Review

Label-free detection with high-Q microcavities: a review of biosensing mechanisms for integrated devices

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Abstract

Optical microcavities that confine light in high-Q resonance promise all of the capabilities required for a successful next-generation microsystem biodetection technology. Label-free detection down to single molecules as well as operation in aqueous environments can be integrated cost-effectively on microchips, together with other photonic components, as well as electronic ones. We provide a comprehensive review of the sensing mechanisms utilized in this emerging field, their physics, engineering and material science aspects, and their application to nanoparticle analysis and biomolecular detection. We survey the most recent developments such as the use of mode splitting for self-referenced measurements, plasmonic nanoantennas for signal enhancements, the use of optical force for nanoparticle manipulation as well as the design of active devices for ultra-sensitive detection. Furthermore, we provide an outlook on the exciting capabilities of functionalized high-Q microcavities in the life sciences.

Keywords: biosensing; integrated photonics; microlasers; optical microcavities; optical trapping; plasmonics; optical resonator; nanoparticle detection.

1. Label-free microsystems biodetection, down to single molecules

Recent years have seen tremendous progress in the development of micro- and nanoscale optical technologies for biodetection, with research activities mainly focused on developing highly sensitive detection schemes. The sensitive and label-free detection of biomolecules such as viruses, DNA and proteins, is particularly important for implementing next-generation clinical diagnostic assays. Such assays, implemented on chip-scale devices, will replace current labor-intensive and expensive laboratory tests. These next generation microchips are ultimately expected to boast ultimate single molecule detection capability, will be integrated with other electric and microfluidic components, and will be capable of stringent and selective detection of biomolecular markers – even against the background of a multitude of other molecular species. Here, it is essential to achieve single molecule detection capability in an aqueous environment since clinical samples are water based and rapid detection relies on transduction of single molecular interaction events.

Although there are many approaches to label-free biosensing only few technologies promise single molecule detection capability potentially integrated on a chip-scale platform. Figure 1 shows what we identify as the most prominent approaches: high-Q optical resonators, plasmon resonance sensors, nanomechanical resonators and nanowire sensors. In this review we will focus on high-Q optical resonator-based biosensors and discuss their various mechanisms for biodetection, possibly down to single molecules. Similar to the nanomechanical [6, 7], electrical [8, 9] and plasmonic [1] counterparts shown in Figure 1 and Table 1, the sensitivity of optical resonators scales inversely with size. In contrast, non-resonant optical detection schemes such as those based on Mach-Zehnder interferometers [2, 28] do not. The fabrication of miniature high-Q optical microcavities from different materials and in different geometries is therefore a particularly important engineering task as we will review in the following. Furthermore, nanotechnology-enabled optical microcavities are not only one of the most sensitive approaches to probing the biological world in solution, they also are multi-function sensing platforms and we will highlight various mechanisms for sizing, trapping, and manipulating at the nano-scale [29–32].

2. Optical resonator-based biomolecular sensors: mechanisms for detection

2.1. Light confinement in high-Q optical microcavities

For most single-pass optical devices, such as waveguide and optical interferometers, light interacts with the analyte molecules or proteins only once. Thus to enhance the interaction between the light and the sensing target usually one must increase the physical length of the sensor. However, in a resonator-based sensor where light is confined in a micron scale sensor element and where the light waves interfere constructively, we can increase the effective interaction length by increasing the optical quality factor (Q) of the resonant system. The quality factor (Q), which is used to quantify the temporal confinement of the electromagnetic energy is defined as

\[ Q = \frac{\int U(t) \, dt}{\left( \frac{dU(t)}{dt} \right) |_{0}^{\infty}} \]

(1)
where $U(t)$ is the total energy of the confined light field and $-(dU(t)/dt)/\omega_0$ is proportional to the energy that is lost for each electromagnetic oscillation. From this it follows that the energy of the charged cavity will decay over time with $U(t)=U_0 \exp(-\omega_0 t/Q)$ once the light source has been shut off. The ringdown time $\tau$ measured with a photodetector placed in close proximity to the microcavity, is $\tau=Q/\omega_0$. The exponentially decay of the energy $U(t)$ is characteristic of a resonant system. The energy $U(t)$ is proportional to the electromagnetic field strength squared $U(t)=E(t)^2$, and it follows that the complex field evolves in time as: $E(t)=\exp(-\omega_0 t/2Q)\exp(-i\omega t)$. Time and frequency domains are linked by Fourier transforms:

$$E(t) \approx \frac{1}{\sqrt{2\pi}} \int E(\omega) e^{-i\omega t} d\omega,$$

and we therefore expect a spectral response that exhibits a Lorentzian line:

$$|E(\omega)|^2 \approx \frac{1}{(\omega-\omega_0)^2 + (\Delta\omega/2Q)^2},$$

where $\omega_0$ is the resonance wavelength and $\Delta\omega=\omega_0/Q$ is the linewidth (full width at half maximum, FWHM). The (total) intrinsic $Q$-factor of an optical mode is calculated from $1/Q_{(\text{total})} = 1/Q_{\text{absorption}} + 1/Q_{\text{scattering}} + 1/Q_{\text{radiation}}$, where $1/Q_{\text{absorption}}$ denotes losses of photons by material absorption, $1/Q_{\text{scattering}}$ represents scattering losses due to surface inhomogeneities or surface defects, and $1/Q_{\text{radiation}}$ is set by the radiative losses [33]. For optical resonators with negligible amount of losses from radiation such as for example $\sim 100$ $\mu$m silica microsphere, the ultimate material limited $Q$ factor [33, 34] is close to $Q_{\text{material}} = \frac{2\pi n_{\text{glass}}}{\alpha_{\text{glass}}} \lambda = 10^9$.

The reported optical attenuation coefficient of $\alpha_{\text{glass}} \sim 7$ $\text{dB/km}$ (where $\sim 5$ $\text{dB}$ is bulk Rayleigh scattering and $\sim 2$ $\text{dB}$ is absorption). Low dissipation systems with high $Q$ factors are particularly suitable for monitoring perturbations of the resonance signal [35] and thus for detecting biomolecules [10]. For example, in an optical microsphere-resonator (Figure 2) with a $Q$-factor of $10^7$ a photon (with a wavelength of 600 nm) has a lifetime of $\sim 30$ $\text{ns}$ and can travel in the cavity for $\sim 10$ $\text{m}$ before it is lost. If the round trip of the photon in the cavity is $100$ $\mu$m, the photon will interact with a target molecule more than $10^7$ times. This creates a “signal build-up process” inside the resonator that gives rise to significant signal amplification and allows ultra-sensitive detection of biomolecules.

High-$Q$ optical resonators have been investigated intensively over the past decade as a promising technology for ultra-sensitive and label-free biosensing [10, 36]. One of the most promising designs is the whispering-gallery-mode (WGM) resonator [37, 38], in which light is trapped in circular orbits by total internal reflections from the boundaries of the resonator (Figure 2). WGM resonators exhibit the highest $Q$ factor [39], up to three orders of magnitude higher than other types of resonators. Other types of high-$Q$ WGM-type microcavity biosensors are ring resonators [40], microtoroids [16], and glass capillaries – so called liquid-core optical-ring resonators (LCORR) [41]. The ultra-high-$Q$ resonators possess many interesting properties, not available in other photonic devices, such as ultra-low loss, ultra-long photon lifetime and ultra-high intracavity power and intensity. Due to these unique attributes, the minimum detectable concentration of a target molecule, i.e., the detection limit, is significantly lower in the ultra-high-$Q$ resonators than in other types of sensors. In fact, it has been demonstrated that a single virus or nanoparticle can be detected by a WGM resonator [3, 30].

As evidenced in Figure 3, few components are needed for an experimental realization of a WGM biosensor. In one implementation, a continuous-wave tunable distributed feedback laser (DFB), for example operating in the telecom band at 1.3 $\mu$m wavelength, excites high-$Q$ optical resonances in a microsphere via a tapered optical fiber. The resonances are excited by evanescent coupling from a tapered section of a single mode optical fiber [43, 44], a method that transfers a high power fraction from the fiber to the microcavity. In fact it has been shown that even critical coupling (no transmission at the output of the waveguide on resonance) can be achieved if the coupling distance and the taper diameter is carefully controlled [45]. Moreover, tapers can be fabricated in automated setups [46]. Once coupled, the microsphere spectrum is recorded by sweeping the wavelength of the laser, typically over a narrow spectral range of $\sim 0.3$ $\text{nm}$. It is worth noting that the $Q$ factor is now further modified by the coupling $Q$ factor [47].
More recent biosensing demonstrations utilize other evanescent coupling schemes such as those based on prism coupling [48, 49] and coupling from integrated bus waveguides [24, 50–53]. Both approaches provide for better mechanical stability [54], improved signal-to-noise-ratio [52] and potential for multiplexed excitation, as well as referenced readout of several microcavities in parallel [49]. For a robust biosensor application the integration of such sensor components in a mechanically stable platform is essential. Ultimately, the laser source could be fully integrated on-chip [55], but for now different external lasers, such as DFB as well as external cavity lasers, must be used [13, 30, 56].

