An ESR Investigation of Synthetic Pyrite Crystals

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Synthetic pyrite crystals doped with halogen (Cl, Br) or manganese (Mn) were investigated by ESR at 78 K with an X-band spectrometer and a TE_{102} cavity with 100 kc field modulation. The crystals were preferably measured with the directions $\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$ parallel to the static magnetic field H_0 . The ESR spectrum of Mn-doped crystals showed a sextet which can be explained by a spin-Hamiltonian for an electron spin $S = 1/2$ in interaction with the nuclear spin $I = 5/2$ of the Mn nucleus for axial symmetry. Due to the observed spin and due to the orientation of the paramagnetic centers the spectra were assigned to Mn^{2+} in the low spin state which resides on cation site in the FeS_2 lattice. In halogen-doped crystals four pairs of lines can be interpreted by the interaction of the two isotopes of $I = 3/2$, ^{79}Br , ^{81}Br and ^{35}Cl , ^{37}Cl , respectively, with an electron spin $S = 1/2$. According to the observed symmetry of the ESR signals the paramagnetic centers can be explained as $(S-X)^{2-}$ radicals ($X = Cl, Br$) which substitute for the $(S_2)^{2-}$ dumb-bells of pyrite. All crystals evoked extremely narrow ESR lines, especially the halogen-doped crystals with linewidths down to 0.03 mT. Excellent agreement between measured and calculated spectra up to the finest details has been obtained.

Key words: Pyrite, ESR, anorganic radicals, hyperfine coupling, spin densities.

1. Introduction

Recently pyrite has attracted great interest due to its photoactive properties that seem to make the material suitable for photoelectrochemical and photovoltaic solar cells [1, 2]. In natural samples the high impurity concentration disturbs these properties, so that synthetic material has to be applied. The remaining impurities strongly influence the photoactive behaviour, and therefore it is desirable to know the nature of these impurities. If they are paramagnetic, electron spin resonance (ESR) often can be applied with great success.

In spite of the fact that pyrite is one of the best known minerals, there are very few ESR investigations with FeS_2 as a host material. In natural crystals the impurity conductivity is mostly too high for ESR measurements, also at low temperatures. Srinivasan et al. [3] reported for the first time ESR spectra of Mn^{2+} in natural pyrite polycrystals using a TE_{101} cavity with a variable Gordon coupler to overcome the problems of the considerable dielectric losses. They observed only one hyperfine sextet, but interpreted their results

by the usual assumption of a $^6S_{5/2}$ ground state for Mn^{2+} , where five hyperfine sextets are to be expected for a single crystal. Chandler and Bené [4] investigated solid solutions of $Ni_xFe_{1-x}S_2$, $Co_xFe_{1-x}S_2$, and $Co_xNi_yFe_{1-x-y}S_2$ in the range $0.0004 < x < 0.03$. They used small synthetic crystals, around 1 mg in weight, to prevent cavity loading. This paper reports on an ESR study of larger synthetic single crystals of pyrite enabling us to evaluate the structure of three different paramagnetic centers.

2. The Crystals

The Mn-doped crystals were obtained from a Te melt, often as platelets or needles with $\{100\}$ and $\{110\}$ faces parallel to the crystal prism. The growth technique is described in [5]. The crystals were mounted on a suitable inclined plane surface of a quartz rod by vacuum grease. In this manner the important orientations for the static magnetic field H_0 could be obtained. The most perfect crystals of several mm in size were grown by a halogen-transport technique described elsewhere [6], using Cl and Br as transport agent, furthermore Cl as a mineralizer for the synthesis from the elements. The polyhedral crystals had ex-

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cellent growth faces, $\{100\}$, $\{111\}$, $\{210\}$, and $\{112\}$, which could be used for crystal orientation by an optical two-circle reflection goniometer. They were glued on a quartz rod with UHU-plus, so that a $\langle 110 \rangle$ direction was parallel to the rod, which entered the cavity perpendicular to H_0 . By rotating the rod the most important directions $\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$ could be orientated parallel to H_0 .

The crystal structure of pyrite is well known. It can be considered as an NaCl structure where the anions are substituted by $(S_2)^{2-}$ dumb-bells with local $\bar{3}$ axes. The space group is $P2_1/a\bar{3}$. The cations' positions together with the centres of the S_2 dumb-bells have the local symmetry $\bar{3}$. All these $\bar{3}$ axes are oriented towards the four different $\langle 111 \rangle$ directions, alternating arranged in a regular manner.

