Crystal and Magnetic Structures of NaMnF₄

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An X-ray single crystal structure determination (monoclinic, space group $P2_1/c$, $a = 573.6(2)$, $b = 489.2(1)$, $c = 574.8(2)$ pm, $\beta = 108.07(2)^\circ$, $Z = 2$; $wR = 0.038$ for 380 reflections) shows that NaMnF₄ crystallizes in the same layered structure type as LiMnF₄. In the quadratic layers the Mn–F–Mn bridges are strongly asymmetric, due to the Jahn-Teller effect, leading to an antiferrodistortive order of elongated octahedra. The bridging angle is 138.4° . The Na⁺ ions are 6-coordinated as well. The common structural arrangement of both [MnF₆] and [NaF₆] octahedra shows topological relation to the rutile structure. In the magnetic measurements performed on powder samples NaMnF₄ behaves as an antiferromagnet with a weak ferromagnetic component below 13 K. By neutron diffraction on powder (4–70 K) a magnetic cell doubled along the a -axis is found and below a Neel temperature of $T_N = 13$ K the magnetic structure shows colinear antiferromagnetic arrangement of the spins pointing slightly (16°) out of the layer plane. The resulting magnetic moment is $3.52 \mu_B$.

Introduction

AMnF₄ compounds (A = K, Rb, Cs, Tl, NH₄) have layered structures deriving from the TlAlF₄ type as shown by several single crystal X-ray investigations of the Cs [1, 2], Tl [3], and K [4] compounds, and by powder diffraction work [5]. Owing to the strong Jahn-Teller effect of the d⁴ high spin configuration of octahedrally coordinated Mn³⁺, the [MnF₆] groups show antiferrodistortive ordering of their elongated axes within the quadratic layers. According to the rules for σ -superexchange, ferromagnetism has been found for CsMnF₄ [1]. By magnetic investigations on the Rb, NH₄ and K [6] and the Tl [3] compounds it has been shown that for smaller cations and, in consequence, for smaller Mn–F–Mn bridge angles, a transition to antiferromagnetic behaviour occurs. Within the scope of investigations on low-dimensional magnets we have been interested in the AMnF₄ compound with the next smaller alkali cation and are presenting here the results of an X-ray single crystal structure determination, and

of magnetic and neutron diffraction measurements on NaMnF₄. For this compound only thermodynamic data had been published until now [7–9].

Experimental

Single crystals of NaMnF₄ were obtained by reaction of NaF and MnF₃ in a sealed platinum tube. The stoichiometric mixture was first heated at 800 °C for 45 h, slowly cooled to 650 °C, and then cooled down faster to room temperature. A transparent brown platelet of about $0.175 \times 0.150 \times 0.025$ mm was used for X-ray film exposures on a precession camera and for intensity measurements on a 4-circle diffractometer (CAD4, Enraf-Nonius). The space group was found to be $P2_1/c$ from the systematic absences $h0l: l = 2n+1, 0k0: k = 2n+1$, with $Z = 2$ as in the case of LiMnF₄ [10]. The monoclinic lattice constants were refined with 25 high-angle reflections to $a = 573.6(2)$ pm, $b = 489.2(1)$ pm, $c = 574.8(2)$ pm, $\beta = 108.07(2)^\circ$ giving $d_c = 3.334 \text{ g cm}^{-3}$.

The 455 reflections (θ : 2–30°; h : –8–+8; k : 0–6; l : 0–8) were collected in ω -scan mode using graphite monochromated MoK α -radiation. After elimination of unobserved ($F_o < 3\sigma$) and averaging of symmetry equivalent reflections, 380 F_o data remained for the refinement of the structure.

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No absorption correction has been applied ($\mu = 41.51 \text{ cm}^{-1}$). The calculations were made with the SHELX-76 program system [11]. The structure was refined starting from the atomic parameters of LiMnF₄ [10] in the space group $P2_1/c$ with anisotropic temperature factors to $R = 0.0394$ and $wR = 0.0383$ (weights $w = 1/\sigma^2(F_o)$) using scattering factors for ions [12]. An anomalous dispersion correction [13] was included and an empirical extinction parameter $\varepsilon = 5 \cdot 10^{-7}$ was refined, based on the relation $F_c(\text{corr}) = F_c(1 - \varepsilon F_c^2/\sin\theta)$. The resulting atomic parameters are compiled in Table I*.

