Huaixian Liu^a, Lin Sun^a, Huiliang Zhou, Peipei Cen, Xiaoyong Jin, Xiangyu Liu* and Qilin Hu

A mononuclear cobalt(III) 3-(2-pyridyl)-5-phenyl-1,2,4-triazolato complex: hydrothermal synthesis, crystal structure, thermostability, and DFT calculations

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Abstract: Starting with 1*H*-3-phenyl-5-(pyridin-2-yl)-1,2,4-triazole (1-Hppt), a Co(III) complex, $[Co(ppt)_3]$ (1), has been synthesized by reaction with CoF_3 under hydrothermal conditions and characterized by its infrared spectrum and elemental analysis. The structure was determined by single-crystal and powder X-ray diffraction. Density functional theory (DFT) was employed to determine the optimized geometry and preferred conformation of the free ligand. A supramolecular network is formed $via \pi - \pi$ stacking interactions. The conformation and geometry of the ligands correspond with the calculated results.

Keywords: 1*H*-3-phenyl-5-(pyridin-2-yl)-1,2,4-triazole; Co(III) complex; crystal structure; DFT calculation.

1 Introduction

In recent years, experimental and theoretical efforts have been extensively devoted to crystal engineering of coordination polymers (CPs) from predesigned bridging ligands and metal ions, because such hybrid materials display a variety of regulated architectures and thus many potential functions [1–5]. The interest in polymer architectures arises not only from their potential applications in luminescence, magnetism, sorption, gas adsorption, nonlinear optics, catalytic materials, and medicine [6–10], but also from their

intriguing variety of topologies and structural motifs [11–14]. However, it is still a great challenge to rationally design and control the exact structure of CPs. Generally, the structure of target CPs is influenced by several factors, such as counter ions, pH, reaction temperature, and solvent system [15]. In addition to controlling the reaction conditions, using theoretical calculations to predict and guide experimental research has long been a target for scientists [16]. What is even more important is conducting research on the reaction systems based on the combination of theory and experiment, which is conducive to revealing the preferred geometry and constructing a structural model of the compounds [17, 18].

Pyridine-based triazole ligands have been proved as a type of excellent connectors to engender a wide range of CPs resulting from the following advantages: (i) the abundant nitrogen donor atoms in the molecule can be selectively coordinated to metal ions, facilitating the generation of CPs [19] and (ii) the ligand can adopt various coordination modes, such as multidentate or bridging [20–22]. In this work, we have adopted the 3-phenyl-5-(pyridin-2-yl)-1,2,4-triazolato anion (ppt⁻) as a ligand to Co(III) to assemble a supramolecular architecture.

Based on the above considerations, we have inferred the optimized structure and conformation of the 1H-3-phenyl-5-(pyridin-2-yl)-1,2,4-triazole (1-Hppt) molecule using the density functional theory (DFT) method. The coordination polymer, $[Co(ppt)_3]$ (1), has been obtained under the hydrothermal condition, and its structure and thermostability were measured. The theoretical and experimental results are compared and discussed.

2 Results and discussion

2.1 Computational results of the 1-Hppt molecule

The optimized geometries of two different conformations shown in Fig. 1 have been obtained. The calculated bond

^aHuaixian Liu and Lin Sun: These authors contributed equally to this work.

^{*}Corresponding author: Xiangyu Liu, School of Chemistry and Chemical Engineering, Ningxia University, Yinchuan 750021, P. R. China, Tel.: +86-951-2062004, Fax: +86-951-2062860, E-mail: xiangyuliu432@126.com; L_xy@nxu.edu.cn Huaixian Liu, Lin Sun, Huiliang Zhou, Peipei Cen, Xiaoyong Jin and Qilin Hu: School of Chemistry and Chemical Engineering, Ningxia University, Yinchuan 750021, P. R. China

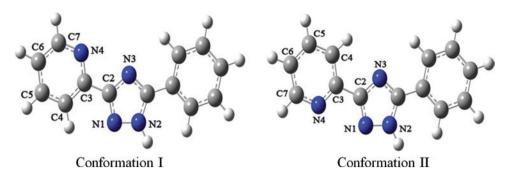


Fig. 1: Two different conformations of 1-Hppt.

lengths N1–C2, N1–N2, C2–C3, and N4–C3 are 1.335, 1.351, 1.477, and 1.404 Å, respectively.