2.2. The reactive biosensing principle

Although the principle applies to any optical microcavity geometry, we will review the detection mechanism for a WGM microsphere sensor, where analytical results are most instructive. Like a nanomechanical resonator biosensor [4], the microsphere optical resonator detects the binding of analyte molecules as changes in the resonance frequency. A WGM exhibits a quite large sensitivity to such perturbations because the light field is confined close to the surface where the evanescent field interacts strongly with the surrounding medium.

The binding of a biomolecule will shift the WGM resonance frequency by a miniscule amount (Figure 4). The shift to longer resonance wavelength occurs because the bound biomolecule will effectively "pull" part of the optical field to the outside of the microsphere, thereby increasing the round-trip path length by \(2\pi\Delta l\). This increase in path length produces the shift (\(\Delta \omega\)) to lower frequency.

The binding of a streptavidin molecule to a microsphere provides an example [13]. Note that a streptavidin molecule (\(\sim 4\) nm) is small with respect to the radial extension of the evanescent field associated with a WGM. Once bound at the surface where the evanescent field strength \(E(r)\) is high, the molecule will become polarized at the optical frequency \(\omega\). The overall induced dipole moment \(P\) is calculated as \(P = \alpha_{\text{ex}} E\), where \(\alpha_{\text{ex}}\) is the excess polarizability of streptavidin, in excess of that of the water it displaces [12, 13]. The energy that is needed to polarize the molecule and induce this dipole moment is \(\frac{1}{2} \alpha_{\text{ex}} |E(r_0)|^2\), where \(E(r_0)\) is the electric field strength at the streptavidin binding site \(r_0\), and

![Figure 2](image-url)  
**Figure 2** Left: total internal reflection of a whispering-gallery-mode (WGM) in a glass microsphere. Right: corresponding wave optics.
$\alpha_{\text{streptavidin}} \sim 4\pi \varepsilon_0 \times 3.3 \times 10^{-21} \text{ cm}^3$. By first order perturbation theory, we can now estimate the frequency shift by comparing the energy that is needed to polarize the biomolecule to the total electromagnetic energy stored in the unperturbed resonator [12]:

$$\frac{\Delta \omega}{\omega} = \frac{\alpha_{\text{streptavidin}}}{2} \frac{\left| \varepsilon(r) \right|^2}{\int \varepsilon(r) dV}$$

(2)

where $\varepsilon$ is the permittivity of the medium. Equation (2), the reactive biosensing principle, allows one to quantify the frequency shift of any optical resonator in response to molecule or nanoparticle binding events.

A large $Q$ factor is necessary in order to resolve the fractional frequency shift $\Delta \omega/\omega$ predicted by Eq. (2). In practice one monitors the resonance wavelength shift $\Delta \lambda$, which is $\Delta \lambda/\lambda = -\Delta \omega/\omega$. The limit of detection, i.e., the smallest detectable wavelength shift $\Delta \lambda_{\text{min}}$, is not simply the linewidth $\Delta \lambda_{\text{FWHM}}$. A shift of only a fraction $F$ of $\Delta \lambda_{\text{FWHM}}$ can be sensed [38], so that $\Delta \lambda_{\text{min}}/\lambda = F \cdot \Delta \lambda_{\text{FWHM}}/\lambda = F/Q$, where the figure of merit $F$ is typically [57] 1/50–1/100 and determined by noise sources such as thermal-refractive noise [58].

Importantly, the magnitude of the wavelength shift $\Delta \lambda$ itself is inversely proportional to the mode volume $V_{\text{mode}}$ given by the denominator in Eq. (2), which for a WGM in a microsphere is [59]

$$V_{\text{mode}} = \frac{\int E^2 dV}{\int (3.4 \pi^{3/2} \lambda/2 \pi N)^{1/6} \sqrt{1-m+1} dV}$$

(3)

Reducing the size (modal volume) of the optical resonator thus boosts sensitivity. For the microsphere, the optimal resonator diameter can be calculated, because radiation loss limits the $Q$ factor in very small microspheres as the diameter approaches the wavelength of the confined light [59].

### 2.3. The mode splitting biosensing principle

An alternative to the reactive biosensing principle is the mode-splitting effect, i.e., one resonant mode splitting into two resonances due to interaction of light with nanoscale objects, such as nanoparticles, in the mode volume. Because light can propagate clockwise (CW) or counterclockwise (CCW) in a WGM resonator with a circular boundary, the optical mode in such a resonator possesses a two-fold degeneracy. The degenerate modes share the same resonant frequency $\omega_c$ and field distributions but propagate in opposite directions; a

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Figure 3 Probing high $Q$ resonances of different optical resonators in biosensor applications. (A–D) Reproduced with permission from [13, 24, 30, 42]. (reprinted with permission from [23]. Copyright (2002), American Institute of Physics. Reprinted from [42]. Copyright (2010), with permission from Elsevier.).
single resonance appears in the transmission spectrum of the resonator.

When a WGM field encounters a light scattering center, such as a molecule or particle, on its optical path, the light is scattered elastically from the particle/molecule. A portion of light is scattered and lost to the environment, while some is scattered back into the mode volume and takes the optical path of the counterpropagating frequency-degenerate mode, coupling between the CW and CCW modes. This lifts the degeneracy of the two modes. Two standing wave modes are formed in the cavity, and this is reflected in the splitting of the single resonance into a doublet structure, i.e., two resonances, in the transmission spectra of the resonator (see Figure 5). Because the two split modes reside in the same resonator, they share many noises sources, such as temperature variation, and since they are compared to one another, this is a self-referencing sensing technique [30].

The mode-splitting effect in WGM resonators was first reported as an interesting phenomenon in high-Q microspheres [60, 61]. It has since been demonstrated in various WGM resonators with different geometries, including microspheres, microtoroids and microdisks [30, 62–64]. Many factors, such as surface defects, material inhomogeneities, and nanoparticles, all of which can induce light scattering in the mode volume of a WGM, may cause mode splitting. Assuming a subwavelength scattering center (Rayleigh scatterer), and that the electric field of the coupled WGMs induces a dipole in the scatter, the interaction between the WGM and the scatterer can be modeled using a dipole approximation [30, 61, 62]. Polarizing the scatterer induces a coupling between the two counter-propagating WGMs. The coupling coefficient \( g \) depends strongly on the polarizability \( \alpha \) of the scatterer and the location of the scatterer in the mode volume \( V_c \) with respect to the mode distribution. We can derive \( g \) as:

\[
g = -\frac{\alpha f(r) \omega_c}{2V_c}
\]  

where \( \omega_c \) is the resonance frequency, \( f(r) \) accounts for the cavity mode distribution of the WGM at location \( r \), \( \alpha \) represents the polarizability of the scatterer which for a spherical scatterer of radius \( R \) can be expressed as \( \alpha = 4\pi R^3(\varepsilon_p-\varepsilon_s)/(\varepsilon_p+2\varepsilon_s) \) in which \( \varepsilon_p \) and \( \varepsilon_s \) denote the electric permittivities of the particle (scatterer) and the surrounding medium, respectively.

Through the interaction of the scatterer with the WGM field, a portion of the field is lost to the environment, adding to the damping. Using a Weisskopf-Wigner approximation, the damping rates due to coupling to the reservoir via Rayleigh scattering is:

\[
\Gamma_g = \frac{\alpha^2 f^2(r) \omega_c^2}{6\pi V_c^3}
\]  

Figure 4 (A) Illustration of a Whispering Gallery Mode (WGM) optical resonance in a glass microsphere. The binding of a protein to the microsphere surface increases the WGM path length by \( \Delta l \), which is detected as a resonance frequency shift \( \Delta \omega \). (B) The reactive sensing principle. A molecule binding to the microsphere surface is polarized within the evanescent field (yellow ring) of a WGM. The energy that is needed to polarize the molecule causes the resonance frequency to shift.

