Flow Characteristic and Heat Transfer for Non-Newtonian Nanofluid in Rectangular Microchannels with Teardrop Dimples/Protrusions

Zheyuan Zhang, Yonghui Xie*, Di Zhang, and Gongnan Xie

DOI 10.1515/phys-2017-0021
Received July 29, 2016; accepted October 31, 2016

Abstract: Porous cavity technology is one of the effective ways to improve local flow structures and thus the overall heat transfer of heat exchanging devices. In the present investigation, the flow characteristics and heat transfer in a microchannel heat sink with teardrop dimples/protrusions are studied with a numerical method. The working substances are Al2O3-water nanofluids, which are defined by power-law shear-thinning model. The relative depth and positive eccentricity of dimples/protrusions arranged in the microchannels are 0.2 and 0.3 respectively. The inlet velocity varies in the range of 1.41 m·s⁻¹ to 8.69 m·s⁻¹ and the volume fraction ranges from 0.5% to 3.5%. The effects of the flow and heat transfer characteristics are investigated by analyzing the limiting streamlines structures and temperature distributions. The overall thermal performance is evaluated by parameters of Fanning friction factor, Nusselt number and thermal performance. It is shown that the combination of teardrop dimple/protrusion structure and Al2O3-water nanofluids could effectively strengthen heat transfer with low pressure loss. Moreover, in order to obtain the best overall thermal performance, working substances with volume fraction of 3.5% is preferred for the proposed microchannel structure.

Keywords: Microchannel heat sink; Nanofluids; Flow characteristics; Heat transfer; Teardrop dimple/protrusion

1 Introduction

In some industries, a normal cavity can be replaced by a novel porous cavity to achieve better overall thermal performance. With the development of high efficiency compact heat exchanger devices, traditional heat transfer enhancement techniques no longer adapt to the requirement of larger heat flux. For this reason, the heat transfer method by means of working fluids innovation is proposed recently [1].

With the advantage of high thermal conductivity and considerable improvement of forced convective heat transfer, nanofluids are playing a significant role in heat exchanging systems, which has led to several recent research into the flow of nanofluids in porous media. By using a mathematical model, Sheremet [2] investigated the heat transfer characteristics of the steady natural convection in a kind of enclosed porous space filled with nanofluids. It was found that the local Nusselt number at the interface of solid wall and porous medium is directly related to five key parameters. The Finite Difference Lattice Boltzmann Method was first used to conduct the research of heat transfer and entropy behavior by Kefayati et al. [3]. This work simulated the natural convection of non-Newtonian laminar flow in a square-shaped porous cavity. Besides, the heat transfer of nanofluids, which is in a square cavity filled with porous media, is studied by Bourantas et al. [4] using a kind of meshless technique. He also investigated the effect of the porous medium on the nanofluid cooling efficiency. Sheremet and Pop [5] used numerical simulation to study the transient natural con-
vection of a nanofluid in a wavy-shaped cavity with porous media. Rashidi et al. [6] conducted a theoretical study on the thermo convective boundary layer for a kind of viscoelastic power-law non-Newtonian fluid flowing over a porous wedge.

Meanwhile, the heat transfer and flow characteristics of non-Newtonian nanofluids has attracted many researchers in other fields. Singh and Harikrishna [7] combined three concentrations of alumina nanofluids and two microchannels to investigate the heat transfer behavior. The laminar convective thermal characteristics of an alumina-water solution, as a typical nanofluid, was researched by Kalteh et al. [8] numerically and experimentally. In his research, a kind of rectangular microchannel were studied with experimental and numerical methods by Lee [16].

Coelastic power-law non-Newtonian fluid flowing over a porous wedge. The thermo convective boundary layer for a kind of viscoelastic power-law non-Newtonian fluid flowing over a porous wedge. The laminar convective thermal characteristics of an alumina-water solution, as a typical nanofluid, was researched by Kalteh et al. [8] numerically and experimentally. In his research, a kind of rectangular microchannel were studied with experimental and numerical methods by Lee [16].

According to the literature review given above, teardrop dimples/protrusions and non-Newtonian nanofluids both have the potential to obtain better thermal performance. In the present research, a numerical investigation is carried out to analyze the flow characteristics and heat transfer of Al₂O₃-water (AW) nanofluids in teardrop dimpled and protrusioned passages for the purpose of observing the thermal performance of non-Newtonian fluids flowing in microchannels.

2 Physical properties of non-Newtonian fluid

The thermal physical properties of nanoparticles (Al₂O₃) and base fluid (H₂O) as are given in Table 1.