3. ESR Spectra and Analysis

3.1. Experimental

The ESR measurements were performed at 78 K with a conventional Varian X-band spectrometer and a standard TE_{102} cavity with 100 kc field modulation. At room temperature the cavity loading was too high for the crystal used, but between 78 K and 90 K the resonance dip indicated very small cavity losses, a hint at the temperature dependence of the dark conductivity. The microwave frequency was measured with a frequency counter, the magnetic field by a Bruker Hall

Table 1. Classification of $\langle 111 \rangle$ -oriented paramagnetic centers for three important orientations of the static magnetic field H_0 with respect to the crystal axes. N = Number of magnetically equivalent centers.

Direction of H_0	Angle θ	N
$\langle 100 \rangle$	54.7°	4
$\langle 110 \rangle$	35.3°	2
	90.0°	2
$\langle 111 \rangle$	0.0°	1
	70.5°	3

effect magnetometer, the reading of it was corrected using DPPH.

For a general direction of the magnetic field we observed 24 lines for the Mn-doped crystals and more than fifty lines for the halogen-transported crystals. These numbers were considerably reduced for the $\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$ orientations, indicating that for these directions crystallographically equivalent centers now become also magnetically equivalent. The remaining numbers of lines and their splitting behaviour, if the magnetic field deviates somewhat from these directions, lead us to conclude that there were axial centers, directed to the four different $\langle 111 \rangle$ axes. For the special directions mentioned above, the angles θ between the center axes and H_0 are given in Table 1 together with the numbers of magnetically equivalent centers.

3.2. Analysis of the Spectra

The ESR parameters were obtained from the spectra by a computer fitting procedure that compared experimental and calculated magnetic fields at resonance for an assumed set of ESR parameters. The latter resonance fields were calculated by means of exact numerical diagonalization of the spin-Hamiltonian matrices. For each transition possible in principle, the quantum mechanical transition probability M_{ij} was calculated with the eigenstates $|i\rangle$ and $|j\rangle$ from the diagonalization procedure according to

$$M_{ij} = |\langle i | \mathcal{H}_1 / \beta H_1 | j \rangle|^2 \quad (1)$$

with

$$\begin{aligned} (\mathcal{H}_1 / \beta H_1) = & (\cos \theta \cos \phi \cos \chi - \sin \phi \sin \chi) g_x S_x \\ & + (\cos \theta \sin \phi \cos \chi + \cos \phi \sin \chi) g_y S_y \\ & - \sin \theta \cos \chi g_z S_z. \end{aligned} \quad (2)$$

Herein $\mathcal{H}_1$ denotes the Zeeman operator due to the magnetic field H_1 of the microwave, the latter with components, expressed by the polar angles θ and ϕ of the static magnetic field H_0 and the third Eulerian

Table 2. ESR parameters, g_N and Q from [14]; energies in 10^{-4} cm^{-1} , Q in multiples of $|e| \times 10^{-24} \text{ cm}^2$; accuracy for the g values: 10^{-4} , accuracy for the energy parameters: $0.5 \times 10^{-4} \text{ cm}^{-1}$; ^u means polarization correction not made.

	$g_{\parallel}$	$g_{\perp}$	$A_{\parallel}$	$A_{\perp}$	P	A_0	$T_{\parallel}$	g_N	Q
$Mn^{2+} (S = 1/2)$	2.0377	2.1490	-8.7	75.1	-	47.2	-55.9	1.3819	0.33 ^u
$(S^{79}Br)^{2-}$	2.0344	2.0996	101.6	12.9	-8.3	42.4	59.1	1.404266	0.293 ^u
$(S^{81}Br)^{2-}$	2.0344	2.0996	109.6	13.6	-7.0	45.6	63.9	1.513706	0.27
$(S^{35}Cl)^{2-}$	2.0322	2.0839	14.8	2.4	2.0	6.5	8.3	0.547916	-0.08249
$(S^{37}Cl)^{2-}$	2.0322	2.0839	12.3	1.9	1.5	5.4	6.9	0.456082	-0.06493

Fig. 1. Experimental and theoretical spectrum for $\text{FeS}_2:\text{Mn}^{2+}$ in the low spin state for $H_0 \parallel \langle 111 \rangle$; * denotes an unidentified signal.