Figure 5 Mode splitting in a WGM resonator. Left: WGM resonators supports degenerate counter-propagating modes: clockwise (CW) and counterclockwise (CCW). Light scattering from a scattering center introduces additional damping to the optical modes and couples the initially degenerate CW and CCW modes, lifting the mode degeneracy. Right: Experimentally obtained mode-splitting transmission spectrum (blue) after the deposition of a single nanoparticle in the mode volume of a microtoroid WGM resonator and the fitted curve (red) adapted from [30].
where $v = c/\sqrt{\varepsilon_m}$ is the velocity of light in the surrounding environment and $c$ is the speed of light in vacuum.

The polarizability of a nanoparticle can be calculated from the mode-splitting transmission spectrum of WGM resonator after a nanoparticle is adsorbed on its surface. The coupling strength $g$ is quantified by the doublet splitting $g = \delta \omega$, where $\delta$ is the frequency detuning of the two split modes. The additional linewidth broadening is $\Gamma = \pi \gamma L$, where $\gamma$ and $\gamma_L$ represent the linewidths of the split modes. The ratio of $(\gamma_L - \gamma)/\delta$ carries information about the polarizability of the particle, and hence on its size and permittivity (i.e., its refractive index). Comparing Eqs. (4) and (5) it is clear that the polarizability of the nanoparticle is then: $\alpha = 4\pi R^3 (\varepsilon - 2\varepsilon_p)/(\varepsilon + 2\varepsilon_p) = (3\lambda^2/8\pi^2)(\Gamma^2/\delta)$. It is important to note here that the measurement of $\Gamma^2/\delta$ is independent of the position of the particle on the resonator. The position-independence of the value of $\Gamma^2/\delta$ gives the mode-splitting technique advantages over schemes using single-resonance spectral shift, which are affected by the particle position.

Once mode-splitting is introduced by the first scatterer, two orthogonal standing-wave modes are formed by the superposition of the split modes in the resonator. The next scatterer deposited/adsorbed scatterer in the mode volume interacts with the two orthogonal modes differently, and subsequently the two standing waves re-distribute themselves to maximize the amount of mode splitting. Given this physical mechanism, we can derive the polarizability of the mechanism, we can derive the polarizability of the respective two standing waves  re-distribute themselves to maximize the amount of mode splitting. Given this physical mechanism, we can derive the polarizability of the

$$\Gamma = \pi \gamma L$$

$$\frac{\Delta \omega}{\gamma} = \frac{\Delta \lambda}{\Delta \lambda} = \frac{\Delta \omega}{\gamma} = \frac{\Delta \lambda}{\Delta \lambda} = \frac{\Delta \omega}{\gamma} = \frac{\Delta \lambda}{\Delta \lambda}$$

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2.4. Detecting biomolecular mass loading

The detection capabilities of a spherical optical resonator biosensor can be predicted by analytic equations [12, 73–79]. For a single nanoparticle binding on the microsphere excited in the fundamental WGM mode $Y_l$, one predicts a resonance frequency shift of [3, 12, 38]

$$\Delta \omega = -\frac{\alpha_{nc}}{\varepsilon_0 R^3 \left(n_s^2 - n_m^2\right)}$$

where $r_p$ is the particle binding site, $L$ is the evanescent field length, $R$ is the microsphere radius, $n_s$ and $n_m$ are the refractive indices of the sphere and the medium, respectively. For a biomolecule that is small compared to the wavelength the exponential factor is negligible. For N molecules binding at random locations to the microsphere surface with surface density $dN/d\Omega = \sigma 4\pi R^2/4\pi$ ( $\Omega$ is the solid angle) Eq. (7) becomes [12]

$$\frac{\Delta \omega}{\omega} = -\frac{\alpha_{nc}}{\varepsilon_0 \left(n_s^2 - n_m^2\right)}$$

allows mode splitting to be detected even if [2g] is smaller than the linewidth of the modes. It also provides an alternative way to detect mode-splitting signals without requiring a tunable laser. Recently an optical gain medium, which helped narrow down the linewidths of the optical modes, was also used to recover mode-splitting from what initially appeared as a broad, single resonance [70].

The first experimental demonstration of size measurement of single nanoparticles utilized a high-Q microtoroid WGM resonator [30]. In this work, single potassium chloride (KCl) and polystyrene nanoparticle as small as 30 nm in radius were detected and measured by analyzing the mode-splitting spectra. Consecutive size measurement of nanoparticles deposited one by one into the mode volume of a high-Q resonator was also achieved by analyzing the frequencies and linewidths of the resonances in the mode-splitting spectra right before and after the deposition of each particle [65].

When a resonator is in liquid solution, the smaller difference between the refractive indices of the resonator and surrounding medium degrades $Q$ factor because it leads to increased radiation loss and decreased particle polarizability. Absorption loss in the surrounding medium is also greater, which further decreases the $Q$ factor of resonant modes. As Eq. (6) suggests, sensing applications in an aquatic environment are more difficult than those in air. To address this issue, a resonator with a $Q$ factor high enough to tolerate the $Q$ degradation must be used [71, 72]. One strategy is to use a thermally-stabilized reference interferometer to reduce the frequency noise in the measurement of mode-splitting. By means of such a scheme, a high-Q microtoroid has been used to detect polystyrene nanoparticles with radii down to 12.5 nm and Influenza A virions in aquatic environment [67].
where $\sigma$ is the surface density of bound biomolecules (typically reported in units of cm$^{-2}$). The excess polarizability of protein or DNA biopolymers is determined from measurements of the refractive index increment $dn/dc$ of the pure biopolymer solution. The excess polarizability is then related to the refractive-index increment by

$$\alpha = \varepsilon_0 \frac{dn}{dc}_{\text{biopolymer}} m_{\text{biopolymer}}$$  \hspace{1cm} (9)$$

where $\varepsilon_0$ is the vacuum permittivity, $n_3$ is the solvent (water) refractive index, $m$ is the molecular weight of the biomolecule (streptavidin: ~1 × 10$^{-19}$ g) and the $dn/dc$ of protein [11] is ~0.183 × 10$^{-9}$ mm$^3$ pg$^{-1}$, $dn/dc$ of DNA ~0.166 × 10$^{-9}$ mm$^3$ pg$^{-1}$. With this Eq. (9) in hand, we can calculate the mass loading (mass.1) associated with the resonance frequency shift and plot the sensor response (sensogram) in units of picograms per millimeter squared sensor area [10]:

$$\text{mass.1} \left[ \text{pg mm}^{-2} \right] = \frac{\Delta \sigma}{\sigma} \frac{(n_l^3 - n_m^3) \times R_{[\text{mm}]}}{2 \times n_m \times \frac{dn}{dc}_{\text{biopolymer}} m_{\text{biopolymer}} \text{pg mm}^{-3}}$$  \hspace{1cm} (10)$$

A similar analysis has been done for LCORRs where calculations for resonance wavelength shifts are calculated as [80]

$$\frac{\delta \lambda}{\lambda} = \frac{\alpha \varepsilon_0 2 \pi R_h E \hat{r}^2}{E(\hat{r})} \frac{dV}{\varepsilon_0} = \frac{2 \pi n_l^3 - n_m^3}{\varepsilon_0 \alpha^2} S$$  \hspace{1cm} (11)$$

where $n_l$ refractive index of medium, $n_m$ is the refractive index of the LCORR, and bulk index sensitivity $S = \delta \lambda / \delta n_l$. For details of this derivation we refer to [80]. For other resonator geometries such as toroids, this analysis has do be done by simulation [81], because no analytic equations that describe the confined light fields are available. In practice, the sensor response is often experimentally determined (calibrated) for different solution concentration levels [51, 82–84]. Examples for this are shown in Figure 6. In surface-based biosensing the most physical and accurate figure of merit is the limit of detection (LOD) in units of pg/mm$^2$ mass loading, see Eq. (10). Very often, researchers also report the sensitivity to bulk index change in units of nm wavelength shift per refractive index unit (RIU): nm/RIU. Although binding kinetics are typically measured by stepwise titration of analyte concentrations, researchers recently reported a method for determining kinetic rates and equilibrium binding affinities in a single experiment during which analyte concentration increased in a nonlinear gradient [91].