<table>
<thead>
<tr>
<th>Property</th>
<th>Al₂O₃</th>
<th>H₂O</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific Heat Cₚ(J·Kg⁻¹·K⁻¹)</td>
<td>765</td>
<td>4179</td>
</tr>
<tr>
<td>Density ρ (kg·m⁻³)</td>
<td>3870</td>
<td>997.1</td>
</tr>
<tr>
<td>Thermal Conductivity λ (W·m⁻¹·K⁻¹)</td>
<td>40</td>
<td>0.6</td>
</tr>
</tbody>
</table>

The specific heat and density of nanofluids are calculated by the equations as follows [20]:

\[ ρ_{nf} = (1 - ϕ)ρ_f + ϕρ_p \]  
\[ C_{pf} = (1 - ϕ)C_{pf} + ϕC_{pp} \]

where \( ϕ \), \( ρ \) and \( C \) represent volume fraction, density and specific heat capacity, respectively. The subscripts 'p', 'f' and 'nf' indicate nanoparticles, base fluids and nanofluids respectively. Equation (3) has been adopted to determine the effective thermal conductivity of aqueous solutions with spherical nanoparticles [20].

\[ λ = λ_f \left[ \frac{λ_p + 2λ_f}{λ_p + 2λ_f + 2ϕ(λ_f - λ_p)} \right] \]

where \( λ_f \) and \( λ_p \) represent thermal conductivity of the base fluid and nanoparticles, respectively. The non-Newtonian power-law model is described by

\[ \tau = kγ^n \]

where \( τ \), \( γ \), \( n \) and \( k \) are the shear stress, shear rate, behavior index and consistency index of power-law fluids, respectively.

Based on the data and equations stated above, the corresponding thermal physical properties of Al₂O₃ aqueous solution with different volume fraction are shown in Table 2. Besides, the shear-thinning model has been used to
define the viscosity of this kind of nanofluid [10] and details are shown in Table 2.

3 Physical model and numerical method

3.1 Geometrical configuration and boundary conditions

The 3D geometrical model of microchannel heat sink and its flow domain with teardrop dimples are shown in Fig. 1. The width and height of the microchannel are 200 µm and 50 µm respectively. Dimples/protrusions are distributed in an aligned arrangement on the lateral side, the width of which is 200 µm. The teardrop dimples/protrusions with positive eccentricity are chosen as the flowing controlling structures, because these cases have the better thermal performance according to the previous studies. Thus teardrop dimple and protrusion structures with relative depth of δ/D_h = 0.2 and positive eccentricity of e/D_h = 0.3 are chosen to be the simulation model in the present study. The brief description for the dimple and protrusion structure is shown in Fig. 2.

3.2 Data reduction

The hydraulic diameter is defined by

\[ D_h = \frac{2WH}{W + H} \]  

(5)
Table 2: Physical properties of Al₂O₃-Water nanofluids.

<table>
<thead>
<tr>
<th>φ, %</th>
<th>Cₚ (J·kg⁻¹·K⁻¹)</th>
<th>ρ (kg·m⁻³)</th>
<th>λ (W·m⁻¹·K⁻¹)</th>
<th>k (Pa·s⁻¹)</th>
<th>n</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>4161.93</td>
<td>1011.97</td>
<td>0.61</td>
<td>0.00187</td>
<td>0.88</td>
</tr>
<tr>
<td>1.5</td>
<td>4127.79</td>
<td>1041.69</td>
<td>0.63</td>
<td>0.00283</td>
<td>0.78</td>
</tr>
<tr>
<td>2.5</td>
<td>4093.65</td>
<td>1071.42</td>
<td>0.64</td>
<td>0.00426</td>
<td>0.68</td>
</tr>
<tr>
<td>3.5</td>
<td>4059.51</td>
<td>1101.15</td>
<td>0.66</td>
<td>0.00641</td>
<td>0.58</td>
</tr>
<tr>
<td>4.5</td>
<td>4025.37</td>
<td>1130.88</td>
<td>0.68</td>
<td>0.00876</td>
<td>0.50</td>
</tr>
</tbody>
</table>

Figure 3: Boundary condition of the computation unit.

where $W$ and $H$ represents the width and height of cross section of microchannel respectively. The Reynolds number of non-Newtonian fluids is defined as [21]

$$Re = \frac{D_h U_{in}^{2-n} \rho}{k}$$

where $\rho$ and $U_{in}$ are the density and inlet average velocity respectively.

