Research Article

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Analysis of magnetized micropolar fluid subjected to generalized heat-mass transfer theories

https://doi.org/10.1515/phys-2023-0117
received September 10, 2022; accepted September 21, 2023

Abstract: In this study, the steady 2D flow of micropolar fluid via a vertical surface is taken into account. The magnetohydrodynamics applied normally to the flow direction at a vertical surface in the presence of temperature-dependent attributes. The effect of the chemical reaction under the generalized Fourier–Fick law is considered to investigate the heat transference rate at the vertical sheet. Under the flow assumptions, the boundary layer approximations were applied to the nonlinear differential equations and partial differential equations were obtained. The use of similarity modifications allows for a reduction in the number of partial differential equations. The resulting ordinary differential equations are then resolved numerically using a technique known as the homotopy analysis method. The results reveal that microparticle suspensions have a significant impact on the flowing domain when varied fluid characteristics are utilized. The effect of potential factors on flow, micro-rotation velocities, temperature, drag force factor, and heat transport rate is investigated. The obtained results show that the velocity profile and micropolar function increase for larger values of micropolar parameters. Drag force effects are also seen, and required outcomes are observed to be in outstanding accord with the available literature. Significant results of this work were toward the velocity function, which gets reduced with increasing magnetic field parameter values, but the velocity function enhances for higher values of $\beta$ and $\lambda$. On temperature distribution, it decreased for higher values of $\epsilon_3$ and temperature profile declines due to higher values of $Pr$, $y_2$ and $y_1$ or both cases of $\delta > 0$ and $\delta < 0$. The higher values of $Sc$ resist declining the temperature function at the surface.

Keywords: generalized Fourier–Fick laws, micropolar fluid, mixed convection, heat generation, temperature dependent properties

Nomenclature

\[(u, v)\quad\text{horizontal and vertical fluid velocities}\]
\[\rho\quad\text{fluid density}\]
\[\nu\quad\text{kinematic viscosity}\]
\[k\quad\text{vertex viscosity}\]
\[g\quad\text{gravitational acceleration}\]
\[\beta_1\quad\text{thermal expansion coefficient}\]
\[\beta_2\quad\text{solutal expansion coefficient}\]
\[\gamma^*\quad\text{spin gradient viscosity}\]
\[j\quad\text{density due to micro-inertia}\]
\[\lambda_T\quad\text{thermal relaxation time flux}\]
\[\lambda_C\quad\text{solutal relaxation time flux}\]
1 Introduction

