmittances of \(x\)- and \(y\)-LP components are almost the same. However, the phase difference between them has two 90° points at 0.38 and 0.75 THz as shown in Figure 5(b). By combining these gratings with InSb, the transmittance and the isolation spectra under the different MFs can be seen in Figure 5(c) and (d). With the growth of the MFs, the transmittance increases under the positive MFs, while the transmittance decreases under the negative MFs. Different from the above results in Section 2.2, for the large MF \((B = 0.17 T)\), the 10 dB isolation bandwidth is broader because these meta-gratings have two perfect QWP points.
which satisfy Eq. (7), its isolation band is located from 0.2 to 0.7 THz with the relative bandwidth of $\Delta f/f_{cen} > 110\%$, where $f_{cen}$ is the center frequency of this device.

### 3 Conclusions

In summary, by combining the meta-gratings with the gyroelectric semiconductor InSb, we proposed a THz isolator for the LP input to LP output. Through theoretical modeling and analysis, we demonstrate that the gyro-mirror symmetry of the InSb for the LP state can be broken by introducing a pair of orthogonal uniaxial anisotropies from the meta-gratings on the two sides of InSb. The experiment results indicate this THz MO device with the cascaded GIG structure isolation of 50 dB at 0.4 THz for the same LP input and output under the weak biased MF of 0.17 T, which are well consistent with the theoretical calculation and numerical simulation. Moreover, we further concluded the factors affecting the 10 dB isolation bandwidth of the device, and also demonstrated a broadband GIG structure with the 10 dB isolation bandwidth from 0.2–0.7 THz, and the relative bandwidth achieves 110%. This THz nonreciprocal transmission mechanism and device structures proposed in this work will contribute to the development of efficient THz magneto-optical isolators and polarization converters, and promote the further development of THz high power sources and highly sensitive detection systems.

**Author contribution:** Z-Y Tan: Investigation, Methodology, Resource, Writing—original draft; F Fan: Conceptualization, Investigation, Writing—review & editing, Supervision. D Zhao: Experiment. S-S Li: Scanning electron microscope operation. X-H Wang: Experiment administration. S-J Chang: Project administration. All the authors have accepted responsibility for the entire content of this submitted manuscript and approved submission.

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