Once the sensor response for different solution concentrations has been experimentally determined or analytically calculated, the sensor can then be used to determine unknown concentrations of an analyte. To ensure only the molecules of interest are detected, the resonator surface is modified (“functionalized”) with elements that recognize the analyte, such as antibodies [82, 84, 92], DNA oligonucleotides [57, 89, 93–96], aptamers [97] or other receptors [13, 98–101]. A few examples are shown in Figure 6 and Table 2 gives an overview of the recognition elements and the sensitivity levels that have been obtained with each element. Opto-fluidic ring resonators (OFRR, LCORR) in particular have been used extensively in various biosensing tasks, such as the detection of organophosphorus pesticide [109], label-free DNA methylation analysis [100], detection of breast cancer biomarker CA15-3 in serum samples [110], and detection of the HER2 breast cancer biomarker [42]. Also silicon, silicon nitrate and polymer ring resonators have been used to detect: antigen (PSA), alpha-fetoprotein (AFP), carcinoembryonic antigen (CEA), tumor necrosis factor-alpha (TNF-alpha), and interleukin-8 [51]; single nucleotide polymorphisms [90], DNA and mRNA [88, 96] as well as tmRNA [105], C-reactive protein (CRP) [84], cytokines interleukin-2 (IL-2), interleukin-4 (IL-4), interleukin-5 (IL-5), and tumor necrosis factor alpha (TNF alpha) [83]; IL-2 [82]; avadin [53, 111]; cadaverine [52] and antibodies [92]. In combination with nanoparticles, different kinetic modalities for sensing have been demonstrated in toroidal cavities [112] and enhancement of sensitivity in a nanoparticle-sandwich assay was demonstrated on silicon ring resonators [84].

Crucial to achieving specificity is the chemical modification of resonator surfaces, which strongly depends on their material properties. For example, for the modification of glass (and the thermal oxide layer on silicon) one can use silanization of the glass-silanol groups [13, 16] or physisorption of proteins and hydrogels [57, 107]. In multiplexed arrays, each sensor element can be individually functionlized, by, for example fluids controlled with microfluidics [23, 24], or ink-jet printing [113] or patterning with silicon etchants [114]. Also very recently, one and two-dimensional photonic crystal resonators have been explored to detect biomolecules, including interleukins 4, 6 and 8 [115] and bovine serum albumin [116] as well as immunoglobulins [106]. Table 2 gives an overview on
molecules that have been detected with optical microcavities, as well as the reported detection limits. Detection limits in the 10 pM range rival those of conventional enzyme-linked-immunosorbent assays (ELISAs).

3. Optical resonator biosensors: materials and geometries

The material and geometry of a microcavity affects its $Q$ factor as well as modal volume $V$ and the optical field’s overlap with analyte molecules. Table 3 gives an overview of the $Q$ and $V$ values for a variety of optical resonators that are currently being championed for biosensing applications. In the following chapter we will focus on the most prominent candidates and review the most recent materials, geometries and sensing approaches.

3.1. High-Q microsphere cavities

Perhaps the simplest example for an optical resonator is a $\sim 100 \mu$m-diameter silica microsphere, where light remains confined due to total internal reflection [150], see Figure 7. Although glass has low dissipation, light confined inside the microsphere is eventually lost due to absorption and scattering. The high-Q microspheres are simple to fabricate. They can be made by melting spheres at the end of high quality optical fiber with a hydrogen torch [33] or a CO2 laser beam [34]. Microspheres fabricated from a standard single mode optical fiber and immersed in a liquid have been used in many biosensor experiments [13, 48, 57, 87, 97, 117, 152], including the first biosensor demonstration in 2002 [13]. Placing the sphere in a liquid limits $Q$-factor to $\sim 10^7$–8 [71, 153], however, because the liquid absorbs light.
Among the resonances of the high-Q micro-spheres, the modes localized along the equator are of particular interest [34]. These WGMs combine a good spatial confinement of the field with the very high-Q factors \((Q)\), two features which are of great importance for sensitive biodetection. Figure 7 illustrates an equatorial mode in an erbium-doped microsphere excited by light transferred from a tapered fiber.

The transverse electric and transverse magnetic fields confined in a microsphere are described by

\[
E_{TE} = j_n(nkr)Y_{lm}^{(\theta, \phi)} \\
E_{TM} = \nabla \times j_n(nkr)Y_{lm}^{(\theta, \phi)}
\]

where \(Y_{lm}^{(\theta, \phi)}\) are the vector spherical harmonics, and \(j_n(nkr)\) represent the spherical Bessel functions, with \(k = 2\pi/\lambda\). These resonances can also be viewed as quasi-bound states of a Bohr-like atom modes [154, 155]. For the Bohr as well as the photonic atom, wave functions are indexed by three quantum numbers \(n, l, m\), where \(n\) represents the number of nodes in radial directions, \(l\) is the angular-mode number proportional to the number of wavelengths in one orbit, and \(m\) is the azimuthal mode number. Modes with the same \(l\)-number but different \(m\) values are degenerate in a perfect sphere, however, for spheres made by melting of a fiber tip this degeneracy is typically removed and instead they exhibit a spectrum rich with modes of different \(m\) numbers. By observing different TE and TM modes in a microsphere it is possible to detect the orientation of molecules bound at the microsphere surface [104, 156]. Furthermore, wavelength multiplexing of several WGMs simultaneously can provide information on the thickness of an adsorbed layer [157].

Microspheres are particularly suitable for table-top experiments since they are easily fabricated [33, 34, 120] and their mode structure is amenable to rigorous theoretical analysis [73, 76–78, 158, 159], as well as simulations based on Mie theory [147, 160]. Recent demonstrations of high-Q microspheres include studies of protein adsorption [87], thrombin detection [97] and refractive index sensing [48, 117]. Very high sensitivity allows the detection of single particles such as polystyrene nanoparticles and virus particles [3, 32]. Recent developments include efforts to further improve the sensitivity [58, 81, 147, 152, 156], multiplexing capability [49] and functionalization strategies [16, 54].
Table 3  Examples for microcavities that have been utilized or proposed for utilization in biosensing applications.

<table>
<thead>
<tr>
<th>Optical resonator</th>
<th>Device example</th>
<th>$Q$ in air/in water</th>
<th>Diameter</th>
<th>Fabrication</th>
</tr>
</thead>
<tbody>
<tr>
<td>Microsphere waveguide coupled [13, 32, 38, 75, 87, 102, 117, 118]</td>
<td><img src="image1.png" alt="Microsphere waveguide" /></td>
<td>$8 \times 10^3/10^7$–$10^8$</td>
<td>50–500 μm</td>
<td>Usually formed by melting a fiber tip</td>
</tr>
<tr>
<td>Microsphere, prism coupled [48, 119] (reprinted with permission from [48], copyright (2008), American Institute of Physics)</td>
<td><img src="image2.png" alt="Microsphere prism coupled" /></td>
<td>$9 \times 10^3$</td>
<td>30–40 μm</td>
<td>Arrayed from a batch of polystyrene microspheres in solution</td>
</tr>
<tr>
<td>Microsphere, angle polished fiber coupled [120, 121] (reproduced with permission, © (1999) Optical Society of America)</td>
<td><img src="image3.png" alt="Microsphere angle polished fiber coupled" /></td>
<td>$1 \times 10^8$</td>
<td>~500 μm</td>
<td>Microspheres fabricated by fusing high-purity silica preforms in a hydrogen-oxygen flame</td>
</tr>
<tr>
<td>Microtoroid, fiber coupled [16, 66, 67, 70]</td>
<td><img src="image4.png" alt="Microtoroid fiber coupled" /></td>
<td>$8 \times 10^3/10^7$–$10^8$</td>
<td>30–200 μm</td>
<td>CO$_2$ reflow of an under-cut silica micro-disk on silicon wafer</td>
</tr>
<tr>
<td>Ring resonator, waveguide coupled [24, 52, 53, 111, 122–125] (image reproduced with permission from the publisher, [24])</td>
<td><img src="image5.png" alt="Ring resonator waveguide coupled" /></td>
<td>$4 \times 10^4$–$2 \times 10^6$</td>
<td>~20–200 μm</td>
<td>Ring resonator sensor arrays fabricated by lithography technology</td>
</tr>
<tr>
<td>Fluorescent microsphere [93, 101, 126–129] (image reproduced with permission from the publisher, [127])</td>
<td><img src="image6.png" alt="Fluorescent microsphere" /></td>
<td>$5 \times 10^5$</td>
<td>~8–15 μm</td>
<td>Microspheres doped with optical gain medium, such as dye</td>
</tr>
<tr>
<td>Capillary, fiber coupled (LCORR) [42, 56] (reproduced with permission, ©(2006) Optical Society of America)</td>
<td><img src="image7.png" alt="Capillary fiber coupled" /></td>
<td>$10^7$–$10^9$</td>
<td>~150 μm</td>
<td>Softening (CO$_2$ laser) and stretching a fused silica capillary</td>
</tr>
<tr>
<td>Disk resonator [130, 131], waveguide coupled (reprinted from [131], copyright (2010), with permission from Elsevier)</td>
<td><img src="image8.png" alt="Disk resonator waveguide coupled" /></td>
<td>~$10^4$</td>
<td>10 μm–100 μm</td>
<td>Fabricated from silicon oxy-nitride film on a silicon wafer by lithography technology</td>
</tr>
<tr>
<td>Bottleneck resonator [132]</td>
<td><img src="image9.png" alt="Bottleneck resonator" /></td>
<td>~$10^8$</td>
<td>30–40 μm</td>
<td>Fabricated from standard optical glass using a two-step heat-and-pull process</td>
</tr>
<tr>
<td>Microtube ring resonators [133, 134] (reprinted with permission from [133], copyright (2011) American Chemical Society)</td>
<td><img src="image10.png" alt="Microtube ring resonators" /></td>
<td>$100$–$300$</td>
<td>&lt;10 μm</td>
<td>Roll up of a strained SiO/ SiO$_2$ nanomembrane to form a micro-tube with thin wall</td>
</tr>
</tbody>
</table>
### Table 3 (continued)