Fourier's relation [1] has been used in various industrial and technological applications for energy transportation by means of heat conduction. While implementing this relation, a parabolic type of energy expression is observed; this is the inadequacy of this relation. Different researchers try to overcome this inadequacy in Fourier's relation. Cattaneo [2] introduced the thermal relaxation parameter in Fourier's relation. Cattaneo analysis [2] has been improved significantly by Christov [3] with the addition of Oldroyd's type upper convective derivative in the thermal relaxation term. In micropolar liquids, every molecule having a limited size contains a microstructure that can turn and twist freely regardless of the movement of the centroid of the molecule. The micropolar hypothesis provides an elective way to deal with mathematically settling the micro-scale liquid elements. Nonlinear convective stagnation point flow under modified Fourier's and Fick laws subject to temperature-dependent thermal conductivity is elaborated by Zubair et al. [4]. Waqas et al. [5] investigated revised Burgers' liquid by using enhanced Fourier–Fick laws in stretchable flow under the impermeable stretching sheet. Novel nonlinear models related to micropolar fluid regarding boundary layer flow are established by Sui et al. [6]. Mixed convective Burger's fluid flow on a stretching surface considering heat generation and variant thermal conductance is elaborated by Waqas et al. [7]. Anwar et al. [8] discussed homotopic solutions for Jaffrey fluid exposure based on modified Fourier's and Fick's principles. Bioconvection magneto-hydrodynamics (MHD) Carreau nanoliquid flowing over a parabolic sheet considering improved Fourier's and Fick rules is presented by Khan et al. [9]. Three-dimensional Sisko liquid considering global heat flux and mass diffusion relationships along with temperature-based thermal conductance is numerically investigated by Khan et al. [10]. Hayat et al. [11] used Fourier–Fick laws along with variable thermal conductivity to study the Jaffrey fluid flowing by a rotary disk having a changeable thickness. Devi and Prakash [12] explored the effects of temperature-dependent characteristics of liquid on hydro-magnetic flowing over a slandering stretching sheet. The Fourier relation is ineffective for solving situations that include a large thermal gradient, temperatures below absolute zero, short temperature shifts, and nano/micro-scales in space and time [13]. Nanoliquid squeezed flow subjected to generalized fluxes is presented by Noor et al. [14]. The traditional heat conduction relation [15] communicates heat flux precisely to temperature gradient utilizing the coefficient of thermal conductivity. For illustration, Daneshjou et al. [16] formulated time-dependent flow in 2D orthotropic non-Fourier based hollow cylinders. Khan et al. [17] reported research that examined the influence of thermal radiation on the flow of chemically reacted Burger's liquid toward a heated surface. By applying the coefficient of thermal conductivity, the conventional relation for heat conduction [18] can accurately convey the relationship between heat flow and temperature variation. For the purpose of illustrative purposes, Alsaeedi et al. [19] developed chemically reacted flow in the stagnation area of Burgers liquid. Tibullo and Zampoli [20] recognized individuality outcomes for incompressible nature problems subjected to modified Fourier law. Analytical consideration of forced convection stratified Burger's fluid movement was given by Waqas et al. [21] in accordance with the improved Fourier law. Khan et al. [22] studied the effects of using an enhanced version of the Fourier law on changeable liquid characteristics in a stratified Carreau nanoliquid. The thermally radiating stratified Jeffrey nanoliquid that was exposed to buoyancy forces was proposed by Waqas et al. [23]. Heat conduction expression via the Fourier situation has a parabolic form, which enables thermal instabilities to communicate the thermal propagation of waves having infinite velocity. This phenomenon has to be enhanced at very smaller time scales and lengths in only a few nano/micro-scale structures. A large number of scholars have made contributions to additional advances that have been analyzed using the Cattaneo model.

The study of the behavior of non-Newtonian liquids has recently gained attention due to its rheological applications in chemically and mechanistic manufacturing activities. Among the industrial uses are oil extraction, artificial production development, nutrition administration, and the performing of coats and oils. Non-Newtonian liquids are commonly used in production and manufacturing processes. There is a non-linear relationship among shearing stress and shearing rate, and the shearing rate is modified by the shear stress period. In the literature, several rheological models exist to illustrate certain physical features of non-Newtonian liquids, such as the viscoelastic fluid model and secondly ordered liquid type, Walter's liquid type, Cattaneo/Christov heat fluxing type, Maxwell liquid framework, and so on. Furthermore, the micro-polarized liquid type is an important model for non-Newtonian liquids for understanding the provenances of liquid transmission and heat transference in several complex liquid-flowing situations. 
The traditional Navier–Stokes principal hydrodynamic concept has important shortcomings, such as the inability to depict liquids with the rotational, body downforce, couple-stress, microstructures, and micro rotations, which are critical in analyzing the flowing behavior of liquids such as melted crystalline, polymer liquids, hemoglobin, colloids' liquids, lifeblood serum, actual liquids with postponements, dye, and so on. The liquid rapidity is sufficient to define the flowing issue of a liquid containing suspensions of stiff molecules or micro-structural these fluids, but the angular impetus is also necessary since each particle in the liquid rotates separately along an axis of movement. Eringen [24] developed the micro-polarity liquid concept to quantify the impacts of micro inertia and micro rotation that the traditional hydrodynamic framework does not comprehend, considering this empathic behavior of the fluid molecules into consideration. Khedar et al. [25] studied micro-polar liquid flowing across an expanded plate with heat generating (absorbing). Ishak [26] and Hussain et al. [27] studied the effect of radiative fluxing on the temperature boundary layer movement of a micro polarity liquid over a stretchable plate. An examination [28] used an exponential declining porousness sheet to investigate micropolar fluid and heat-flowing transfer. The results of Ohmic heating and viscosity dissipative of micro polarity liquid flow via an expanded plate were presented by Haque et al. [29]. Numerous studies have extensively examined the micro-polar liquid in different spatial formations, as seen by the publications [30–32].