Fig. 2. Angular dependence for $\text{FeS}_2:\text{Mn}^{2+}$, — calculated, $\circ\circ\circ$ measured values.

angle χ that determines the direction of H_1 . The reference frame is given by the principal axes of the g tensor.

3.3. Mn-doped Crystals

The ESR spectrum of an Mn-doped crystal is shown in Fig. 1 for $H_0 \parallel \langle 111 \rangle$. Corresponding to Table 1, there is a sextet for $\theta = 0^\circ$ and another one for $\theta = 70.5^\circ$ with threefold intensity. The surplus line in-

dicated in Fig. 1 belongs to an other still unknown impurity, as could be proved by its different temperature dependence. As there were no further side sextets we tried to analyze the spectrum by the following spin-Hamiltonian appropriate for an electron spin $S = 1/2$ in interaction with the nuclear spin $I = 5/2$ of the Mn nucleus for axial symmetry:

$$\begin{aligned} \mathcal{H} = & g_{\parallel} \beta H_z S_z + (1/2) g_{\perp} \beta (H_+ S_- + H_- S_+) \\ & + A_{\parallel} S_z I_z + (1/2) A_{\perp} (S_+ I_- + S_- I_+) \\ & + P(I_z^2 - 35/12). \end{aligned} \quad (3)$$

The matrix representation within the states $|S, M; I, m\rangle = |1/2, M; 5/2, m\rangle$ (12×12 matrix) is given in Table 4 (Appendix). As we observed only allowed transitions with $\Delta m = 0$, the nuclear Zeeman operator had not to be included. The final ESR parameters are summarized in Table 2. From the fitting procedure a value of about -10^{-4} cm^{-1} was obtained for P , but this value is not very significant and therefore not included in Table 2. It is, however, of the right order of magnitude, the corresponding nuclear quadrupole operator had very little influence on the magnetic fields at resonance. The theoretical stick diagram is also shown in Fig. 1 for $H_0 \parallel \langle 111 \rangle$, and the angular dependence in Figure 2. It was not possible to reproduce this angular dependence for a middle sextet of a presumptive $S = 5/2$ spin system. The good agreement of the calculated fields at resonance with the experimental values is a proof that the assumption of an $S = 1/2$ spin system was right.

3.4. Halogen Transported Crystals

In the halogen transported crystals the ESR lines were extremely narrow, about 0.03 mT in width. Thus

Fig. 3. Experimental and theoretical spectrum for $\text{FeS}_2\text{:Br,Cl}$ with $H_0 \parallel \langle 100 \rangle$; upper stick diagram for $\text{FeS}_2\text{:Cl}$, lower stick diagram for $\text{FeS}_2\text{:Br}$; dotted sticks: forbidden transitions with $\Delta m \neq 0$.

Fig. 4. Experimental and theoretical spectrum for $\text{FeS}_2\text{:Br,Cl}$ with $H_0 \parallel \langle 111 \rangle$; upper stick diagram for $\text{FeS}_2\text{:Cl}$, lower stick diagram for $\text{FeS}_2\text{:Br}$; dotted sticks: forbidden transitions with $\Delta m \neq 0$; * denotes an unidentified signal.

Table 3. Hyperfine coupling constants and spin densities.

	A_0^*/MHz	$T_{ }^*/\text{MHz}$	ϱ_s	ϱ_p
(S ^{79}Br) $^{2-}$	20 672	1095	0.006	0.162
(S ^{35}Cl) $^{2-}$	4 433	241	0.004	0.103
(O ^{19}F) $^{2-}$	—	—	0.02	0.21

their splitting behaviour could be easily observed and the crystals could be very exactly (within 0.1 degree of angle) adjusted for the special directions of H_0 parallel to $\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$.