The average Nusselt number of the wall is determined by:

$$Nu = \frac{q}{\Delta T} \cdot \frac{D_h}{\lambda}$$

where $\lambda$ represents the thermal conductivity, $\Delta T$ is the average temperature difference between fluid and wall, which is defined by the following equation [22]:

$$\Delta T = \frac{(T_{w,inlet} - T_{f,inlet}) - (T_{w,outlet} - T_{f,outlet})}{\ln [(T_{w,inlet} - T_{f,inlet})/(T_{w,outlet} - T_{f,outlet})]}$$

where the subscripts ‘w’ and ‘f’ represent wall and fluid respectively. According to the former literature, the Fanning friction factor, which is determined by eq. (9), can be used to describe the degree of pressure loss.

$$f = \frac{(\Delta p/L)D_h}{2\rho U_{in}^2}$$

where $\Delta p$ is the average difference between inlet pressure and outlet pressure. The thermal performance, which is proposed to evaluate the overall effect of heat transfer, is defined by:

$$TP = \left( \frac{Nu}{Nu_0} \right) \cdot \left( \frac{f}{f_0} \right)^{-1/3}$$

where the subscript ‘0’ represents the corresponding parameters of water flowing in the smooth microchannel cases with the same boundary condition.
3.3 Governing equations

The simplified three-dimensional Navier-Stokes equations are solved to characterize the details of flow and heat transfer. The simulations are conducted by using the commercial software FLUENT. It could be obtained that the maximum Reynolds number of the cases studied is less than 450, by using the physical properties and equations above. According to the assumption above, the cases investigated are steady-state laminar flow, of which the governing equations can be simplified as follows [22].

\[
\frac{\partial \rho}{\partial t} + \frac{\partial \rho u_i}{\partial x_i} = 0 \tag{11}
\]

\[
\frac{\partial \rho u_i}{\partial t} + \frac{\partial \rho u_i u_j}{\partial x_j} = \rho g_i + F_i - \frac{\partial \rho}{\partial x_i} + \frac{\partial}{\partial x_i}(2\mu S_{ij}) \tag{12}
\]

\[
\frac{\partial \rho E_0}{\partial t} + \frac{\partial \rho u_i E_0}{\partial x_i} = \rho u_i F_i - \frac{\partial q_i}{\partial x_i} + \frac{\partial}{\partial x_i}(u T_i) \tag{13}
\]

where \( t, x, u, g \) and \( P \) are time, coordinate, velocity, gravity acceleration and pressure, respectively. \( F, T, E_0 \) and \( S \) are body force, surface force, total internal energy and strain rate tensor. \( i, j = 1,2,3 \).

3.4 Grid independence validation

The grid independence validation is conducted using the AW0.5 solution flowing at the boundary conditions of \( U_{in} = 1.41 \text{ m·s}^{-1}, T_{in} = 300 \text{ K} \) and \( q = 5 \times 10^5 \text{ W·m}^{-2} \). Four different sets of grids are applied and the detailed comparison between given sets is shown in Table 3.

The relative discrepancies of \( Nu \) and \( f \) decrease gradually with the increase of nodes. It is shown that the discrepancies are small enough in the case of mesh 3. So mesh 3 is selected in the present investigation.

3.5 Numerical method validation

In order to verify the numerical method, the data reported in the literature [17] is regarded as the reference. The flow and heat transfer in the corresponding smooth microchannel is simulated by the numerical procedure applied in the investigation. In the validation, a kind of shear-thinning fluid with \( n = 1, k = 10^{-3} \text{ Pa·s}^{-2} \) is chosen as the working substance. The rectangular microchannel scaled 200 \( \mu \text{m} \times 50 \mu \text{m} \times 150 \mu \text{m} \) is selected to be the computational domain. The boundary condition of \( q = 5 \times 10^5 \text{ W·m}^{-2} \) and \( T_{in} = 300 \text{ K} \) is applied and the average inlet velocity varies from 1.41 m·s\(^{-1}\) to 8.69 m·s\(^{-1}\).

Table 4 shows the comparison of the \( Nu \) and \( f/Re \) between referenced and proposed model. The maximum deviation is 0.88% for \( Nu \) and 0.92% for \( f/Re \) respectively, which shows the proposed model is feasible for the simulations in the present investigation.