Nevertheless, boundary layer issues with various thicknesses are commonly encountered in engineering disciplines. The researchers became interested in analyzing the flow, heat flux, and diffusion attributes via a stretchable plate with a changeable thicker due to its outstanding significance in manufacturing and production developments such as mechanical systems, architectural styles, maritime and aerospace structural systems, powder metallurgy, polymer extruding, and metallurgic progressions. Fang et al. [33] quantitatively investigated the varied thicknesses' impact on boundary layer movement through the stretchable plate, displaying the shift in rapidity and shearing stress of a plate affected by its non-uniformity. Khader and Megahed [34] used a similar geometry to investigate the impact of slippage rapidity and exponential rapidity on the movement of a Newtonian fluid. Using the same configuration, Hayat et al. [35] studied the magneto flowing of a heat fluxing of Cattaneo/Christov kind for non-Newtonian liquids. Cortell [36], on the other hand, addressed heat transmission through a viscosity flowing. Yang et al. [37] investigated the rapidity and temperature of a varying extended plate in the presence of double fractions of Maxwell fluid. Abdel-wahed et al. [38] investigated heat transmission and the transmission of a nanoliquid over a moving surface with changing thicknesses. Few studies on different aspects of physical phenomena were analyzed by various researchers [39–47]. Because it is used in ablation cooling, rocket motor burning, pulmonary circuit air movement, and binary gas dispersion, fluidization in tubes is prevalent in industrial and molecular genetics. Fluid properties such as diffusion coefficient, viscosity, conductance, and so on are assumed to remain unchanged for the dexterity of analysis. However, diverse fluid qualities are used in food processing, fiber and wire coating, extrusion processes, chemical manufacturing aids, and other activities. The frictional force caused by viscosity determines the amount of heat transferred by the flowing and is critical in the compilation of fluid measuring for flowing visualization. When the viscous dissipative flow in nearly all actual fluids is observed, the viscosity changes with temperature influences. The viscosity of several fluids, such as honey, syrup, and blood, is affected by temperature. Thermal conductance is an important thermophysical property that impacts the rate of heat transfer in micropolar fluids, which is important when working with heat-generation items like electrical equipment and heat-resistant composites.

With the insight of the aforementioned kind of literature, this work was planned to study the significant thermal characteristic aspects of micro-polar fluid in a chemical reactive environment. Toward the applicability in energy industries, the heat transference analysis has been made in the presence of varying qualities of thermal conductivity and mass diffusivity under generalized Fourier–Fick laws. The novelty of this work can be noted that to the best of the authors' view, this work could be a fresh attempt to study the effects of MHD-based micropolar fluid flow with temperature-dependent properties on a vertical stretching sheet. It will be interesting to explore how under this above circumstance how the MHD-based micro polar fluid flow behaves while passing over another shape with various physical constraints.

2 Mathematical modelling

We formulated the incompressible steady 2D flow of micropolar fluid under generalized Fourier–Fick laws. Heat generation aspects are included. Also, variable thermal conductivity and mass diffusivity are introduced. Non-Newtonian mixed convective flow is considered. The expressions governing the micropolar fluid flow are

\[ \nabla \cdot \mathbf{V} = 0, \]

\[ \rho \frac{DV}{Dt} = -\nabla p + (\mu + k)\nabla \times \nabla \times \mathbf{V} + k \nabla \times \mathbf{N}, \]
\[
\rho \frac{\partial u}{\partial t} = y \nabla (u \cdot \nabla N) - \nabla \times (\nabla \times N) + k \nabla \cdot \nabla - 2kN, \tag{3}
\]

where \( \frac{\partial}{\partial t} \) represents the material derivative, \((V, N)\) represents the (velocity, microrotation) vectors, \(j\) and \(\rho\) illustrate the fluid gyration factor and density, \(\mu\) represents the dynamic viscosity, and \(k, y\) represents the (vortex, spin gradient) viscosity.