The ESR spectrum of a Br-transported crystal is shown in Fig. 3 for $H_0 \parallel \langle 100 \rangle$ and in Fig. 4 for $H_0 \parallel \langle 111 \rangle$. In Fig. 3 four pairs of strong lines have nearly the same intensity. If one bears in mind that there are two Br isotopes of $I = 3/2$ with nearly the same natural abundance and similar magnetic moments, the strong lines can be explained by $S = 1/2$ in interaction with the two isotopes of $I = 3/2$, ^{79}Br and ^{81}Br . In the middle part of the experimental spectrum of Fig. 4 one observes a similar situation, but now one line of each pair is considerably smaller than the other. The intensity ratio is about 3:1 and corresponds fairly well to the natural abundance of the two Cl isotopes, ^{35}Cl and ^{37}Cl , that have $I = 3/2$ too and the abundance ratio 3.01:1. Therefore the spectra had to be described by four spin-Hamiltonians for the different paramagnetic centers with the ^{79}Br , ^{81}Br , ^{35}Cl , and ^{37}Cl isotopes. For the halogen-transported crystals we observed also forbidden lines with $\Delta m \neq 0$, and therefore the nuclear Zeeman operator had to be included. So we analyzed the different line systems with the following spin-Hamiltonian for $S = 1/2$ and $I = 3/2$ in axial symmetry:

$$\begin{aligned} \mathcal{H} = & g_{||} \beta H_z S_z + (1/2) g_{\perp} \beta (H_+ S_- + H_- S_+) \\ & + A_{||} S_z I_z + (1/2) A_{\perp} (S_+ I_- + S_- I_+) \\ & + P(I_z^2 - 5/4) - g_N \beta_N H_z I_z - (1/2) \\ & \cdot g_N \beta_N (H_+ I_- + H_- I_+). \end{aligned} \quad (4)$$

The corresponding matrix representation within the states $|S, M; I, m\rangle = |1/2, M; 3/2, m\rangle$ is given in Table 5 (8×8 matrix). From the fitting procedure the final ESR parameters are listed in Table 2. Because of the high precision of the experimental line positions and the greater number of lines that were fitted, the parameter P is now significant. To demonstrate the agreement between the experimental and calculated ESR lines, the relative heights of the single sticks of the stick

diagrams were also calculated and plotted according to (1) and (2) with consideration of the numbers of equivalent centers from Table 1 and the natural abundance of the isotopes. There is excellent agreement between the measured and calculated spectra up to the finest details of forbidden transitions for the three field directions H_0 parallel to $\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$. This agreement surpasses the accuracy of the plots in Figs. 3 and 4.

4. Discussion

A noteworthy characteristic of our spectra is the small linewidth of the observed signals down to 0.03 mT for the halogen transported crystals. Similar linewidths were observed for Mn^{2+} in ZnS (0.04 mT for a line of the middle sextet [7]). A necessary condition for these narrow lines is the absence of nuclear spins of the ions of the host lattice. Apart from this, the crystals must be well ordered and free from internal strains. Viceversa, the extremely narrow signals indicate good crystallinity. We were thus able to determine all the ESR parameters of the Hamiltonian (4).

4.1. $\text{FeS}_2\text{:Mn}$

Due to the observed spins $S = 1/2$ and $I = 5/2$ and due to the orientation of the paramagnetic centers, we assign the spectrum of Fig. 1 to Mn^{2+} in the low-spin state on cation sites in FeS_2 . This is in contradiction to Srinivasan *et al.* [3], who assumed the high-spin configuration but could not determine the angular dependence of Fig. 2 because of the polycrystalline structure of their samples. It is well known that in pyrite Fe^{2+} is in the low-spin state too [8], and this is apparently transferred to Mn^{2+} . We emphasize this result because in inorganic materials the low-spin configuration is very unusual for Mn^{2+} . For example, in the mineral hauerite (MnS_2), which also crystallizes in the pyrite structure, Mn^{2+} occurs exclusively in the high spin state [9, 10]. After Tanabe and Sugano [11] the low-spin configuration in octahedral symmetry is expected if the crystal field splitting $\Delta = 10 \text{ Dq}$ surpasses $2B(\text{Fe}^{2+})$ and $2.8B(\text{Mn}^{2+})$, respectively. (B is the Racah parameter for the corresponding ion.) The latter expression will always be greater than the first one. If one assumes that Δ does not change very much on substitution of Fe^{2+} by Mn^{2+} , one can argue that Δ is at least $2.8B(\text{Mn}^{2+})$ for Fe^{2+} in pyrite.

The hyperfine interaction tensor $\mathbf{A}$ is decomposed, as usually, in an isotropic part $\mathbf{A}_0$ with the principal value A_0 and a traceless tensor $\mathbf{T}$ with the principal values $T_{||}$ and $T_{\perp}$, whereby $T_{||} = -2 T_{\perp} \cdot A_0$ and $T_{||}$ are included in Table 2.