<table>
<thead>
<tr>
<th>Optical resonator</th>
<th>Device example</th>
<th>$Q$ in air/in water</th>
<th>Diameter</th>
<th>Fabrication</th>
</tr>
</thead>
<tbody>
<tr>
<td>Photonic crystal resonator [115, 116, 106, 135–137] (reproduced with permission, © (2007) Optical Society of America)</td>
<td><img src="image" alt="Photonic crystal resonator" /></td>
<td>$10^6$</td>
<td>Micron-scale</td>
<td>e-beam lithography and reactive ion etching</td>
</tr>
<tr>
<td>Fabry perot resonator [138]</td>
<td><img src="image" alt="Fabry perot resonator" /></td>
<td>Finesse: $38$</td>
<td>$40 \mu m$</td>
<td>Resonator is formed between two highly reflecting reflectors composed of two period Si/SiO$_2$ Bragg structures</td>
</tr>
<tr>
<td>Fiber-based [139, 140] (reprinted with permission from [139], copyright (2005), American Institute of Physics)</td>
<td><img src="image" alt="Fiber-based" /></td>
<td>$10^4$–$10^6$</td>
<td>$20$–$200 \mu m$</td>
<td>Resonator is formed between the plane tip of a fiber and a concave micro-mirror fabricated by standard silicon etching and optical coating techniques</td>
</tr>
<tr>
<td>Microbubble [141–143] (reproduced with permission, © (2011) Optical Society of America)</td>
<td><img src="image" alt="Microbubble" /></td>
<td>$10^2$–$10^7$</td>
<td>$70$–$500 \mu m$</td>
<td>Heating a glass capillary with a CO$_2$ laser</td>
</tr>
<tr>
<td>Micro-coil [144–146]</td>
<td><img src="image" alt="Micro-coil" /></td>
<td>$10^5$</td>
<td>$500 \mu m$</td>
<td>Wind a microfiber coil on a cylindrical rod with lower refractive index</td>
</tr>
<tr>
<td>Photonic-plasmonic WGM: microsphere coupled to nanoantenna [58, 147–149] (reprinted with permission from [147], copyright (2011), American Institute of Physics)</td>
<td><img src="image" alt="Photonic-plasmonic WGM" /></td>
<td>$/10^6$</td>
<td>Light localized at the nanoantenna site</td>
<td>Nanoparticle layer deposition, nanoparticle WGM trapping</td>
</tr>
</tbody>
</table>

**Figure 7** Equatorial WGM. The green ring, which traces the trajectory of the fundamental equatorial WGM, is due to the luminescence of the erbium ions with which the microsphere is doped image taken from [151].

### 3.2. Ring and disk resonators

Ring and disk resonator geometries were among the first to be proposed for biosensing applications, and they have since become the most prominent resonators in biosensing. They are fabricated on-chip with photolithographic techniques in different materials systems and in large sensor arrays [24, 40, 50, 52, 53, 89, 130, 131, 162–168]. For example, ring, racetrack and disk resonators can be fabricated in silica, silicon [24, 50, 89, 111, 166, 168] and organic polymers [52, 165, 167, 169, 170]. Early biosensing demonstrations proposed a high-finesse (low loss) WGM disk resonator [130] and utilized...
a vertically coupled glass microring resonator with Q of about 12000 [111] as well as an integrated silicon nitride (Si$_3$N$_4$/SiO$_2$) ring resonator [53]. Within arrays, individual sensors can be used as an internal reference, thereby eliminating noise due to thermal fluctuations and nonspecific molecular binding events [24]. Often compatible with CMOS techniques, ring and disk resonators are ideal candidates for integration into portable electronic devices and commercial bench-top systems [92] and indeed silicon ring resonator biosensors are already on the market. Microfabricated ring/disk resonator arrays are also quite easily incorporated with microfluidics because they are fabricated on planar substrates.

One interesting approach to integration is an electrical tracing-assisted dual-microring resonator-based optical sensor system fabricated on silicon-on-insulator (SOI) wafer. The resonance wavelength shift of a sensing microring is measured by the electric power needed for a second, tracing microring to match the resonance shift. The electrically tunable tracing microring thus eliminates the need for wavelength scanning of a laser source [171]. Nanoporous polymer ring resonators reportedly increase device sensitivity by 40% because bio-analyte enter pores and interact with electromagnetic energy in the core of the ring, not just its surface [169]. Cascaded microrings that exploit the Vernier effect have also recently been proposed to increase sensitivity [172, 173]. In addition, it was found that for certain sensing schemes extending the ring cavity length of SOI microring sensors increases the resonator quality factor, and can thereby enhance the sensor resolution and minimum level of detection [103]. Vertically stacked microracetrack made from the photoresist SU8 have low noise and are exceptionally stable, although prone to temperature fluctuations [52].

In the meantime, the applications for these sensors have also been expanding. A commercial silicon ring resonator biosensor has been used for the first time to detect a biomarker (the cancer biomarker carcinoembryonic antigen) in the complex media of undiluted serum [85]. The same group used silicon ring resonators to detect single-nucleotide polymorphisms via kinetic DNA dissociation measurements [89]. They also used silicon ring resonators to simultaneously measure several protein biomarkers secreted from cells in cell culture media [82]. SOI ring resonator arrays with one output port that rely on wavelength division multiplexing have shown excellent sensitivity (0.3 pg/mm$^2$) monitoring multiple molecular-binding events [168].

Silicon nitride waveguides have also found applications in biomolecular detection [53]. Because silicon nitride is resistant to the diffusion of moisture and sodium ions, it can maintain a stable refractive index when operating in biological liquids. A packaged array of optical-slot-waveguide silicon-nitride ring-resonator sensors demonstrated high sensitivity of 0.9 pg/mm [174]. Another approach using slot-waveguide-based ring resonators on SOI demonstrated a refractive-index sensitivity of $2 \times 10^5$ RIU within a small footprint [122].

Microring resonators made of high index glass have been developed as a platform for detecting whole bacterial cells, proteins and nucleic acids [123]. Finally, ring resonators made from silicon nanowire optical waveguide (SNOW) have also shown promise for biosensing [175].

### 3.3. Liquid-core optical ring resonators

WGM resonances are also sensitive to biomolecules binding to the interior of thin-walled microcapillaries, and this is the basis for liquid-core optical ring resonator (LCORR) [56, 94, 176, 177]. The capillaries are fabricated by pulling the capillary while softening the glass with a CO$_2$ laser [56, 178]. The hollow-core cylindrical devices are easily integrated with microfluidics; indeed one of the main advantages of this approach is the ease of fluid handling as shown in Figure 3C. Theory and experiment put the protein detection capability of the LCORR in the sub-pg/mm$^2$ range [80]. LCORRs have been used in various sensing applications including the detection of DNA, viruses, proteins and biomarkers of cancer [80, 94, 179, 180]. Theoretical analysis shows that the thickness of capillary wall can be optimized to minimize or eliminate thermal drift, which could help stabilize the resonant modes in the presence of temperature fluctuations [181]. Recently a fluorescence based refractometric sensing was demonstrated in a glass capillary coated on the interior with fluorescent silicon nanocrystals [182].