The governing boundary-layer equations under the aforesaid assumptions are as follows [26]:

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \tag{4}
\]

\[
 \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \left( y + k \frac{\partial^2 u}{\partial y^2} + \frac{k}{\rho} \frac{\partial N}{\partial y} \right) + g [\beta_z(T - T_m) + \beta_C(C - C_m)] - \frac{\sigma B_0^2 u}{\rho}, \tag{5}
\]

\[
 \frac{\partial N}{\partial x} + v \frac{\partial N}{\partial y} = v' \frac{\partial^2 N}{\partial y^2} - \frac{k}{\rho} \frac{\partial u}{\partial y} + 2N, \tag{6}
\]

\[
 \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + \lambda_T \left( \frac{\partial u}{\partial x} + v \frac{\partial T}{\partial y} + \frac{\partial u}{\partial x} \right) + u' \frac{\partial^2 T}{\partial y^2} + 2\nu' \frac{\partial^2 T}{\partial x^2} + v' \frac{\partial^2 T}{\partial x^2} \right) + \frac{\partial^2 T}{\partial y^2}, \tag{7}
\]

\[
 \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + \lambda_C \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + \frac{\partial u}{\partial x} \frac{\partial C}{\partial y} + \frac{\partial v}{\partial y} \frac{\partial C}{\partial x} + \frac{\partial u}{\partial x} \frac{\partial C}{\partial x} + \frac{\partial v}{\partial y} \frac{\partial C}{\partial x} \right) + 2\nu' \frac{\partial^2 C}{\partial x^2} + v' \frac{\partial^2 C}{\partial x^2} \right) \frac{\partial C}{\partial y}, \tag{8}
\]

Boundary constraints used for this inspection are [26]

\[
\begin{align*}
\begin{cases}
\frac{\partial u}{\partial y} = 0, & N = 0, \\
T = T_m, & C = C_m \text{ at } y = 0, \\
u \to 0, & T \to T_m, \quad N \to 0, \quad C \to C_m \text{ when } y \to \infty,
\end{cases}
\end{align*}
\]

where \((u, v)\) represents the horizontal and vertical fluid velocities, \(\rho\) represents the fluid density, \(v\) represents the kinematic viscosity, \(k\) represents the vertex viscosity, \(\gamma\) represents the gravitational acceleration, \(\beta_z\) represents the thermal expansion coefficient, \(\beta_C\) represents the solutal expansion coefficient, \(\gamma'\) is the spin gradient viscosity, \(j\) signifies the density due to micro-inertia, \(\lambda_T\) is the thermal relaxation time, \(\lambda_C\) is the solutal relaxation time flux, \(c_p\) is the specific heat, and \(Q\) is the heat generation coefficient.

Regarding the boundary conditions, \(c\) is the constant, \(m_0\) is the boundary layer parameter, \(N\) velocity due to micro-rotation, \(T, T_m\) and \(C, C_m\) represent the fluid, wall temperature, and concentricity of the normal regime, and \(T_0, C_0\) denote the fluid temperature and concentricity of ambient regime correspondingly.

Mathematically variable thermal conductivity and mass diffusivity are defined as follows:

\[
K(T) = K_m (c \theta(\eta) + 1), \quad D(C) = D_m (c \phi(\eta) + 1),
\]

where \(K_m\) and \(D_m\) are ambient fluid thermal conductivity and mass diffusivity, and \(\varepsilon_1\) and \(\varepsilon_2\) are arbitrary small parameters. By applying a flowing group of transformations

\[
\begin{align*}
\eta &= y \sqrt{\frac{C}{\sqrt{V}}}, \quad N = \sqrt{\frac{C}{\sqrt{V}}} g(\eta), \quad u = cxf'(\eta), \\
v &= -\sqrt{cv} f'(\eta), \quad \theta(\eta)(T_0 - T_m) = T - T_m, \quad \phi(\eta)(C_0 - C_m) = C - C_m,
\end{align*}
\]