Besides, powder samples of NaMnF₄ were prepared for magnetic measurements *via* the reaction $2\text{NaF} + \text{Mn}_2\text{O}_3$, both dissolved in 40% HF, and let to evaporate. Those measurements have been carried out using both a vibrating sample magnetometer (Foner) and a Faraday microbalance, in a temperature range from 4.2 to 300 K.

Neutron diffraction studies have been performed on the same powder, using the D1B diffractometer at the Institute Laue Langevin in Grenoble. The incident wavelength was 252.4 pm. The sample was loaded in a vanadium container and the patterns were recorded in the $6\text{--}86^\circ 2\theta$ range for the 4–70 K temperature range. The crystallographic and magnetic structures were refined using the Rietveld profile technique with Young's program [14]. The magnetic form factor of the manganese atoms was tabulated from the values of P. J. Brown [15].

* Listings of the structure factors are available from Fachinformationszentrum Karlsruhe, Gesellschaft für wissenschaftlich-technische Information mbH, D-7514 Eggenstein-Leopoldshafen 2, F.R.G., under specification of deposit No. CSD 55851, authors and journal reference.

Results and Discussion of the X-Ray Structure Determination

NaMnF₄ belongs to the wide group of compounds with structures related to the TiAlF_4 type. The $[\text{MnF}_6]$ octahedra form quadratic layers parallel to the (100) plane by sharing four corners (Fig. 1). Those $[\text{MnF}_4]$ layers are separated by layers of 6-coordinated Na cations (Fig. 4). The topology of interconnection of both kinds of octahedral groups corresponds to that of the rutile structure, as was pointed out for the isostructural LiMnF₄ [10] and LiCoF₄ [17] compounds by Hoppe, Ferey and coworkers.

The Mn^{3+} Jahn-Teller ion induces a strong elongation of the $[\text{MnF}_6]$ octahedra (long Mn–F 216.7(3) pm), and it is noticeable that this effect is more pronounced in the present case than in any other compound of the AMnF_4 (A = alkali metal) series (Tables II, III). The long axes are antiferro-

Fig. 1. ORTEP [16] drawing of the $[\text{MnF}_4]$ layer in NaMnF₄. Thermal ellipsoids at the 50% probability level.

Table I. Atomic fractional coordinates and temperature factors [10^{-20} m^2] for NaMnF₄, $T = \exp[-2\pi^2(U_{11}h^2a^{*2} + \dots + 2U_{12}hk a^*b^*)]$.

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>U</i> ₁₁	<i>U</i> ₂₂	<i>U</i> ₃₃	<i>U</i> ₂₃	<i>U</i> ₁₃	<i>U</i> ₁₂
Na	1/2	1/2	0	0.0193(14)	0.0196(15)	0.0126(12)	−0.0023(16)	−0.0004(10)	0.0063(1)
Mn	0	1/2	1/2	0.0120(5)	0.0089(5)	0.0043(4)	−0.0013(5)	0.0026(3)	−0.0005(6)
F 1	0.8757(6)	0.7633(6)	0.6655(5)	0.0235(17)	0.0157(15)	0.0123(14)	−0.0055(12)	0.0061(12)	0.0040(1)
F 2	0.3014(5)	0.6529(6)	0.6101(5)	0.0168(16)	0.0182(17)	0.0108(13)	0.0007(12)	0.0031(11)	−0.0064(1)

Table II. Characteristic bond lengths (pm) and angles (°) in NaMnF₄.