LCORRs can be arranged in parallel on integrated waveguides to create a sensor arrays already integrated with microfluidics [183]. By positioning multiple waveguides along a single capillary, it is possible to interrogate the region of the capillary near each waveguide independently. This linear configuration is well suited to such applications such as capillary electrophoresis [184].

Although LCORRs have found diverse applications in biosensing, they have not yet demonstrated single particle/molecule resolution. Recent analysis has showed, however, that optofluidic ring resonators (OFRRs), which resemble LCORRs but which confine the WGM in three rather than two dimensions (by creating a bubble in capillary) are capable of detecting nanoparticles $<20$ nm in radius [185].

### 3.4. Toroids

Silica toroidal resonators are fabricated from layers of silica (glass) grown on crystalline silicon substrates by thermal oxidation. The silica is etched into discs with hydrofluoric acid, and the discs are then undercut with a xenon difluoride etch to form silica discs on silicon posts [186]. The disc are transformed into toroids (donuts) by heating the silica with a CO$_2$ laser, a self-terminating process. The modal volumes of toroidal resonators are smaller than those of microspheres of comparable diameter, and the resonators also have ultrahigh Q factors [186] because of the almost atomically smooth surface produced by reflowing glass. Thus, the toroid geometry boasts a sensitivity comparable to that of the microsphere and is a good candidate for achieving single molecule detection [30, 66, 67, 70, 81]. Toroids could potentially be produced in arrays like those described for disks and rings. However, integrating the resonators with waveguides or optical fibers requires secondary fabrication steps and remains a challenge.
This challenge may be addressed by avoiding the secondary fabrication step yet obtaining high-Q microcavities of up to 875 million for on-chip applications, for diameters larger than 500 μm [187]. Toroids are increasingly used in biosensor demonstrations [16, 65, 102, 112].

Researchers have recently used microcavity ring down spectroscopy to track the $Q$ factor and wavelength shift during a biodetection event in order to make the resonator less susceptible to noise [98]. Computational schemes can also be employed to calculate the toroid response to detection events in order to achieve higher sensitivities [81].

An interesting variant of the toroidal microcavity is the goblet resonator, made of a thermoplastic polymer that assumes a cupped shape on refloowing [188]. Finally, another modification of the fabrication scheme produces high-Q toroids with beveled edges, called wedge resonators [187].

### 3.5. Fluorescent beads, capillaries and tubes

Mie resonances in microspheres or capillaries doped with fluorescent dyes can be identified by epifluorescence microscopy and spectroscopy. These are lower-Q sensors, but they still provide a reasonably small modal volume for biosensing [101, 189, 190]. Fluorescent beads a few μm in diameter are capable of detecting proteins [126, 127, 191, 192]. They can also be used to detect the forces during endocytosis because microbead deformation induces azimuthal mode splitting [128]. In addition, a new detection scheme using clusters of fluorescent microsensors was introduced recently [191]. Each clusters of microresonators has a specific WGM spectrum that serves as its “fingerprint” and would allow clusters on a chip to be read out properly without knowing their exact locations.

Another recent innovation is the use of flexible split-wall fluorescent microtube resonator sensors to detect mouse fibroblast cells [133]. The same authors then discussed the integration of this device with others to constitute a lab-on-a-tube [193]. Quantum dots embedded in polystyrene microspheres can also serve as fluorescent sensors; the wavelengths of their resonant modes shifts as the bulk index of refraction is changed in ethanol-water mixtures [194]. Another approach combines fluorescence imaging with WGM resonators for multiplexed detection of biomolecules [49].

### 3.6. Other resonator geometries: coils, bubbles and photonic crystals

Optical fiber nanowires can be coiled-up to form microcoil resonators where a microfluidic channel runs through the inside of the coil for biosensing applications [144–146]. Recently a novel refractometric sensor based on a coated all-coupling optical-fiber-nanowire microcoil resonator with device sensitivity as high as 700 nm/RIU was reported [146, 195]. An entire review is dedicated to the subject of microcoil resonators and we refer the interested reader to [144]. Also, controlling the melting of a capillary microbubble resonator has been shown to have potential in biosensing by filling the bubble with analyte solution [141–143]. Another fiber-based high-Q cavity with potential applications in biosensing is the bottleneck resonator fabricated by melting a standard single mode fiber [132].

A very promising planar platform for biosensing applications is based on two-dimensional silicon photonic crystals where light can be confined by Bragg reflection and within the photonic bandgap [115, 116, 196, 197]. Photonic crystal cavities can offer ultra-low modal volumes combined with high-Q factors which continue to improve as the design files and the nanofabrication recipes advance [198, 199]. The highest sensitivity for detection with a Q~9300 photonic crystal microcavity has recently been demonstrated at mass loading sensitivity of 0.8 pg/mm², and with a concentration of only 0.1 μg/ml protein in the pico-molar range [106]. Also recently, a one-dimensional photonic crystal resonator array was introduced for significantly enhancing the light-matter interaction. It was shown that spatially localized optical fields down to mode volumes of a wavelength cubed improve the detection limits of previous designs [115].

Extended photonic crystal membranes without cavities have also been proposed as biosensing elements for detecting particles by “dark field” imaging [200]. In another fundamental study it has been shown that by disordering of the photonic crystal lattice, very high-Q cavities with various modal volumes can be introduced, for example along the length of a photonic crystal waveguide [201]. The random cavities can be potentially used in multiplexed detection and are more easily to fabricate as compared to highly-engineered defect cavities.

We also note that photonic crystal structures that effectively form 1D gratings have been used extensively in biosensing [135]. Because of the low Q, large modal volume and resulting lower sensitivity for detecting a limited number of molecules, such reflectivity filters fall outside the scope of this review and we refer the reader to [202, 203].

### 4. Active resonators for sensing enhancement

A narrow resonance can help to resolve a small resonant shift caused by trace amount of molecules attached to the resonator, which could have been missed by a broad resonance. The resonance linewidth of a passive optical resonator, i.e., a resonator without optical gain, is affected by fabrication process, geometry, materials absorption, radiation loss and scattering loss of the resonator. Appropriate design and optimization of the fabrication process could help increase the passive $Q$-factor, and therefore decrease the linewidth, by minimizing the radiation and scattering induced loss, but the loss from materials absorption will set the limit of the $Q$-factor, i.e., the linewidth, for a passive resonator. However, in an active optical resonator, i.e., a resonator with optical gain, where the loss can be compensated by the gain medium, the effective loss felt by the photon is decreased dramatically, which will increase the effective $Q$-factor, subsequently decrease the linewidth, and hence improve the sensitivity and detection limit.

The active resonator can operate in either below-threshold and above-threshold regime; in both cases, the detection limit
and resolution is significantly improved. The above-threshold regime, also termed as lasing region, in particular, is very attractive for detection purposes since the lasing line usually has much narrower linewidth than the resonance linewidth of the cold cavity (i.e., the gain medium is not pumped). According to Schawlow-Townes formula, the fundamental linewidth of a lasing mode in a resonator is

$$\Delta \nu_{\text{laser}} = \frac{\pi \hbar \nu (\Delta \nu_{\text{cold}})^2}{P_{\text{laser}}}$$  (13)

where $\Delta \nu_{\text{cold}}$ is the resonance linewidth calculated from “cold” cavity Q factor $P_{\text{laser}}$ is the power of the lasing mode and $\nu$ is the resonant frequency. For an active resonator with cold Q-factor of $10^8$ and lasing wavelength wavelength at 1550 nm, the laser linewidth is at the Hertz level, which is almost six orders of magnitude narrower than the cold resonance linewidth of 2 MHz. In principle, it suggests that the microcavity laser as a sensing element could provide a much lower detection limit than its passive counterpart.

The sensing performance of the reactive shift method can be enhanced through optical gain by improving the minimum detectable resonant shift (Figure 8). Active WGM resonators have been proposed to enhance the sensitivity in spectral shift technique. With gain medium doped polymer microspheres it is possible to detect effective refractive index change of the order of $10^8$ RIU [129]. Nile red has been used to improve Q factors of polystyrene microspheres to enhance the sensitivity in both the spontaneous (i.e., below threshold) and stimulated emission (i.e., above threshold) regimes. The active microspheres have demonstrated eight-fold SNR improvement and three-fold Q enhancement which helps monitor the real-time adsorption kinetics of bovine serum albumin in phosphate buffered saline (PBS) [126]. Active microspheres doped with quantum dots have been used for biosensing with the minimum detection limit of 260 pg/mm² for a minimum detectable mass of ~80 fg protein [194] and the minimum detectable refractive index change of $2.5 \times 10^4$ RIU [204]. Using tetramethylrhodamine as gain medium, active silica microspheres were also demonstrated to achieve detection of oligonucleotides [93]. Recently a new active sensor composed of a ring laser and an optofluidic tube has achieved sensitivity of 5930 nm/RIU, which is around one order of magnitude higher than what has been demonstrated by a sensor based on passive ring resonator [205]. Microcavity in liquid form is naturally compatible for sensing in solution. It has been shown that millimolar of surfactant can be detected by measuring the lasing spectrum of a liquid-crystal droplet in water [206]. Also other structures, such as gratings and photonic crystals have been utilized recently in active cavity sensing [207].