Eq. (4) is derived obviously while formulas (5)–(8) are as follows:

\[
(1 + K) f'''' + P_{ff} f'' - f' - g'K + \lambda(\beta + \phi) - M f'' = 0, \tag{11}
\]

\[
\left[ 1 + \frac{K}{2} \right] g'' + g' - g'' - K(f'' + 2g) = 0, \tag{12}
\]

\[
(1 + \varepsilon_1 \theta) \theta'' + \varepsilon_2 \theta'' + P_{ff} \theta'' - P_{ff} \theta'' - P_{ff} \theta'' = 0, \tag{13}
\]

\[
(1 + \varepsilon_1 \phi) \phi'' + \varepsilon_2 \phi'' + S_{cccc} \phi'' + S_{cccc} \phi'' = 0, \tag{14}
\]

\[
f(\theta) = 1, f(0) = 0, f(\infty) \to 0, \tag{15}
\]

\[
g(\phi) = -m_0 f''(0), \quad g(\infty) \to 0, \tag{16}
\]

\[
\theta(0) = 1, \quad \theta(\infty) \to 0, \tag{17}
\]

\[
\phi(0) = 1, \quad \phi(\infty) \to 0. \tag{18}
\]

The skin frictional factor in dimensionless structure is

\[
C_f = \frac{(1 + (1 - m_0)K) f''(0)}{\text{Re}_k^{1/2}}. \tag{19}
\]

### 3 Solution procedure

The homotopy analysis method (HAM) [48] is utilized to calculate the convergent outcomes of non-dimensional expressions (11)–(14) while considering the imposed boundary conditions (15)–(18). The initial guesses \((f_0(\eta), \phi_0(\eta), \theta_0(\eta), \phi_0(\eta))\),
as well as the necessary auxiliary operators \((L_f, L_g, L_\theta, L_\phi)\) for HAM computations, are as follows:

\[
f_0(\eta) = 1 - e^{-\eta}, \quad g_0(\eta) = m_0 e^{-\eta}, \quad \theta_0(\eta) = \exp(-\eta), \quad \phi_0(\eta) = \exp(-\eta),
\]

\[
L_f = \dot{f}' - f', \quad L_g = \dot{g}' - g', \quad L_\theta = \theta'' - \theta, \quad L_\phi = \phi'' - \phi.
\]

The operators \((L_f, L_g, L_\theta, L_\phi)\) must validate the ensuing properties:

\[
L_f(B_1^* + B_2^* e^{\eta} + B_3^* e^{-\eta}) = 0, \quad L_g(B_4^* e^{\eta} + B_5^* e^{-\eta}) = 0, \quad L_\theta(B_6^* e^{\eta} + B_7^* e^{-\eta}) = 0, \quad L_\phi(B_8^* e^{\eta} + B_9^* e^{-\eta}) = 0,
\]

where \(B_i^* (i = 1-9)\) signify arbitrary factors.

The embedding factor is exhibited through \(w^*\); however, auxiliary factors are denoted by \(h_f, h_g, h_\theta, \text{ and } h_\phi\).
4 Convergence analysis

We used a homotopy scheme [48] to analyze convergent solutions. It is clear that \( h \)-curve (s) perform a fundamental part in analyzing the convergence of nonlinear differential systems. That is why the \( h \)-curve in Figure 1 is shown to predict our objective. A flat portion of the \( h \)-curve helps to obtain usable values of \( h_f, h_j, h_g, \) and \( h_\phi \). We examined that 

\[-1.25 \leq h_f \leq -0.247, \quad -1.27 \leq h_g \leq -0.24, \quad -1.5 \leq h_\phi \leq -0.4, \quad \text{and} \quad -1.8 \leq h_\phi \leq -0.4 \]

along with the assumptions \( K = n = 0.5, \lambda = 0.1, M = \epsilon_1 = \delta = y_1, N = 0.2 = \epsilon_2 = y_2, \) \( Sc = 0.8, \) and \( Pr = 1.1 \). In addition, converging is seen computationally with the assistance of Table 1. Table 2 displays comparison upshots of employed methodology (HAM) for authentication with earlier simulations of Akbar et al. [49]. The analytical upshots of \( C_{Re} \) are in decent settlement subjected to different parametric variations of \( M \).