The molecular total energies $(E_{\rm total})$, frontier orbital energy levels $(E_{\rm HOMO})$ and $E_{\rm LUMO}$, and the gaps $(\Delta E_{\rm (LUMO-HOMO)})$ of the two different conformations have been calculated, and the results are listed in Table 1. Compared with the *trans*-conformation I, the *cis*-conformation II displays lower total energies, representing the preferred geometry. The surfaces of highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) for the two conformations are shown in Fig. 2. According MO theory, the HOMO and LUMO are the most important factors that influence the properties of a compound [23].

The natural charges and electron configuration for the conformation II have been calculated by using natural bond orbital (NBO) analysis. As shown in Table 2, Mulliken charges and natural charges of the N1, N2, N3, and N4

Table 1: Calculated energies and frontier orbital energies for two conformations of 1-Hppt.

	Conformation I	Conformation II
E, hartree	-720.4099	-720.4109
E _{HOMO} , hartree	-0.22443	-0.22513
E_{LUMO} , hartree	-0.04197	-0.04388
$\Delta E_{\text{(LUMO-HOMO)}}$, eV	4.97	4.93

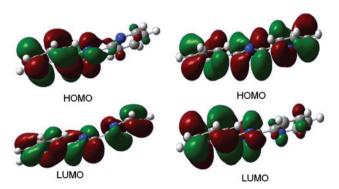


Fig. 2: Isodensity surfaces of HOMO and LUMO for 1-Hppt (left: conformation I, right: conformation II).

atoms are obtained as negative values. The natural charge of N3 (-0.52) is more negative than that of the N1 (-0.36) and N2 (-0.26) atoms in the triazole ring. The natural charge of N4 in the pyridine ring is -0.43. The results demonstrate that all four N atoms provide donor position to coordinate with metal ions.

2.2 Synthesis of complex 1

The Co(III) complex **1** was synthesized from CoF_3 and 1-Hppt in water by hydrothermal reaction at 140 °C for 3 days in the presence of terephthalic acid. The latter was not found to be incorporated in the final product which proved to be $[Co(ppt)_3]$ (**1**) as dark red crystals. The phase purity of bulk **1** was proved by a comparison of the observed and simulated powder X-ray diffraction (PXRD) diagrams as described below.

2.3 Structural description of complex 1

Single-crystal X-ray diffraction analysis reveals that the complex crystallizes in the triclinic system, space group $P\overline{1}$ with Z = 2 (Table 3). The asymmetric unit of the complex consists of one crystallographically independent Co(III) ion and three [ppt]- anions. The auxiliary ligand (terephthalic acid) did not take part in coordination. As shown in Fig. 3a, the six-coordinated Co(III) center presents a slightly distorted octahedral geometry. The four equatorial positions are occupied by three nitrogen atoms from triazole rings of three different ligands (Co1-N1 1.874(3), Co1-N5 1.900(3), Co1–N9 1.883(3) Å) and one nitrogen atom from a pyridine ring (Co1–N12 1.976(3) Å). Two nitrogen atoms from pyridine rings of two different ligands are located at the axial positions (Co1-N4 1.953(3), Co1-N8 1.954(3) Å) (Table 4). Compared to the previous reports, the Co-N bond lengths of the title complex are similar to those of Co(III) complexes (<2.0 Å [24]), and deviate from the range of Co(II)–N bond

Table 2: Natura	l configurations and natur	ral and Mulliken charges of conformation	II of 1-Hppt.