4 Results and discussions

4.1 Flow characteristics

The limiting streamline distribution and temperature contours on the teardrop dimpled and protrusioned surface for AW0.5 nanofluids are presented in Fig. 5 and Fig. 6. For dimpled structures, the narrow leading edge makes streamline distorted at the front region. Under the effect of pressure gradient, a part of fluids deviates from the mainstream direction and impinging directly onto the trailing section of the teardrop dimple and then reverses. This part of fluids interacts with the mainflow at the core zones of teardrop structure, which leads to the relatively low pressure and a large backward vortex. It can be seen that there is apparent mass exchange and heat transfer. It should be noticed that when \( U_{in} = 1.41 \text{ m·s}^{-1} \), the reverse point of limiting streamline is not at the rear edge of dimple, mainly because the effect of low pressure is bigger than that of mainflow inertia inside the dimple and the reverse point moves down. With the increase of the velocity, the radian of the flow separation line increase gradually. As shown in the case of \( U_{in} = 8.69 \text{ m·s}^{-1} \), the area of the vortex zone is almost as big as the teardrop dimple and the radian of the separation line is large enough to distort the streamline around the rear section. The limiting streamline distribution basically keeps symmetrical in all cases. It is shown that the temperature of flow impinging zones and the trailing section is apparently lower than that of flow separation zones.

As seen from the figures, the working substance moving through the teardrop protrusion region shows symmetrical fusiform flow structure. At the leading edge, the flow moves along the teardrop protrusion surface and the velocity of nanofluids increases gradually because of the area decrease at cross section. As shown in Fig. 6, there is apparent vortex and flow separation at the trailing edge and the size of vortex zone becomes bigger as the velocity increases. As seen from the contours, the temperature at the back region of the protrusion structure is a little bit higher, which indicates that the flow separation weakens the heat transfer and mass exchange. As the velocity increases, the influence from backflow to mainflow grows bigger, which
Table 3: Grid independence validation.

<table>
<thead>
<tr>
<th>Mesh</th>
<th>Nodes</th>
<th>Nu</th>
<th>Difference,%</th>
<th>f</th>
<th>Difference,%</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>792792</td>
<td>3.161</td>
<td>0.1684</td>
<td>1.622</td>
<td>0.282</td>
</tr>
<tr>
<td>2</td>
<td>1357884</td>
<td>3.178</td>
<td>0.1162</td>
<td>1.624</td>
<td>0.179</td>
</tr>
<tr>
<td>3</td>
<td>2404630</td>
<td>3.159</td>
<td>0.0962</td>
<td>1.627</td>
<td>0.0083</td>
</tr>
<tr>
<td>4</td>
<td>4571555</td>
<td>3.156</td>
<td></td>
<td>1.627</td>
<td></td>
</tr>
</tbody>
</table>

Table 4: Numerical method validation.

<table>
<thead>
<tr>
<th>$U_{in}$ ($m \cdot s^{-1}$)</th>
<th>Nu</th>
<th>Deviation %</th>
<th>$fRe$</th>
<th>Deviation %</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.41</td>
<td>2.94</td>
<td>2.914</td>
<td>0.88</td>
<td>18.233</td>
</tr>
<tr>
<td>3.72</td>
<td>2.94</td>
<td>2.961</td>
<td>0.71</td>
<td>18.233</td>
</tr>
<tr>
<td>6.21</td>
<td>2.94</td>
<td>2.923</td>
<td>0.58</td>
<td>18.233</td>
</tr>
<tr>
<td>8.69</td>
<td>2.94</td>
<td>2.935</td>
<td>0.17</td>
<td>18.233</td>
</tr>
</tbody>
</table>

Figure 5: Limiting streamline and temperature contour on the teardrop dimple surface for AW0.5.

leads to the distortion of the limiting streamlines as shown in the case of $U_{in} = 8.69 \, m \cdot s^{-1}$.

The distribution of streamline and temperature counter on the streamwise middle section at $U_{in} = 1.41 \, m \cdot s^{-1}$ with four non-Newtonian nano/liquids, as displayed in Fig. 7 and Fig. 8, illustrates the flow characteristics from another point of view. It is clearly found that at the same inlet velocity, the size of vortex grows gradually with the increase of the solution volume fraction. When the non-Newtonian fluids flow through the teardrop dimple region, the special structure produces low pressure, which makes the flow moves down and forms vortex. It should be noticed that there appears secondary flow structure caused by the non-Newtonian shear thinning effects in the dimple region for the solution of $\varphi = 3.5%$.