5 Results and discussion

Figures 2–6 reveal the characteristics of distinct variables against the velocity profile \( f'(\eta) \). Figure 2 shows that as the vertex velocity \( K \) increases, the rapidity outline increases due to the impact of the vertex effect. Figure 3 shows the outcome of the boundary parameter over the velocity.

Table 1: Converging investigation in diverse order approximations when \( K = n = 0.5, \lambda = 0.1, M = \epsilon_1 = \delta = y_1, N = 0.2 = \epsilon_2 = y_2, \) \( Sc = 0.8 \) and \( Pr = 1.1 \).

<table>
<thead>
<tr>
<th>Approximation order</th>
<th>(-f''(0))</th>
<th>(-g''(0))</th>
<th>(-\theta'(0))</th>
<th>(-\phi'(0))</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.8560</td>
<td>0.3780</td>
<td>0.7351</td>
<td>0.7045</td>
</tr>
<tr>
<td>5</td>
<td>0.8423</td>
<td>0.3750</td>
<td>0.5576</td>
<td>0.5374</td>
</tr>
<tr>
<td>10</td>
<td>0.8402</td>
<td>0.3742</td>
<td>0.5263</td>
<td>0.5018</td>
</tr>
<tr>
<td>15</td>
<td>0.8394</td>
<td>0.3739</td>
<td>0.5183</td>
<td>0.4895</td>
</tr>
<tr>
<td>20</td>
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<td>0.3738</td>
<td>0.5161</td>
<td>0.4836</td>
</tr>
<tr>
<td>30</td>
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<td>0.3737</td>
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<td>0.4825</td>
</tr>
<tr>
<td>40</td>
<td>0.8388</td>
<td>0.3737</td>
<td>0.5159</td>
<td>0.4825</td>
</tr>
</tbody>
</table>

Figure 2: Influences of vertex velocity \( K \) on flow \( f'(\eta) \).

Table 2: Comparative outcomes featuring \( C_{Re} \) for different estimations of \( M \).

<table>
<thead>
<tr>
<th>( M )</th>
<th>Ref. [49]</th>
<th>Present findings</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>-1.00000</td>
<td>-1.00000</td>
</tr>
<tr>
<td>0.3</td>
<td>-1.01980</td>
<td>-1.01980</td>
</tr>
<tr>
<td>0.5</td>
<td>-1.11803</td>
<td>-1.11803</td>
</tr>
<tr>
<td>0.7</td>
<td>-1.28063</td>
<td>-1.28062</td>
</tr>
<tr>
<td>1.0</td>
<td>-1.41421</td>
<td>-1.41421</td>
</tr>
</tbody>
</table>

Figure 3: Influences of boundary parameter \( n \) on flow \( f'(\eta) \).
profile, which shows that the velocity function declines due to a mass of the value of boundary parameter $n$. Figure 4 interprets the difference in the rapidity function for diverse amounts of $\lambda$. It shows that relaxation time flux $\lambda$ increases the velocity due to improved momentum. Figure 5 depicts the micro-rotation velocity against the velocity profile. It illustrates assistance gained by the flow velocity from the micro-rotational aspects. Figure 6 clearly expresses the impact of the Lorentz force due to increasing magnetic field $M$ which suppresses the flow velocity. Figures 7 and 8 show that lateral directional flow $g(\eta)$ increases for larger values of vertex velocity $K$ and vortex rotation $N$.

Figure 9 reports arbitrary thermal conductivity $\epsilon_1$ characteristics on $\Theta(\eta)$. Clearly, $\Theta(\eta)$ increases as $\epsilon_1$ increases due to increased thermal conductivity, which assists the heat transfer.
transfer. Figure 10 elaborates that a larger Pr value yields less diffusivity which reduces the temperature profile $\theta(\eta)$. Figure 11 addresses ($\delta > 0$) the heat generation and ($\delta < 0$) heat absorption variables against the temperature profile $\theta(\eta)$. It illustrates that $\delta > 0$ increases the temperature dispersion due to improved heat generation, whereas $\delta < 0$ decreases the temperature dispersion $\theta(\eta)$ due to heat absorption. Figure 12 depicts that the temperature profile decreases by increasing the values of the velocity spin gradient $\gamma_1$, which is related to the non-conductivity comportment caused by which $\theta(\eta)$ decreases. Figure 13 shows the behavior of the thermal spin gradient $\gamma_2$.