Atom	Natural electron configuration	Natural charge	Mulliken charge	
N1	[core]2 <i>S</i> (1.44)2 <i>p</i> (3.84)3 <i>p</i> (0.01)3 <i>d</i> (0.01)	-0.36286	-0.49234	
N2	[core] $2S(1.44)2p(3.79)3p(0.01)3d(0.01)$	-0.25581	-0.29671	
N3	[core] $2S(1.40)2p(4.10)3p(0.01)3d(0.01)$	-0.51760	-0.57613	
N4	[core] $2S(1.41)2p(4.01)3p(0.01)3d(0.01)$	-0.43053	-0.49547	
C2	[core] $2S(0.82)2p(2.83)3p(0.02)3d(0.01)$	0.31229	0.41707	
C3	[core] $2S(0.85)2p(2.97)3p(0.02)$	0.16323	0.25091	
C6	[core] $2S(0.98)2p(3.28)3p(0.01)$	-0.27183	-0.14027	
C7	[core] $2S(0.96)2p(3.01)3p(0.01)$	0.01968	0.04239	

Table 3: Crystallographic data and data collection and structure refinement details for complex 1.

Formula	$C_{39H_{27}CoN_{12}}$
$M_{\rm r}$	722.66
Crystal size, mm³	$\textbf{0.17} \times \textbf{0.15} \times \textbf{0.10}$
Crystal system	Triclinic
Space group	$P\overline{1}$
a, Å	12.4949(12)
b, Å	12.6369(12)
c, Å	13.3796(17)
α , deg	107.975(2)
β , deg	106.025(2)
γ , deg	110.876(3)
<i>V</i> , Å ³	1691.2(3)
Z	2
$D_{\rm calcd}$, g cm $^{-3}$	1.42
$\mu(CuK\alpha)$, cm ⁻¹	43.8
<i>F</i> (000), e	744
hkl range	$\pm 14, -14 \rightarrow 7, \pm 15$
θ range, deg	3.9-66.2
T_{\min}/T_{\max}	0.523/0.669
Refl. measured/unique/R _{int}	10 294/5905/0.058
Param. refined	469
$R(F)/wR(F^2)$ (all reflexions)	0.0937/0.1444
GoF (<i>F</i> ²)	1.007
$\Delta\! ho_{\mathrm{fin}}$ (max/min), e Å $^{\mathrm{-3}}$	0.46/-0.34

lengths (2.037–2.187 Å [25]). For the ligand, the bond lengths of N1-C2, N1-N2, C2-C3, and N4-C3 are 1.332(5), 1.345(4), 1.453(5), and 1.360(5) Å, respectively, in accordance with the calculated values. Adjacent units are connected to each other *via* two kinds of π – π stacking interactions between benzene and pyridine rings (Fig. 3b). The distance between two benzene rings is 3.909 Å, but 3.720 Å between benzene and pyridine rings, which is close to the π - π interaction distances reported in [26].

It is interesting to note that all [ppt]- ligands exhibit conformation II in the structure of the complex, confirming that the preferred conformation calculated by DFT is correct. The ligands display uniform coordination modes with pyridine N4 and triazole N1 atoms chelating the Co(III) ions. The coordination ability of N3 with the most negative charge is probably restricted by steric hindrance.

2.4 Thermogravimetric analysis and PXRD of complex 1

The thermal behavior of 1 was studied by thermal gravimetric (TG) measurements under nitrogen atmosphere

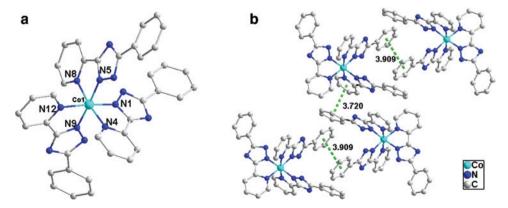


Fig. 3: (a) Coordination environment of the Co(III) ion in complex 1; (b) intermolecular $\pi - \pi$ stacking in the crystal structure of complex 1.