As we have proved that the Mn^{2+} center has definitely $S = 1/2$, we tried to understand the anisotropy of the hyperfine interaction in a simple one electron picture for the unpaired electron. Due to the trigonal distortion, the three t_{2g} states of Mn^{2+} in the octahedral complex $\text{Mn}^{2+}(\text{S}_2^{2-})_6$ are further split into one low-lying single level $|t_0\rangle$ and two degenerate higher states $|t^+\rangle$ and $|t^-\rangle$. The new orbitals can be expressed by the five normalized d functions $|0\rangle$, $|\pm 1\rangle$, $|\pm 2\rangle$, related to the trigonal axis as a new axis of quantization [12]:

$$\begin{aligned} |t^+\rangle &= (1/3)^{1/2} |1\rangle + (2/3)^{1/2} |-2\rangle, \\ |t^-\rangle &= (1/3)^{1/2} |-1\rangle - (2/3)^{1/2} |2\rangle, \\ |t_0\rangle &= |0\rangle. \end{aligned}$$

In the low-spin configuration of Mn^{2+} these levels are thought to be filled up with the five d electrons so that there remains one unpaired electron of the type $|t^+\rangle$, $|t^-\rangle$. As $|t^+\rangle^* = -|t^-\rangle$, both orbitals have the same charge distribution and therefore give rise to the same anisotropic hyperfine splitting. With regard to the trigonal axis we have for the anisotropic hyperfine splitting according to [12]:

$$\begin{aligned} T_{||} &= g\beta g_N \beta_N \langle (3z^2 - r^2)/r^5 \rangle \\ &= g\beta g_N \beta_N \langle 4(\pi/5)^{1/2} Y_2^0/r^3 \rangle. \end{aligned}$$

Here the brackets denote an average over the whole spatial distribution of the unpaired spin. As the d orbitals can also be expressed by the spherical harmonics Y_n^m , it is easy to calculate the mean values through well-known tables for integration. If one uses $|t^+\rangle$ or $|t^-\rangle$ for the unpaired spin, the result is $-(2/7)\langle r^{-3} \rangle$. With the factor $g\beta g_N \beta_N$ and $\langle r^{-3} \rangle$ after [13] we get -160 MHz for $T_{||}$, in excellent agreement with the measured value of -167 MHz corresponding to 0.00559 cm^{-1} from Table 2. The isotropic part A_0 may be explained by a very small admixture of s states. A pure $4s$ electron centred on Mn^{2+} would produce an isotropic HF constant of 4731 MHz [13] compared to only 141.5 MHz from Table 2.

A calculation of the principal g values requires a more sophisticated procedure including the orbitals of the ligands too. This is not the aim of this paper.

4.2. The radicals $(\text{SBr})^{2-}$ and $(\text{SCl})^{2-}$

According to the interaction of an electron spin $S = 1/2$ with a single nuclear spin $I = 3/2$, and due to the observed symmetry of the ESR signals we assumed two chemically different paramagnetic centers in interaction with a single Br and Cl, respectively. This is confirmed by the splitting according to natural abundances of the involved halogen isotopes. The ratio of the HF constants for each pair equals the ratio of the nuclear magnetic moments, i.e. the ratio of the g_N values. According to Table 2 we have $A_{||}({}^{81}\text{Br})/A_{||}({}^{79}\text{Br}) = 1.079$, in excellent agreement with $g_N({}^{81}\text{Br})/g_N({}^{79}\text{Br}) = 1.078$ and $A_{||}({}^{35}\text{Cl})/A_{||}({}^{37}\text{Cl}) = 1.203$ compared to $g_N({}^{35}\text{Cl})/g_N({}^{37}\text{Cl}) = 1.201$. The centers turned out to be axial, $\langle 111 \rangle$ -oriented. An assumed single halogen ion would require an unpaired s -electron because of its spin $1/2$. But such an s orbital could not produce the large anisotropy of the hyperfine interaction. Therefore we assigned the observed signals to diatomic radicals, $(\text{SBr})^{2-}$ and $(\text{SCl})^{2-}$, respectively. These molecules substitute for the $(\text{S}_2)^{2-}$ dumb-bells, lowering the local symmetry from $\bar{3}$ to 3 that cannot be distinguished by ESR.