Figure 14 shows the Schmidt number $Sc$ and its impact on concentration dispersal $\phi(\eta)$. Here, flow concentration $\phi(\eta)$ reduces by increasing $Sc$ values work against the mass transference process. Schmidt number $Sc$ describes Brownian diffusivity which has opposite behavior with concentration dispersal. Figure 15 shows the characteristics of arbitrary mass diffusivity $\epsilon_2$ on flow concentration $\phi(\eta)$. It is clear that larger values of $\epsilon_2$ improves mass diffusivity, which raises the flow concentration $\phi(\eta)$. Figures 16 and 17 illustrate the influence of vertex velocity $K$ and relaxation time flux $\lambda$ the skin friction, respectively. Vertex velocity $K$ favors the flow movement, which acts against skin friction, while relaxation time flux $\lambda$ enhances the skin friction due to more contact time availability between fluid and the surface.
6 Final remarks

In the occurrence of the generalized Fourier–Fick rule, we examined how the temperature-dependent features of the micropolar fluids affected the flow of the MHD fluids as they passed through the vertical linear stretchable sheet. In order to get the numerical findings, an effective version of the HAM was used. The following is a list of the major results obtained from this work:

- For higher micro-planar rotation, the velocity and micropolar functions get elevated.

Figure 13: Effects of spin gradient viscosity \( \gamma_2 \) on thermal dispersal \( \theta(\eta) \).

Figure 14: Effects of Schmidt number \( \text{Sc} \) on concentration \( \phi(\eta) \).

Figure 15: Effects of arbitrary concentration parameter \( \epsilon_2 \) on concentration \( \phi(\eta) \).

Figure 16: Effects of vertex velocity \( K \) on Skin friction \( C_f \text{Re}^{1/2} \).

Figure 17: Effects of relaxation time flux \( \lambda \) on Skin friction \( C_f \text{Re}^{1/2} \).
• Constraints like solutal and thermal expansions work in favor of the flow to increase its velocity while the magnetic field parameter tends to suppress the flow through the Lorentz force.

• Thermal dispersal gets assisted by thermal conductivity $\epsilon_1$ and both cases of $\delta > 0$ and $\delta < 0$ heat generation constraints are for higher values of $\epsilon_1$ and temperature profile declines due to higher values of Prandtl number $Pr$ and Spin gradient $\gamma_1$.

• Concentration dispersal $\phi(\eta)$ gets improved for the increasing diffusivity $\epsilon_5$, on contrary the Spin gradient $\gamma_2$ and Schmidt number $Sc$.

• The skin friction decreases for the viscous alterations $K$ and time relaxation constraints $\lambda$.

7 Future insights

In this work, the effects of MHD-based micropolar fluid flow with temperature-dependent properties on a vertical stretching sheet under Fourier–Fick laws were studied. It could create a greater impact on the thermal and mass transfer research stream. In the future, such concepts can be extended for flow past various geometries with numerous types of fluids such as nanofluid, hybrid nanofluid, and ferrofluids. The existing scheme could be applied to a variety of physical and technical challenges in the future.

Funding information: The authors state no funding involved.

Author contributions: Conceptualization: Muhammad Imran Anwar; formal analysis: Muhammad Saqlain; investigation: Muhammad Waqas, M. Prakash, and Abdul Wahab; Methodology: Muhammad Waqas, M. Prakash, and Abdul Wahab; software: Wasim Jamshed; writing – original draft: Mohamed R. Eid; validation: Wasim Jamshed and Mohamed R. Eid; re-graphical representation: Nek Muhammad Katbar; computational process breakdown: Yijie Li; Re-modelling design: Ahmed M. Hassan. All authors have accepted responsibility for the entire content of this manuscript and approved its submission.

Conflict of interest: The authors state no conflict of interest.

Data availability statement: All data generated or analyzed during this study are included in this published article.

References