Table 4: Selected bond lengths (Å) and bond angles (deg) of comp

Bond		Bond		Bond	
Co(1)-N(1)	1.874(3)	Co(1)-N(5)	1.900(3)	Co(1)-N(9)	1.883(3)
Co(1)-N(4)	1.953(3)	Co(1)-N(8)	1.954(3)	Co(1)-N(12)	1.976(3)
Angle		Angle		Angle	
N1-Co1-N9	92.42(14)	N1-Co1-N5	90.11(14)	N9-Co1-N5	176.23(14)
N1-Co1-N4	82.33(14)	N9-Co1-N4	88.31(13)	N5-Co1-N4	94.80(13)
N1-Co1-N8	90.78(14)	N9-Co1-N8	94.83(14)	N5-Co1-N8	82.34(14)
N4-Co1-N8	172.55(14)	N1-Co1-N12	173.69(14)	N9-Co1-N12	81.29(14)
N5-Co1-N12	96.19(14)	N4-Co1-N12	96.84(13)	N8-Co1-N12	90.32(13)

with a heating rate of 10 °C min⁻¹. In order to confirm the phase purity of the compound, a PXRD experiment was carried out (Fig. 4). The experimental pattern matches with the simulated pattern, indicating the phase purity of the compound within the limits of experimental error. The sample was heated to 800 °C (Fig. 5). The TG curve shows that a continuous weight loss of 92.3 % is observed in the temperature range from 263 to 660 °C, due to the decomposition of the ligands (calcd. 91.84 %). The final residue mass is 7.7 % of the initial mass, which coincides with the calculated value of elemental cobalt (8.2 %), determined by PXRD (PDF 05-0727).

3 Conclusions

A Co(III) complex with the 3-phenyl-5-(pyridin-2-yl)-1,2,4-triazolato ligand has been determined under hydrothermal conditions. Single-crystal structure analysis has revealed that the title complex features a OD mononuclear structure, but forms a 3D supramolecular network

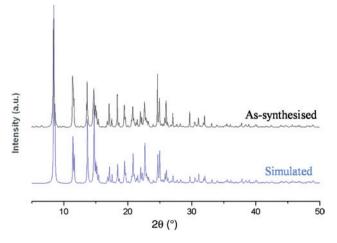


Fig. 4: Observed and simulated PXRD diagrams of complex 1.

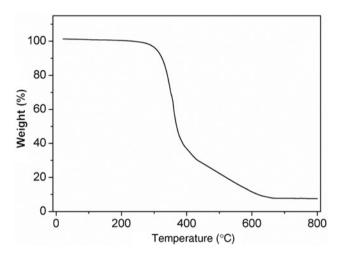


Fig. 5: TGA curve for complex 1.

through $\pi - \pi$ stacking. TG analyses showed that the complex possesses high thermostability with decomposition standing at 263 °C. The observed geometric parameters and preferred conformation of the [ppt] ligand are consistent with the DFT calculated results for the present molecule. The present work is an example of the combination of experiment and theory, providing the guidance for the design and synthesis of coordination polymers.

4 Experimental section

4.1 Materials and instruments

Commercially available solvents, such as 2-cyanopyridine, phenyl hydrazide, absolute methanol, sodium metal, terephthalic acid, and ${\rm CoF_3}$, were used as received without further purification (Xi'an Haixin Company, China). $^1{\rm H}$ and $^{13}{\rm C}$ nuclear magnetic resonance (NMR; Beijing Oxford Instrument Company, China) spectra were taken with a

Varian 400 spectrometer using tetramethylsilane as an internal standard. NMR spectra were obtained from solutions in dimethyl sulfoxide (DMSO). Elemental analyses (C, H, and N) were performed on a Vario EL III analyzer (Nanjing Hua Xin Analysis Instrument Manufacturing Company, China). Infrared (IR) spectra were obtained using KBr pellets on a BEQ VZNDX 550 FTIR (Shimadzu Corporation) instrument within the 400-4000 cm⁻¹ region. The phase purity of the bulk or polycrystalline samples was confirmed by PXRD (Brucker Company, Germany) measurements executed on a Rigaku RU200 diffractometer at 60 kV, 300 mA with CuK α radiation (λ = 1.5406 Å), with a scan speed of 5° min⁻¹ and a step size of 0.02° in 2θ . TG analysis was performed on a SETARAM Setsys16 (Nanjing Research Institute, China) instrument under N₂ atmosphere with a heating rate of 10 °C min⁻¹.