As shown in Fig. 8, the flow structure indicates that the vortex appears at the back region of the protrusion structure, because of the flow separation caused by the adverse pressure gradients. With the solution volume fraction increases, the size of the backflow vortex grows gradually bigger. As stated above, the existence of the rear vortex leads to the weakness of the mass exchange and heat transfer, so the temperature in this region is little higher than others. However, the temperature of the mainflow is apparently lower compared with the flow in dimpled channel at the same condition, mainly because the protrusion structure, diminishing the cross section area, makes the velocity increase and enhances the heat transfer of the mainflow. Meanwhile, with the increase of the volume fraction, the temperature of the mainflow is increasing gradually, which indicates the secondary flow effect of non-Newtonian fluids weakens the local heat transfer.
4.2 Heat transfer characteristics

The variations of relative Nusselt number $Nu/Nu_0$ based on the flow of water in smooth channel at same boundary conditions, with the inlet velocity for four solutions are shown in Fig. 7 and Fig. 8 respectively. The relative Nusselt number increases steadily with increasing velocity and the values for all the cases discussed in the present study are bigger than 1.0, which means teardrop dimple and protrusion structures effectively strengthen the heat transfer of $\text{Al}_2\text{O}_3$-water nanofluids compared with water flow. As stated before, a bigger volume fraction leads to a larger vortex in the teardrop dimple/protrusion region, which makes $\text{AW}2.5$ and $\text{AW}3.5$ have better heat transfer performance. Meanwhile, the increasing ratio of $\text{AW}3.5$ is larger than that of $\text{AW}2.5$ for the flow in dimpled microchannel. In the case of the protrusion, it can be seen that the higher volume fraction leads to better heat transfer performance.

4.3 Flow resistance characteristics

The variations of normal Fanning friction factor $f/f_0$ based on the flow of water in smooth passage are presented in Fig. 10. The $f/f_0$ for all the cases investigated in the present study increases with the growth of the inlet velocity. For the flow in dimpled/protrusioned microchannels, the $f/f_0$ of $\text{AW}0.5$ always shows the highest value and that of $\text{AW}3.5$ shows the lowest. As the volume fraction increases, the non-Newtonian shear thinning effect
is strengthened gradually and the development of boundary layer is disturbed in advance, which makes AW3.5 show the best flow characteristics with low resistance loss among the cases discussed in the present study.

4.4 Thermal performance evaluation

It is known that TP is the parameter used to evaluate the heat transfer augmentation quantity [18, 19]. In order to obtain the overall thermal performance, the variation of TP with inlet velocity for all the cases studied is shown in Fig. 11. It is clearly found that TP for these four solutions in these two microchannels all increase gradually with the increase of the velocity. The values of most cases are bigger than 1.0, except the flow of AW0.5 and AW1.5 in dimpled microchannel at relatively low velocity. Comparing all the results, TP of AW0.5 is roughly the lowest and that of AW3.5 is the highest for the specific channel structure. The maximum value of TP has reached 2.59, which indicates AW solution has favorable overall thermal performance, compared with the flow of water in smooth microchannel. In the cases discussed in the present study, AW3.5 solution shows the best thermal performance in the dimpled and protrusioned microchannel. Meanwhile, the increasing ratio of the TP of dimpled cases is mostly higher than that of protrusioned cases.
5 Conclusions

The flow structure and heat transfer behavior of Al\textsubscript{2}O\textsubscript{3} aqueous solutions with four different volume fractions in the teardrop dimpled/protrusioned microchannel with positive eccentricity as $e/D_h = 0.3$ and relative depth as $\delta/D_h = 0.2$ are investigated numerically. The following conclusions can be obtained.

1. The working substance flowing through the teardrop dimpled region is affected by pressure gradient and inertial force, which produces large vortex and backflow. As flow velocity and volume fraction increase, the size and intensity of vortex grows gradually. When the shear-thinning effect is large enough, there is secondary vortex in the dimple region. These characteristics enhance the exchange of mass and energy, which leads to the enhancement of overall thermal performance.

2. There is an apparent flow separation at the trailing edge of protrusion structures when the nanofluids flow through the channel. It is different from the dimpled cases in that the vortex caused by flow separation leads to the weakness of local heat transfer effect. However, the increase of mainstream velocity leads to the enhancement of the overall thermal performance.

3. Normalized Nusselt number $Nu/Nu_0$ is increasing as inlet velocity increases in the range of present study. Comparing all the values studied, the cases of AW2.5 and AW3.5 show the best thermal characteristics. Meanwhile all the values are larger than 1.0, which illustrated that Al\textsubscript{2}O\textsubscript{3}-water nanofluids have superior heat transfer performance than water flowing in smooth microchannel.

4. The normalized Fanning friction factor $f/f_0$ increases with the inlet velocity, based on the flow of water in smooth microchannels. Solutions with higher volume fractions produce lower pressure loss at the same velocity due to the shear-thinning effects and the special flow structure.

5. $TP$ increases gradually as the inlet velocity increases and AW3.5 solution shows the best thermal performance in most cases. The maximum of $TP$ has reached 2.59. In order to obtain the best overall thermal performance, working substances with AW3.5 in the teardrop dimpled/protrusioned microchannel is preferred with the condition stated in the present study.

References