Rius *et al.* [15] observed the similar molecular ion $(\text{OF})^{2-}$ in MgO , and we will follow their discussion to some extent. For the unpaired electron the following linear combination of atomic s and p orbitals centred on halogen and sulphur may be adopted:

$$\begin{aligned} \psi &= a_{\text{Br}} 4s(\text{Br}) + b_{\text{Br}} 4p_z(\text{Br}) - a_s 3s(\text{S}) \\ &\quad + b_s 3p_z(\text{S}) \quad \text{for} \quad (\text{SBr})^{2-}, \\ \psi &= a_{\text{Cl}} 3s(\text{Cl}) + b_{\text{Cl}} 3p_z(\text{Cl}) - a'_s 3s(\text{S}) \\ &\quad + b'_s 3p_z(\text{S}) \quad \text{for} \quad (\text{SCl})^{2-}, \end{aligned}$$

The coefficients a_X ($X = \text{Br}, \text{Cl}$) determine the isotropic hyperfine interaction with the halogen nucleus in essential, b_X the anisotropic part. The corresponding spin densities ϱ for the s and p contributions follow from

$$\begin{aligned} \varrho_s(X) &= |a_X|^2 = A_0(X)/A_0^*(X), \\ \varrho_p(X) &= |b_X|^2 = T_{||}(X)/T_{||}^*(X). \end{aligned}$$

The values with an asterisc mean the hyperfine coupling constants of a corresponding electron that would be fully localized on the X^- ion. These coupling constants from [13] are given in Table 3 together with the calculated spin densities. For comparison we have included the results for $(\text{OF})^{2-}$ in MgO from [15]. It is obvious from this Table that the unpaired electron

of the $(\text{SX})^{2-}$ molecular ion in FeS_2 is mainly localized on the chalcogen site, and that for a larger extend than for $(\text{OF})^{2-}$ in MgO .

Therefore we may indicate the electronic structures of the sulphur radicals as S^-Br^- and S^-Cl^- , respectively. This is very reasonable due to the tendency of halogens to form inert gas configurations. In consequence, the overall spread of our ESR spectra is considerably smaller than that of the similar spectra due to the well known FBr^- and FCl^- centers in alkali halides [16], i.e. 0.03 T for S^-Br^- compared to 0.25 T for FBr^- in KCl. The spreads for the chlorine centers are smaller mainly because of the smaller g_N value.

4.3. Nuclear Quadrupole Interaction

The quadrupole coupling constant P is proportional to the electric quadrupole moment Q of the nucleus and to the electric field gradient V_{zz} . As the latter is identical for isotopes of the same element there should be a proportionality between P and Q for these isotopes. We have from Table 2 $P(^{79}\text{Br})/P(^{81}\text{Br}) = 1.19$ whereas the corresponding ratio for the moments Q is 1.09, furthermore $P(^{35}\text{Cl})/P(^{37}\text{Cl}) = 1.33$ compared to the moment ratio of 1.27. The corresponding ratios are equal within the experimental errors. In addition, Table 2 indicates a proportionality between P and Q for Br and Cl, and that means that V_{zz} is about the same for these elements. V_{zz} is the sum of a lattice contribution and an orbital contribution. As the former one will be identical for the different centers, the latter one will be either also the same for the Br and Cl centers, or it will be of unimportant magnitude compared to the lattice contribution.

Table 4. Matrix representation for $S = 1/2$ and $I = 5/2$ with consideration of hyperfine interaction and nuclear quadrupole interaction; column I contains the matrix elements of the diagonal, column II the elements of the 5th upper parallel, column III the elements of the 6th upper parallel. All the other matrix elements of the upper half are zero.