Optical gain also improves the sensitivity and detection limit of mode splitting by decreasing the resonance linewidth which help resolve the two split modes which could have otherwise appeared as one broad resonance in the spectrum. For example, Figure 9 shows that gain medium helps decrease the resonance linewidth and reveal the mode splitting, which would otherwise remain unresolved without narrowing the linewidth using optical gain. A new self-heterodyne measurement of mode-splitting signals for nanoparticle and biomolecule detection has been demonstrated by operating the active resonator in lasing regime [66]. When a nanoparticle enters the mode volume of an active resonator pumped above lasing threshold, the single lasing mode splits into two, which generate a heterodyne beat note signal when mixed in a photo-receiver. The heterodyne beat note signals carry the information of mode splitting and vary with time as particles or molecules enter the resonant mode consecutively. Since the lasing mode has a linewidth much narrower than a passive mode by several orders of magnitude, it could resolve smaller mode-splitting. Moreover, in contrast to a passive resonator in which only one mode is monitored at one time, multiple lasing modes can be utilized simultaneously in an active resonator to achieve multi-wavelength sensing with single-wavelength pump. Thus, it relieves the requirement on laser source with multiple wavelengths to achieve multi-wavelength sensing. Moreover, in resonators with multiple lasing modes, one of the modes can capture an event (e.g., change in heterodyne beat frequency due to a binding particle) which is missed by the other one(s). This shows that multi-mode sensing not only provides extra information obtained at different wavelength but also improves the sensing response of the resonator since different modes cover different areas of the devices.

5. Enhancement mechanisms by localizing the resonant light field

5.1. Plasmon enhancements

An entirely new approach to enhancing the sensitivity of WGM biosensors utilizes the fact that the frequency shift
signal produced by a protein or nanoparticle binding to the microcavity is in proportion to the intensity $\sim E^2(r_0)$ encountered at the binding site $r_0$ [147], see Eq (2). Any mechanism that can amplify the field intensity at the binding site while maintaining high $Q$ factor will therefore produce a boost in the frequency shift signal, dramatically increasing the sensitivity in single molecule detection. Hot spots of high field intensities can be generated by evanescent coupling of the microcavity resonance to a plasmonic nanoantenna, Figure 10. WGM evanescent excitation of plasmon resonances, for example in a gold nanoparticle, can produce very large field enhancements. Many nanoantenna geometries can be explored for this purpose and their designs are similar to nanostructures that are investigated in surface enhanced Raman spectroscopy (SERS) [208]. Examples for nanoantennas commonly investigated in SERS are nanoparticle or nanoshell dimers [209] and bowtie antennas [210]. Different from SERS, which seeks to enhance the far-field scattering signal, WGM biosensing relies entirely on enhancing the near-field intensity. In fact it is necessary to minimize the scattering loss to maintain high-Q factor which is required for sensitive biomolecular detection. Through careful choice of WGM wavelength it is indeed possible to enhance the near field intensity at the nanoantenna site while minimizing scattering loss. Simulations, theory and experiments indicate that by detuning the microcavity resonance from the plasmon resonance an overall boost in sensitivity by several orders of magnitude is attainable [147, 148, 211, 212]. Indeed, first experimental reports indicate such dramatic sensitivity enhancements [108, 147–149].

The first demonstrations of this plasmon-enhanced microcavity detection scheme utilized a random nanoparticle layer to generate hot spots of high field intensity after coupling to a WGM microsphere cavity [147, 148]. High near-field enhancements were obtained by excitation of a WGM at optimal wavelength. It can be shown that the optimal WGM resonance wavelength is close to the plasmon resonance but significantly detuned from it to limit scattering loss. In theory, optimized plasmon coupling can produce near field enhancements up to three orders in magnitude, increasing the frequency shift signal for detecting a protein molecule and
brought label-free single molecule detection within reach [58, 213]. For example, a nanorod immobilized on a microtoroid will boost the frequency shift signal obtained for binding of a single BSA molecule into the MHz-range, which is more than an order of magnitude larger than the expected measurement noise [58]. Other demonstrations for plasmon enhanced frequency shifts have utilized plasmon nanoshells optically trapped with the WGM and delivered towards another gold nanoparticle for several-fold more sensitive detection of the nanoshell [149]. Recently it has also been shown that sensitivity for virus detection can be enhanced with a plasmon-coupled microcavity [108].

The large near field enhancements in a random nanoparticle layer were proposed to be capable of also optically trapping single protein molecules, producing femto-molar sensitivity levels in μl-scale sample volumes [148]. In other demonstrations, the high field strengths of WGMs [214, 215] as well as WGMs coupled to nanoparticles were used to enhance the far-field SERS scattering signal [216], without any utility in boosting the actual WGM frequency shift signal, however. Furthermore, enhanced evanescent coupling to a WGM with the help of a plasmonic nanoparticle has been reported [217]. Interestingly, hybrid photonic plasmonic microcavity structures promise ultra high sensitivity not only in biosensing but also in cavity-QED experiments [213].

It should be noted that microcavities have also been used for the excitation of surface plasmon polaritons (SPP) in a continuous metal film coated on a micodisc-shaped cavity [218]. Such high-Q SPP-WGM has also been predicted in a metal coated WGM resonator [219]. Here, an exterior surface mode possesses high quality factors at room temperature, and can be efficiently excited by a tapered fiber. Furthermore, metal films have been shown to enhance prism-based coupling to WGMs [220]. It was also shown theoretically that a nanosized scatterer immobilized on the microresonator surface enables the efficient coupling to WGMs from a free space beam [221]. Another configuration for realizing hybrid photonic plasmonic microcavities are microring silicon resonators optically coupled to a metal microdisk located inside the ring. Here, optical energy is greatly concentrated in the narrow gap between the metal and the silicon ring [222]. Also a microring resonator with a metal strip has been shown to efficiently couple to a plasmonic nanostrip [223].

5.2. Other enhancement mechanisms based on field confinement

Other non-plasmonic enhancements of microcavity biosensing rely for example on confining light in dielectric slotted ring resonators [224] and slotted photonic crystals where high field amplitudes at the slot are accessible for molecules. Slotted photonic crystal cavities were for example used to detect bound molecules at low surface mass densities [197]. Also, slotted ring resonators have been utilized for improved detection limits, for example within a 100 nm slot [122]. In a packaged slot-waveguide ring resonator sensor array, a surface mass density detection limit down to 0.9 pg/mm² has been demonstrated [174]. Enhanced sensitivity of a spherical microcavity biosensor was demonstrated by confining the
WGM near the surface using a subwavelength high refractive index coating [152].

Multiple-hole defects have been used to improve the sensitivity in silicon slab photonic crystal cavities [196] by increasing the surface area available for label-free detection without degrading the quality factor. Compared to photonic crystals with L3 defects, adding multiple hole defects into photonic crystal cavities enabled a 44% increase in detection sensitivity. Refractive index sensitivity of guided resonances in photonic crystal slabs could be enhanced by three-fold for suspended slab designs, in contrast to designs with a slab resting over a substrate. Spectral sensitivity values are additionally shown to be unaffected by quality factor reductions, which are common to fabricated photonic crystal nanostructures [225].

A cluster of evanescently coupled 2D WGM optical microcavities (termed “photonic molecules”) were introduced for biosensing with enhanced sensitivity [211]. Here, photonic molecules supporting modes with narrow linewidths and wide mode spacing show enhanced sensitivity to the changes in the dielectric constant of their environment and to the presence of individual subwavelength-sized nano-particles in the evanescent-field region.