Mn ³⁺ octahedron			
Mn–F 1 ^{a,b}	2 × 186.9(3)	F 1 ^a –Mn–F 1 ^c	89.4(1)
Mn–F 2, F 2 ^c	2 × 180.8(3)	F 1 ^a –Mn–F 1 ^d	90.6(1)
Mn–F 1 ^{d,e}	2 × 216.7(3)	F 1 ^c –Mn–F 2 ^c	96.0(1)
<Mn–F>	194.8	F 1 ^c –Mn–F 2	84.0(1)
		F 1 ^b –Mn–F 2	89.4(1)
		F 1 ^b –Mn–F 2 ^c	90.6(1)
Na ⁺ octahedron			
Na–F 1 ^{f,g}	2 × 237.0(3)	F 1 ^f –Na–F 2 ^h	110.2(1)
Na–F 2 ^{f,g}	2 × 224.2(3)	F 1 ^g –Na–F 2 ^f	90.3(1)
Na–F 2 ^{b,h}	2 × 230.1(3)	F 1 ^g –Na–F 2 ^h	69.8(1)
<Na–F>	230.4	F 1 ^g –Na–F 2 ^g	89.7(1)
		F 2 ^g –Na–F 2 ^h	96.5(1)
		F 2 ^f –Na–F 2 ^h	83.5(1)
Metal–metal distance and bridge angle			
Mn–Mn ⁱ	377.4(1)	Mn–F 1 ^b –Mn ⁱ	138.4(2)

Symmetry codes: ^a $x-1, y, z$; ^b $1-x, 1-y, 1-z$; ^c $-x, 1-y, 1-z$; ^d $x-1, 1.5-y, z-0.5$; ^e $1-x, y-0.5, 1.5-z$; ^f $x, 1.5-y, z-0.5$; ^g $1-x, y-0.5, 0.5-z$; ^h $x, y, z-1$; ⁱ $x, 0.5-y, z-0.5$.

distortively ordered within the layers. Thus, the distances in the two shorter axes are split into very short terminal bonds (180.8(3) pm) and medium short bonds (186.7(3) pm) taking part in the very asymmetric Mn–F–Mn bridges. A survey of the Mn–F–Mn bridging angles, important for the magnetic superexchange interactions, shows that the value found for NaMnF₄ is in good agreement

with a regular increase from LiMnF₄ to CsMnF₄ (Table III). Considering the puckering type of the layer, *i.e.* the distribution pattern of the bridging fluorine atoms above and below the manganese plane (Fig. 2), it is interesting to note that according to the alkali cation size, three different arrangements of those fluorine atoms are induced; they are either aligned (in LiMnF₄ and NaMnF₄), in a zigzag pattern (in KMnF₄ and RbMnF₄ [18]), or building squares (in CsMnF₄).

The coordination of the Na ions deviates from a regular octahedron not so much regarding the Na–F distances ranging from 234 to 237 pm, but rather the angles which vary between 69.8 and 110.2° for the “right” F–Na–F angles.

Magnetism

In the magnetic measurements below 15 K, a remanent magnetization was detected, and the variation of the magnetization M with H was roughly of the form:

$$M = M_0 + \chi H \tag{1}$$

The variation of the magnetization extrapolated to zero field (M₀) with T (Fig. 3a) led to a curve which does not fit well with a Brillouin function, especially in the transition temperature region. Taking the ordering temperature T_N = 13 K from the results of neutron diffraction (see below Fig 5), a probable curve for the three dimensional phase may be drawn (solid line). The flat spur above the

Fig. 2. Scheme of the three different puckering types in the AMnF₄ layered structures. a: A = Li, Na; b: A = K, Rb; c: A = Cs. The bridging F atoms are either above (+) or below (–) the plane of the Mn atoms.

Compound	Mn–F [pm] elongated	Mn–F [pm] bridge	terminal	Mn–F–Mn [°]	Ref.
LiMnF ₄	213.7	186.9	181.8	132.7	[10]
NaMnF ₄	216.7	186.9	180.8	138.4	this work
TlMnF ₄	215	186	178	146.5	[3]
RbMnF ₄	215.4	188.2	180.5	152.0	[18]
CsMnF ₄	216.2	186.0	182.1	161.9	[2, 18]

Table III. Comparison of geometric data for AMnF₄ compounds.

Fig. 3. a: Temperature dependence of zero field magnetization. The lines are guides for the eye (see text); b: Temperature dependence of the reciprocal molar susceptibility of NaMnF₄.

ordering point (dotted line) may be attributed to 2-dimensional magnetic phenomena. We are now investigating this interesting regime by means of Mössbauer spectroscopy on Fe doped samples.