I	II	III
$b_{\parallel} n + (5/4) A_{\parallel} + (10/3) P$	0	$b_{\perp} n_{-}$
$b_{\parallel} n + (3/4) A_{\parallel} - (2/3) P$	$(1/2) \sqrt{5} A_{\perp}$	$b_{\perp} n_{-}$
$b_{\parallel} n + (1/4) A_{\parallel} - (8/3) P$	$(3/2) A_{\perp}$	$b_{\perp} n_{-}$
$b_{\parallel} n - (1/4) A_{\parallel} - (8/3) P$	$(3/2) A_{\perp}$	$b_{\perp} n_{-}$
$b_{\parallel} n - (3/4) A_{\parallel} - (2/3) P$	$(1/2) \sqrt{5} A_{\perp}$	$b_{\perp} n_{-}$
$b_{\parallel} n - (5/4) A_{\parallel} + (10/3) P$	$(1/2) \sqrt{5} A_{\perp}$	$b_{\perp} n_{-}$
$-b_{\parallel} n - (5/4) A_{\parallel} + (10/3) P$	0	
$-b_{\parallel} n - (3/4) A_{\parallel} - (2/3) P$		
$-b_{\parallel} n - (1/4) A_{\parallel} - (8/3) P$		
$-b_{\parallel} n + (1/4) A_{\parallel} - (8/3) P$		
$-b_{\parallel} n + (3/4) A_{\parallel} - (2/3) P$		
$-b_{\parallel} n + (5/4) A_{\parallel} + (10/3) P$		

Table 5. Matrix representation for $S = 1/2$ and $I = 3/2$ with consideration of hyperfine interaction, nuclear quadrupole interaction and nuclear Zeeman operator.

m	$M = -1/2$					
	$3/2$	$1/2$	$-1/2$	$-3/2$	$3/2$	$-3/2$
$n(b_{\parallel} - 3b_N) + (3/4) A_{\parallel} + P$	$n(b_{\parallel} - 3b_N) + (3/4) A_{\parallel} + P$	$-\sqrt{3} n_{-} b_N$	0	0	$n_{-} b_{\perp}$	0
$-\sqrt{3} n_{+} b_N$	0	$n(b_{\parallel} - b_N) + (1/4) A_{\parallel} - P$	$-2 n_{-} b_N$	0	$(1/2) \sqrt{3} A_{\perp}$	0
0	0	$n(b_{\parallel} + b_N) - (1/4) A_{\parallel} - P$	$n(b_{\parallel} + b_N) - (3/4) A_{\parallel} + P$	$-\sqrt{3} n_{-} b_N$	0	$n_{-} b_{\perp}$
0	0	$-\sqrt{3} n_{+} b_N$	0	0	$(1/2) \sqrt{3} A_{\perp}$	0
$n_{+} b_{\perp}$	$n_{+} b_{\perp}$	0	0	$-\sqrt{3} n_{-} b_N$	0	0
0	0	$A_{\perp}$	0	0	$n(-b_{\parallel} - b_N) - (1/4) A_{\parallel} - P$	0
0	0	$n_{+} b_{\perp}$	$(1/2) \sqrt{3} A_{\perp}$	0	$n(-b_{\parallel} + b_N) + (1/4) A_{\parallel} - P$	$-\sqrt{3} n_{-} b_N$
0	0	0	$n_{+} b_{\perp}$	$(1/2) \sqrt{3} A_{\perp}$	$-\sqrt{3} n_{+} b_N$	$n(-b_{\parallel} + 3b_N) + (3/4) A_{\parallel} + P$

4.4. Closing Remarks

In all pyrite samples, natural [17] and synthetic [2], studied so far by photo-electrochemical methods, n-type conductivity was found and often connected with the sulfur deficit of these samples. Our $(S-X)^{2-}$ defects cannot account for such relatively great sulfur deficits (in the percent region, e.g. $FeS_{1.94}$ [18]) as their concentration is at least one order of magnitude smaller (e.g. 350 ppm bromine [6]). The hypothesis that S^{2-} ions replace $(S_2)^{2-}$ molecules cannot be investigated by ESR directly because S^{2-} is diamagnetic. Therefore this hypothesis has to be taken into account furtheron. As for the conductivity, we assume that the $(S-X)^{2-}$ defects act as donors and that this effect becomes more and more important as the other defects, which are responsible for the greater sulfur deficits, diminish.

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Appendix

For the matrix representations of the Hamiltonians (3) and (4) in Tables 4 and 5 the following abbreviations were used:

$$\begin{aligned} b_{\parallel} &= (1/2) g_{\parallel} \beta H_0, & b_{\perp} &= (1/2) g_{\perp} \beta H_0, \\ b_N &= (1/2) g_N \beta_N H_0, \\ n_{\pm} &= l \pm im; & l, m, n, &\text{are direction cosines,} \end{aligned}$$

which determine the direction of the static magnetic field H_0 .

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