6. Optical manipulation for biosensing

WGM resonators exhibit strong evanescent field gradients which can be used for trapping of nanoparticles by optical forces. Using light to apply force has applications in biosensing for accurately determining the size of a trapped particle, extracting information about the particle-to-surface interaction and for speeding up detection by breaking diffusion limits [32]. For example, nanoparticles that diffuse within the reach of the evanescent field of the microsphere resonator are pulled towards the sensor surface by optical gradient forces similar to those in optical tweezers. The nanoparticles are drawn towards the equatorial region of the microsphere where the evanescent field intensity is maximal and where they tend to accumulate at the sensor surface. In the case of a low affinity or a low density of binding sites the nanoparticles do not bind but instead remain trapped within the evanescent field and are now propelled around the microsphere resonator. The driving force for this orbital motion is the absorption and scattering of light. While trapped, the nanoparticle visits the sensor surface many times due to Brownian motion during its circumnavigation. As a result, binding is essentially assured once trapped and this mechanism can be used to considerably speed up the binding rate at extremely low concentrations [32]. Furthermore by recording the resonance wavelength fluctuations of the trapped nanoparticle it is possible to accurately determine the trapping potential and the forces that arise at the sensor surface (Figure 11). Similar to an atomic force microscope (afm), the random tapping of an optically trapped nanoparticle (in afm: controlled tapping by a nanotip) is thus used to measure forces acting on the nanoparticle at the sensor interface [32]. The interaction between a trapped nanoparticle and a WGM can be complex due to modification of the WGM field with position of the nanoparticle [158].

Building up on these works, it has been shown recently that plasmon enhancements in WGM coupled nanoparticles can provide trapping potentials strong enough for trapping protein molecules at the sites of highest sensitivity [148].

In other examples, effective trapping of 500 nm-diameter polystyrene beads at mW coupled power level was achieved with micron-sized silicon ring resonators propelling the particles along the resonator with velocities of up to 100 μm/s [226]. Moreover particle can be routed on and off the resonating structures with applications in developing all optical microintegrated particle switches and add drop devices [29, 227], see Figure 11.

In another report, direct measurement of the biomechanical stress induced by a live cell during endocytosis of a microcavity is reported [128]. Fluorescent dye-doped polystyrene microspheres were used as microscopic remote optical sensors applying WGMs as transducer mechanism. Monitoring of the WGMs throughout the incorporation of the microsphere into the cell enabled the determination of the deformation experienced by the microsphere.

Very recently, a photonic crystal microcavity was developed as “nanotweezer” that can trap and release on-command Wilson disease proteins, quantum dots, and 22 nm polymer particles with a temperature rise less than similar to 0.3 K, which is below the point where unwanted fluid mechanical effects will prevent trapping or damage biological targets [228].

7. Discussions and outlook

In this article we have reviewed the state-of-the-art sensing schemes using optical resonator for ultra-sensitive detection of molecules, viruses, and particles. Although still in the early stage of research and development, optical resonators may become very useful for many applications ranging from early disease diagnostics, environmental monitoring and pharmaceutical analysis. Thanks for the effort devoted to this emerging area, high-Q resonators have shown promise for commercialization with the superior sensitivity of single particle/molecule/virus detection. To further enhance the sensing performance of optical resonators, different enhancement mechanisms, such as plasmonic effect and active gain medium, have been pursued; detection of single virus and nanoparticle has been demonstrated. One of the other key issues to push such a promising sensing platform closer to application is the sample collection. An effective way to deliver trace amounts of samples to the proximity of the miniature resonator in various environments is of great importance to reduce the detection time and utilize the unprecedented sensing capability provided by the device. Integrating the resonators with appropriately designed fluidic channels or digital microfluidics [229] will become important in this respect. It is also possible to resolve such an issue by combining super-hydrophobic artificial structure, which can help drive and concentrate molecules over a sensing area in nano-scale, in the design of resonator based sensing system. Specifically the super-hydrophobic substrate enables low
adhesion forces between the solution and surface, forcing the solution drop to slide on the surface. With appropriate design of the system, the resonator could be set in a position where ultimately the solution with molecules will concentrate on and precipitate after evaporation; subsequently, trace amount of molecules can be detected by the microresonator [230].

In order to achieve selective sensing, various surface functionalization techniques have been developed and used in optical resonators. Sometimes, the degradation of the $Q$-factor resulting from the surface functionlization process deteriorates the sensitivity of the resonators. An effective method to recover the $Q$-factor using active gain medium could be one of the options to maintain the sensing performance provided by the high-$Q$ micro-resonators.

The limit of detection for a microcavity biosensor is also governed, in part, by the accuracy of the surface chemistry, i.e., the number of accessible binding sites. Ideally, the number of binding sites should be determined by using the sensor itself to monitor the functionalization procedure. We anticipate that future studies will use such and other calibration approaches to provide further insight into the chemical aspects of biodetection, especially when performed in complex samples such as serum or lysate [54].

As a self-referencing sensing scheme recently demonstrated for detection and measurement of individual nanoparticles and virions, mode-splitting method provides new capabilities, such as single-shot size measurement of individual nanoparticles, which has not been reported for single-resonance shift based sensing method following reactive sensing principle. There has been ongoing debate on mode splitting and reactive sensing principle referring to their advantages and the conditions under which one is favored over the other one. More investigation could be done to develop guideline making use of full advantages provided by optical resonators for future studies and applications.

Until now most optical resonators utilized for sensing applications are usually fabricated from silica or silicon. Investigating WGM resonators made from other materials could benefit the sensing field. For example, the small index contrast between silica (~1.46) and water (~1.33) increase the radiation loss of the resonators in aqueous environment and makes it challenging to achieve high-$Q$ which is critical to maintain the ultra-high sensitivity. One remedy is to...
increase the size of the resonator, which, however, increases the volume of the optical mode and decreases the sensitivity. Replacing silica with some high refractive-index materials will help achieve high-Q resonators with small size. In this respect, the engineering of planar photonic crystal cavities in silicon or silicon-nitrate material systems will become more and more prevalent as fabrication tools and protocols for making high Q/V cavities become more pervasive. In the future one may even see 3D photonic crystal cavities [231] (or 2D disordered photonic crystals [201, 232]) that localize light in ultra-high Q/V resonators for biosensing applications.

Moreover, integrating WGM resonator with other existing technique, such as microfluidic platforms and silicon photonics will provide more advance functionalities for biosensing. In contrast to conventional enzyme-linked-immunosorbsent assays (ELISAs), a sensing technique relying on labeling and often fluorescent readout by imaging, the emerging WGM resonators have been approved as a simple, ultra-sensitive and stand-alone sensing platform without request for external labeling and imaging systems. The diversity of the designs of WGM resonators has made it possible to tailor the geometries of the sensors for different applications. The developments of WGM resonators have paved the way for label-free detection at the single molecule level with the potential to replace or complement other existing sensing platforms. A very important task of any integrated microfluidics platform will be the rejection of noise due to temperature and refractive index fluctuations. Here, differential measurements for example within the same microcavity might be a solution.

The combination of plasmonic nanoantennas with the local density of states provided in microcavities promise novel physics that will guide the development of a highly sensitive approach [10]. In particular, we believe that hybrid photonic-plasmonic microcavities will provide the ability to observe and manipulate single biomolecules in real-time. This will enable groundbreaking experiments in the life sciences, allowing studies on the mechanisms of molecular machines. We also believe that hybrid photonic-plasmonic biosensor systems based on random nanoparticle assemblies [148] will be used to study more complex biological reactions such as DNA transcription and protein translation reactions. Using a random approach for such assays guarantees signal read-out where otherwise matching a single nanoantenna with a complex biological reaction might be difficult to achieve. Ultimately we envision the use of molecular machines such as DNA polymerases or Ribosomes in photonic-plasmonic devices that sequence or even manufacture DNA and protein molecules. The high field intensities at the site of a nanoantenna coupled to a microcavity can further enable the observation of non-linear effects in biomaterials. It is also conceivable that mechanical resonances in biological structures could be probed with plasmon-coupled microcavities given their superior sensitivity.

In clinical diagnostics, the integration of photonic-plasmonic optical resonators on microchips will enable the next-generation label-free biosensors envisioned in the introduction of this article. By exploring various resonator geometries in combination with free space coupling, we foresee many applications including the monitoring of live cells and engineered tissue [233].

We also anticipate that light field and temperature gradients of plasmon-coupled microcavities will enable technologies to control flow fields in lab-on-chip devices and manipulate analyte molecules [234, 235]. We also believe that new materials such as graphene will find applications in plasmon-enhanced detection. In the future we also predict that not only antibody-antigen reactions will be used for molecular detection. Instead, complete networks of interacting molecules will be designed to produce specific pathways that mimic the specificity and sensitivity of the cell. The output of such networks will be monitored with microcavities, implementing various cellular functions on chip-scale devices [236].

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