The thermal variation of the susceptibility (Fig. 3b) gave $\theta_p = -19$ K, $C = 2.93$ and $\mu_{\text{eff}} =$

$4.84 \mu_B$, a value in good agreement with previous results on Mn³⁺. In that Figure, the values of χ have been directly taken from the microbalance results for $T > 15$ K and from eq. 1 below 15 K. The θ value corresponds to that of a bulk antiferromagnet and the origin ordinate value $M_0 = 0.16 \mu_B$ (Fig. 3a) is consistent with weak ferromagnetism due to slightly canted spins.

Fig. 4. Magnetic structure of NaMnF₄.

Neutron Diffraction

A neutron diffraction pattern was recorded at 70 K in the paramagnetic region. The refinement confirmed the structure found by X-ray single crystal analysis with slightly different parameters due to the temperature dependence (Table IV).

Several patterns have been recorded in the range 4–20 K in order to estimate the ordering temperature. The extrapolation of the intensity of the (110) reflection as shown in Fig. 5 leads to $T_N = 13 \pm 0.5$ K. In the 4 K pattern, additional reflections were observed and indexed with a propaga-

Fig. 5. Variation of the (110) magnetic reflection with temperature.

	70 K	4 K
a (Å)	5.755(2)	5.755(1)
b (Å)	4.892(1)	4.889(1)
c (Å)	5.760(2)	5.755(1)
β (°)	108.62(1)	108.67(1)
$x_F 1$	0.878(1)	
$y_F 1$	0.767(1)	
$z_F 1$	0.660(1)	
$x_F 2$	0.304(1)	
$y_F 2$	0.651(1)	
$z_F 2$	0.615(1)	

Table IV. Lattice parameters and fractional coordinates from the neutron diffraction data on NaMnF₄.

Table V. Observed and calculated intensities of magnetic reflections for NaMnF₄ at T = 4 K (m = multiplicity).

<i>h</i>	<i>k</i>	<i>l</i>	<i>m</i>	<i>I</i> _{obs.}	<i>I</i> _{calc.}
1	0	0	2	183	177
-1	0	1	2	457	486
1	1	0	4	3648	3575
1	0	1	2	507	368
-1	1	1	4	4	11
3	0	0	2	18	15
-3	0	1	2	844	661
1	1	1	4	8	13
3	1	0	4	1093	1142
-3	1	1	4	14	8
-1	0	2	2	37	7
3	0	1	2	188	299
-3	0	2	2	4	5
-1	1	2	4	221	177
1	0	2	2	7	6
3	1	1	4	8	7
-3	1	2	4	286	250
-5	0	1	2	303	237
-1	2	1	4	526	421
3	2	0	4	27	2
5	1	0	4	333	334

tion vector $Q = (1/2, 0, 0)$. Choosing the magnetic atoms in the magnetic cell as follows:

Mn1: 0, 0, 0

Mn2: 0, 1/2, 1/2

Mn3: 1/2, 0, 0

Mn4: 1/2, 1/2, 1/2

the magnetic intensities are in good agreement

with those calculated (Table V) assuming a colinear arrangement of the moments with:

along *x*, $A_x = M1_x - M2_x - M3_x + M4_x$ with a moment value $M_x = (1.0 \pm 1) \mu_B$

along *y*, $C_y = M1_y + M2_y - M3_y - M4_y$ with a moment value $M_y = (0.4 \pm 1) \mu_B$

along *z*, $A_z = M1_z - M2_z - M3_z + M4_z$ with a moment value $M_z = (3.70 \pm 5) \mu_B$

The reliability factor *R* is about 10%. The magnetic structure is shown in Fig. 4. The resultant magnetic moment $M = 3.52 \pm 5 \mu_B$ is close to the expected value for a *S* = 2 magnetic ion. The quality of the pattern did not allow either to determine or to exclude the small canting of spins suggested by the magnetization measurements. It is worthwhile to note that this magnetic structure differs from that of antiferromagnetic TlMnF₄ [3] not only by the offset of the spin direction out of the [MnF₄] layer, but mainly in the inter-layer coupling mode which is antiferromagnetic here, whereas it is ferromagnetic in the case of the Tl compound. In CsMnF₄ [1] both intra- and inter-layer couplings are ferromagnetic.

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