4.2 Synthesis of the 1-Hppt ligand

The ligand was synthesized according to [27]. Sodium metal (0.1 g) was added (carefully) to 40 mL absolute methanol followed by the addition of 2-cyanopyridine (2.1 g). The resulting reaction mixture was stirred with a magnetic stirrer for 80 min. Thereafter, it was allowed to cool and phenyl hydrazide (2.1 g) was added. The solution was refluxed for a further 3 h until a yellow solid complex precipitated. The precipitate was filtered off, washed with hot absolute ethanol, and dried in vacuum. The white ligand was precipitated, yield 70 % (based on 2-cyanopyridine). M.p.: 191.8–192.6 °C. – Analysis for C₁₂H₁₀N₂: calcd. C 74.97, H 4.85, N, 20.18; found C 74.92, H 4.83, N, 20.12 %. - IR (film): 3404(s), 3213(s), 3057(m), 2361(m), 1670(s), 1612(s), 1589(w), 1446(s), 1313(s), 1180(w), 1053(m), 792(m), 717(m), 696(w), 579(w) cm⁻¹. – ¹H NMR (400 MHz, $[D_c]DMSO$, 25 °C, ppm): $\delta = 6.95$ (d, 1H, Ph-H⁴), 7.49–7.51 (d, 2H, Ph-H2/H6), 7.55–7.57 (dd, 2H, Ph-H³/H⁵), 8.60–8.61 (dd, 1H, Pz-H³), 7.87–7.93 (d, 1H, Pz-H⁶), 7.53 (t, 1H, Pz-H⁴), 8.17–8.19 (t, 1H, Pz-H⁵), 10.20 (s, 1H, triazole-H). – ¹³C NMR $(75 \text{ MHz}, [D_{\epsilon}]DMSO, 25 \,^{\circ}\text{C}, ppm): \delta = 163.24, 150.75, 148.20,$ 147.85, 137.04, 134.70, 131.13, 128.31, 127.76, 124.87, 120.81.

4.3 Synthesis of complex 1

A mixture of CoF₃ (5.8 mg, 0.05 mmol), terephthalic acid (8.3 mg, 0.05 mmol), 1-Hppt (11.1 mg, 0.05 mmol), and water (6 mL) was sealed in a 10 mL Teflon-lined stainless steal vessel and heated at 140 °C for 3 days and then cooled to room temperature at a rate of 5 °C h⁻¹. Dark red crystals of complex 1 were collected in a yield of 40 % (based on Co). – Analysis for $C_{39}H_{77}CoN_{12}$: calcd. C 64.81, H 3.77, N 23.26; found C 64.75, H 3.73, N 23.20 %. – IR (film): 3599(s), 3447(s), 3063(m), 2822(m), 2662(s), 2548(s), 1690(w), 1618(s), 1576(s), 1464(w), 1425(m), 1287(m), 1111(m), 941(w), 785(w), 735(w), 696(w), 529(w).

4.4 X-ray crystallography

All diffraction data were collected on a Bruker Smart Apex CCD diffractometer with graphite-monochromatized Cu $K\alpha$ radiation ($\lambda = 1.54178$ Å) at 293(2) K. Absorption corrections were applied using SADABS [28]. The structure was solved by Direct Methods using the Shelxs program of the Shelxtl package and refined with Shelxl-97 [29]. The hydrogen atoms were located geometrically. All nonhydrogen atoms were refined anisotropically. Crystal data and numbers pertinent to data collection and refinement are given in Table 3. Selected bond lengths and bond angles are listed in Tabel 4.

CCDC 1034723 contains the supplementary crystallographic data for this paper. These data can be obtained free of charge from the Cambridge Crystallographic Data Centre via www.ccdc.cam.ac.uk/data_request/cif.

4.5 Computational details

Geometry optimization was carried out at the all-electron level using the GAUSSIAN 03 quantum chemistry program package [30] at the B3LYP/6-31G(d) [31, 32] level of theory. Mulliken population analysis, total molecular energies, and NBO calculations were also performed on the B3LYP/6-31G(d) level.

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